Practical
NAVIGATION
or
An Introduction
to that whole
ART.
By John Seller
Hydrographer
to the KING.
English Pilot.
R. White sculp:

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Practical Navigation:

OR,

An Introduction to the whole Art.

Containing many Useful and Geometrical Definitions and Problems; The Doctrine of Plain and Spherical Triangles; Plain Mercator, and great Circle-Sayling; Sundry useful Problems in Astronomy; The use of Instruments; The Azimuth-Compass; Ring-Dyal; Variation-Compass; The Fore-Staff, Quadrant, Plow, Cross-Bow-Quadrant, Removing-Quadrant, Nocturnal and Moon Dyals; The Plain Scale; *Gunter*'s-Scale; Sinical-Quadrant; Plain-Chart, Mercators-Chart, both Globes, the Inclinatory Needle, and the Vertues of the Load-Stone; Useful Tables of the Moons Age, of the Tydes, of the Sun's Place, Declination and Right Ascention; of the Stars Right Ascention and Declination; The Latitude and Longitude of Places; A Table of Meridional Parts; New Traverse Tables, and their Use in keeping a Reckoning at Sea: Also a Table of 10000 Logarithms, and of the Log. Sines, Tangents and Secants.

The Second Edition, enlarged.

By *John Seller*, Hydrographer to the King.

LONDON,
Printed by *John Darby*, and are to be sold by the Author, at his Shops, at the *Hermitage* in *Wapping*, and in *Exchange-Alley*, near the Royal-Exchange in *Cornhil*; and by *John Wingfield* Book-seller, in *Crutched-Fryars*, right against the Church, 1672.

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Viro

D. Nicholao Millet

EQUITI AURATO.

Hunc, Secundò Editum, Navigationis Tractatum, in perpetuum obſervantiæ, & gratitudinis Teſtimonium.

D. D. D. *Johannes Sellerus.*

The Preface to the Reader.

Courteous Reader,

I *Have here preſented thee with a ſecond Edition of this Treatiſe, called* Practical Navigation, *wherein ſeveral Emendations and Corrections are made, of Errors that were committed in the firſt Impreſſion; Alſo with ſome Additions that I judged neceſſary, for the better accommodating the Book, and rendering it more generally practicable for the Uſe of Sea-Men: As in the Doctrine of Oblique Spherical Triangles,* Mercators, *and Great-Circle-Sayling. Many uſeful Problems of Aſtronomy; the Variation Compaſs, Plain Scale, and its Uſe in Mercators Sayling; Great-Circle-Sayling, and in Problems of Aſtronomy; a large Table of the Latitudes and Longitudes of Places: The Table of Meridional Parts enlarged, to every Degree and Minute; new Traverſe Tables, and their Uſe in keeping a* Reckoning; *with Tables of Logarithmes, and Artificial Sines, Tangents, and Secants. All which I humbly tender to the favourable and candid Acceptation of the judicious Mariner, and reſt, yours to ſerve you to my power,*

From my Houſe, at the Hermitage Stairs *in* Wapping, *this* 24th *of* November, 1672.

John Seller.

On

On the Practical Navigation of my very good Friend Mr. JOHN SELLER.

YOur Book (kind Sir) I have perus'd, and find
Rich Arguments of an ingenious Mind;
That for our good your Talent will not hide,
But build a *Light-House* Mariners to guide.
What others have in mighty Volumns done,
You neatly here have couched all in one;
Yet is your Book to no great Volumn grown,
Though grac'd with learn'd Additions of your own.
For me to praiſe your Work, might be my blame,
Fearing my meanneſs might diſpraiſe the ſame:
You want not learned Pens, in lofty Verſe,
Your well-deſerved Praiſes to rehearſe.
Mean Artiſts, Men obſcure (and ſuch am I)
Ought t'wiſh and pray for your proſperity.
Yet rouſe (for once) my humble Muſe, and let
The Countrey Oat-Pipe drown the Flajolet;
And 'tis but fitting (ſith your pains in this
To City and to Countrey uſeful is)
That City Poetry, and Countrey Layes,
With joynt conſent ſhould eccho forth your praiſe.
Who doth peruſe your Work, ſhall ſurely find,
The Subject handled well, and well deſign'd.
You much have done in little: here we find,
What in this Art may pleaſe a curious mind.
The *Longitude* excepted: but if we
Your Rules obſerve, obtained it may be
For uſe ſufficient; but the ſame to get,
With certainty, is not diſcovered yet.

Which

Which rare Performance, if that any can
Make plainly out, I wiſh you be the Man.
But ſtay my Muſe, be ſhort, and not ſo rude,
I'le only wiſh you well and ſo conclude.
May theſe your Labours (as they profit all)
Turn to your profit, and your good withall.
May no baſe Plagiarie arrogate
That to himſelf which you by pains have got.
May never Engliſh Man be ſo unkind,
(As famous * *Wright*, and reverend † *Ward* do find)
T' aſcribe to Strangers what you have ſet forth,
Detracting ſo from their and your true worth.
May you encourag'd be, as reaſon is,
To publiſh more ſuch uſeful Works as this.
May you be happy ever, in the end;
Thus prayes your humble Servant, and your Friend,

* Maſter *Wrights* Chart aſcribed to *Mercator*.
†Dr *Wards* Invention of a Triangle in an Ellipſis, & applyed to Aſtronomy, aſcribed to Co. *Pagan*.

Weſterleigh in *Gloceſterſhire*,
ſix miles from *Briſtol*,
Sept. 20. 1672.

Nathaniel Friend.

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Practical Navigation,

OR,

AN INTRODUCTION

TO THE

Whole ART.

NAVIGATION, that uſeful part of the *Mathematicks*, is a Science which has been highly valued by the Antients, eſpecially by our Anceſtors of this Iſland; it being indeed the Beauty and Bulwark of *England*, the Wall and Wealth of *Brittain*, and the Bridge that joynes it to the Univerſe.

It conſiſts of two general Parts.

Firſt, That which may be called the *Domeſtick*, or more ~~common~~ *Navigation*, I mean Coaſting or Sailing along the Shore. This part imploves the Mariners *Compaſs* and *Lead*, as the chief Inſtruments, and for an Introduction of this kind, I refer you to my Book Intituled, *The* ENGLISH PILOT *and* SEA ATLAS, deſcribing the Sea-Coaſts, Capes, Soundings, Sands, Rocks and Dangers; the Bayes, Roads, Harbors, Rivers and Ports, in moſt of the known parts of the World, *Shewing*

the Courſes and Diſtances from one place to another, the ſetting of the Tydes and Currents, the Ebbing and Flowing of the Sea, and many other things belonging to the practick part of Navigation. *Being furniſhed* with new and exact Draughts and Deſcriptions, collected from the experience of divers of *Our able Navigators*, the Like not heretofore publiſhed in *England*.

Secondly, That which may more properly bear the Name, and principally deſerves to be Intituled the ART OF NAVIGATION, is that part thereof which guides the Ship in her courſe through the Immenſe Ocean, to any part of the known world; which cannot be done unleſs it be determined in what place the Ship is at all times, both in reſpect of *Latitude* and *Longitude*; this being the principal care of a *Navigator*, and the *Maſter-piece* of *Nautical Science*.

To the comendable accompliſhment of which knowledge, theſe four things are ſubordinate Requiſites.

Viz. { Arithmetick, Geometry, Trigonometry, and The Doctrine of the Spheres.

For the firſt of theſe, ARITHMETICK, I ſhall refer you to ſome of thoſe Books already extant; the reſt ſhall be here treated of in their order.

CHAP.

CHAP. I.

Containing ſundry uſeful Definitions and Problems of GEOMETRY.

SECT. I.

Geometrical Definitions.

A POINT, is that which cannot be divided, having neither Part nor Quantity, and therfore void of length, breadth, or depth; and is repreſented in the Margine by the Letter A. A.

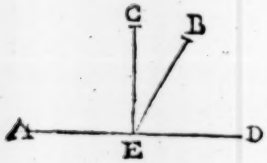
A LINE, is a ſuppoſed length, extending it ſelf without breadth or thickneſs, and is Right, as A,
Or Curved, as B,

An ANGLE, Is the Inclination of two Lines one to another, the one touching the other, yet not ſo as to make one Line.

A RIGHT-LIN'D ANGLE, is that which is contained by right Lines, as the Angle, A B C.

A RIGHT-LIN'D ANGLE, is either Right-angled or Oblique.

A RIGHT-ANGLE, is when a Right Line ſtanding upon a Right Line, makes the Angles on each ſide equal to each other; as the Right Angles A C D, and B C D.



An OBLIQUE-ANGLE, is either Acute or Obtuſe.

An ACUTE-ANGLE, is leſs than a Right, as the Angle D E B.

An OBTUSE-ANGLE, is greater than a Right Angle, as A E B.

A Plain Figure, is contained under one term or many.

A Circle, is a plain Figure contained under one term or Line, called the *Circumference*, unto which all Lines drawn from a certain point within the Figure are equal; and that point is called the Center, as A.

A Right-lin'd Figure, is contained by Right-Lines, and is either three-ſided, four-ſided, or many ſided.

A Triangle, is a three-ſided Figure, and is conſidered either in reſpect of its Sides or Angles.

In reſpect of its Sides, 'tis either,

Equilateral, having three equal Sides; as A.

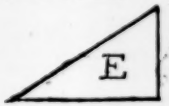
Or *Equicrural*, having two equal Sides, as B.

Or

Or *Scalenum*, having three unequal sides; as D.

In respect of its Angles, 'tis either;

Right-angled, which hath a Right-Angle as E.



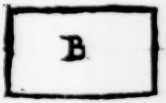
Or *Oblique-angled*, which hath no Right-Angle, but an Obtuse-Angle, as C.

Or three *Acute-Angles*, as G.

Of four-sided Figures.

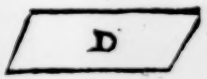
A Square, is that which hath four equal Sides, and four Right-Angles, as A.

An Oblong, hath four Right-Angles, and the opposite sides equal, as B.

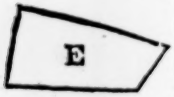


A Rombus, hath four equal Sides, but is not Right-Angled, as C.

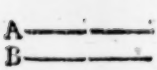
A Romboides, hath the Opposite Sides and Angles equal; but is neither equal-sided, nor Right-angled, as D.



All



All other four-sided Figures are called *Trapezia's*, as E.

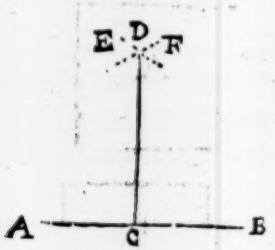


Parallel, or equi-distant Right Lines are such, which being in the same Superficies, if infinitely produced would never meet, as A and B.

Sect. II.

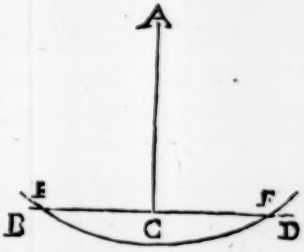
Geometrical Problems.

How to raise a Perpendicular from the middle of a Line given.



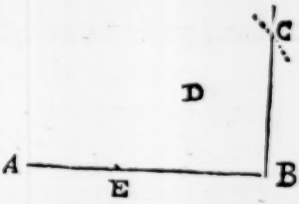
LET the Line given be A B, and let C be a point therein whereon it is required to raise a Perpendicular. First therefore, open the Compasses to any convenient distance, and setting one foot in the Point C, with the other set off on either side thereof the equal distances C A and C B; Then opening the Compasses to any convenient wider distance, setting one foot in the point A, with the other strike the occult Arch at E, then with the same distance set one foot in the point B, and with the other draw the Arch F, crossing E in the point D; from whence draw the Line D C, which Line is a Perpendicular unto the given Line A B as was required.

To let a Perpendicular fall from a Point assigned to the middle of a Line given.



Let the Line given whereupon you would have a Perpendicular let fall, be the Line B C D, and the Point A to be the Point assigned from whence you would have a Perpendicular let fall upon the given Line B C D. First set one foot of your Compasses in the Point A, and opening them to any convenient distance, so that it be more than the Line A C; Describe an arch of a Circle with the other foot so that it may cut the Line B C D twice, that is, at E and F; then finde the middle between these, which will be the Point C, from which Point draw the Line A C, which is the Perpendicular which was to be let fall.

To raise a Perpendicular upon the end of a Line given.

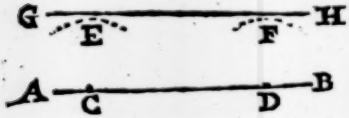


Suppose the Line whereupon you would have a Perpendicular raised, be the Line A B; First open your Compasses to a convenient distance, and set one foot in the Point B, and let the other Point fall any where above the Line, as at the Point D; and in that Point let one foot of your Compasses remain, turning the other about, until it touch the Line A B in the Point E; then turn the same Foot of the Compasses towards C, and draw an occult Arch, and lay the edge of a Ruler to those two Points E and D, and where the same edge of the Ruler doth cut the Arch C, from that Point draw the Line C B, which shall be a Perpendicular at the end of the Line A B.

To let fall a Perpendicular from a Point assigned unto the end of a Line given.

Let the Line A B be given, unto which it is required to let a Perpendicular fall from the assigned Point D, unto the end A. First from the assigned Point D, draw a Line unto any part of the given Line A B, which may be the Line D C E, then find the middle of the Line D E, which is at C, place one foot of your Compasses in that Point, and extend the other foot unto D or E, with which distance draw the Semicircle D A E, which shall cut the given Line A B in the Point A; from which Point draw the Line D A, which is the Perpendicular let fall from the assigned Point D, near the end of the given Line A B, as was required.

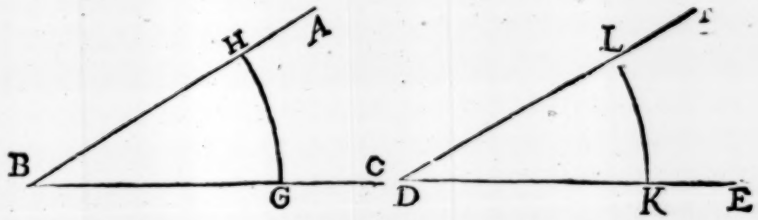
To draw a Line Parallel to a Line given.



Let A B be a Line given, whereunto it is required to draw a Parallel. First set one foot of your Compasses in the Point C, and opening the other foot at pleasure, draw the Arch E; then with the same distance set one Foot in the Point D, and draw the other Arch F; Lastly lay a Rule to the Convexities of both those Arches, and draw the Line G H, which shall be a Parallel, to A B, as was required.

How to make an Angle equal to an Angle given.

Let A B C be the given Angle, draw the Line D E, and upon B as a Center, deſcribe the Arch G H, between the ſides B A and B C, and



upon the Point D, with the ſame extent, deſcribe the Arch K L, and place the extent G H from K to L; then through the Point L, draw D F; ſo is the Angle E D F equal to A B C, which was required.

CHAP. II.

Treateth of the Doctrine of Plain or Right-Lin'd *TRIANGLES.*

SECT. I.

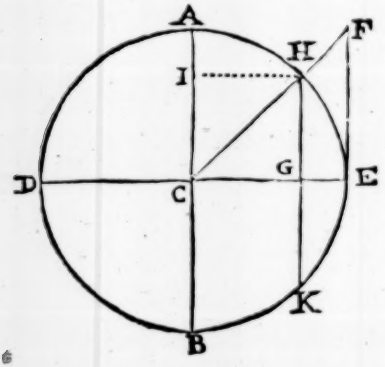
Containing ſome things neceſſary to be underſtood, relating to the Science of Plain Trigonometry.

THE *Doctrine of Triangles* is converſant in the *Menſuration of Triangles Plain or Spherical*, comparing the Sides and Angles together, according to known Analogies; whereby three things being given, either Sides, Angles, or both, a fourth Side or Angle may be found.

But becauſe the Angles of both Plain and Spherical are meaſured by Arches of Circles, and the ſides likewiſe of Spherical Triangles are themſelves Arches of great Circles, therefore theſe Arches are in manner *reduced into the Right Lines applyed thereunto.*

The Right Lines applyed to Circles, are *Chords*, *Sines*, *Tangents* or *Secants*.

A Chord is a Right Line drawn in a Circle, from one part of the Circumference to the other, as in the annexed Figure.



H K is the *Chord* of the Arches H E K and H D K, alſo D E the *Diameter* is the Chord of the *Semicircles* D A E and D B E.

The right Sine of an Arch is half the Chord of twice that Arch, as H G being half the Chord H K, is the right Sine of the Arch H E; alſo of the Arch H A D, the Arch H E being the half of H E K, the Sine Complement of the Arch H E is H I, equal to C G.

The Verſod Sine of an Arch, is that part of the Diameter which lyeth between the right Sine of that Arch and the Circumference, ſo that G E is the Verſod Sine of the Arch H E, and G D the Verſod Sine of the Arch H A D.

The Tangent of an Arch, is a Right Line touching the Arch, being Perpendicular to the Radius drawn to the point of Contacts, and concurring with a Line drawn from the Center, through the term or end of that Arch; ſo E F is a Tangent of the Arch E H.

A Se-

A Secant is that Right Line drawn from the Center of the Arch until it meet with the Tangent; So C F is a Tangent of the Arch E H.

It is to be underſtood that every Circle is divided into 360 equal parts, called Degrees, every Degree into 60 parts, called Minutes, and every Minute into 60 parts, called Seconds, *&c.*

The Complement of an Arch or Angle, is commonly the Complement thereof to (or that which makes it up) 90 Deg. But if it be ment the Complement thereof to a Semi-Circle, it's expreſſed by the Complement to 180 deg.

A Plain Triangle is contained under three right Lines, and is either Right-Angled or Oblique.

In all Plain Triangles, two Angles being given, the third is alſo given: And one Angle being given, the Sum of the other two is alſo given; becauſe the three Angles together are equal to two right Angles.

Therefore in a Plain Right-Angled Triangle, one of the Acute Angles is the Complement of the other, to 90 deg.

In the ſolution of Plain Triangles, the Angles being onely given, the Sides cannot be found, but only the reaſon of the Sides: It is therefore neceſſary that one of the Sides be known.

In a Right-Angled Triangle two Terms (beſides the Right-Angle) will ſerve to find the Third, ſo one of them be a Side.

In Oblique-Angled Triangles there muſt be three things given to find a fourth.

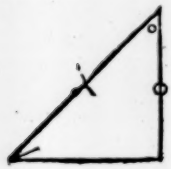
Some Symbols uſed in the Doctrine of Triangles, for brevities ſake.

= Equal to.
+ More.
− Leſs.
× Multiplyed by, or drawn into.
° Over a Number, ſtands for Degrees as 12° ſignifies 12 deg.
′ Signifies Minutes, as 12′ is 12 Minutes.
cr. A Side. cr^{s} Sides.
V An Angle. *V V* Angles.
Z The Sum.
X The Difference.
S Sine.
Sc Co-Sine, or Sine Complement.
Co.Ar. Complement Arithmetical.

t Tangent.
tc Co-Tangent, or Tangent Complement.
2 R Ang. Two right Angles.
Q Square.

In Right-Angled Plain Triangles, the Sides comprehending the Right Angle are called the *Legs*, and the Side ſubtending (or oppoſite to) the Right Angle, is called the *Hypothenuſe*.

In the Doctrine of Triangles, three Letters denote an Angle, as B A C ſignifies the Angle at A. A C B the Angle at C. Two Letters ſhew a Side, as Side A B, or A C.



In the Doctrine of Triangles, the given Sides or Angles are noted with a daſh thus (′)

The required Sides or Angles with a Cypher thus (o)

In Right-angled Plain Triangles there are ſeven Caſes, and five in Oblique. For the Solution of which, theſe four *Axiomes* are ſufficient.

Axiome 1.

Of Right-Angled Triangles.

In all Plain Right-angled Triangles any of the Sides may be put as Radius; and the other Sides will be as Sines, Tangents or Secants.

Axiome. II.

Of Oblique Triangles.

In all Plain-Triangles the Sides are in ſuch proportion one to annther as are the Sines of their oppoſite Angles.

Axiome III.

In all Plain Triangles, As the Sum of two Sides is to their difference, ſo is the Tangent of the half Sum of their two oppoſite Angles, to the Tangent of the difference of either of them, above or under the half Sum.

Axiome IV.

In all Plain Triangles, As the true Baſe is in proportion to the Sum of the other Sides, ſo is the difference of theſe Sides, to the difference of the Segments of the Baſe.

SECT. II.

Of Right-angled Plain Triangles.

1. Caſe.

THE Angles and one of the Leggs given, to find the other Leg.

Example.

In the Triangle A B C,
There is given
B A C, 33° 45'. } B C required.
A B, 90. }

Tho

The Operation by the Logarithme.

As S. ABC, 56° 15′ Log.	9.91984
To AB, 90°	1.95424
So is S. BAC, 33° 45′	9.74473
	11.69897
To BC required, 60	1.77913

The General Rule for working Proportions by the Logarithms.

Add the Log^s. of the second and third Numbers together; From that Sum Substract the Log. of the first, and the remainder is the Log. of the fourth Number sought; as is apparent by the precedent Operation.

The work may be abreviated in this Case, and the succeeding, when Radius is not one of the Terms in the Proportion, by taking the Complement Arithmetical of the Logarith. of the first Number; and then adding the Logarithms of the second and third, and the Complement Arithmetical of the first into one Sum, from which bating Radius (or a Unite towards the left hand) the remainder is the Log. of the fourth number.

The Operation by the Compl. Arith.

	Co. Ar.
As S. ACB. 56° 15′. Log.	0.08016
To AB 90	1.95424
So is S. BAC, 33° 45′	9.74473
To BC required, 60	11.77915

The *Comp. Arith.* of a Log. is the Remainder thereof, being substracted from Radius;

So the Comp. Arith. of S. 56° 15′	10.00000
	9.91984
is 0.08016, as here appears.	0.08016

But

But a readier way is hinted by Mr. *Norwood*, thus: By taking the Compl. or reſidue of the firſt figure towards the left hand unto 9, and ſo of the reſt, until you come to the laſt figure towards the right hand, thereof ſet down the reſidue to 10, thus; To take the Compl. Arith. of 9.91984. For 9 I write his reſidue unto 9, which is 0; for 9, 0; for 1, 8; for 9, 0; for 8, 1; for 4, the Compl. to 10, which is 6. And ſo I have 0.08016, which is the Compl. Arith. of 9.91984, unto 10.00000.

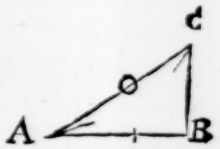
How to work this and the following Caſes by *Gunters Scale*, ſhall be ſhewn in the uſe of that Inſtrument.

II. Caſe.

The Angles and one of the Legs given, to find the *Hypothenuſe*.

Example.

In the Triangle A B C,
There is given,
A C B, 56° 15′, } A C required.
A B, 90,



The Operation.

As S. A C B, 56° 15′ Log.	9.91984
To A B 90.	1.95424
So is Radius,	10.00000
To A C required, 108.	2.03440

In the Operation of the precedent Caſe, there's no need to take the Compl. Arith. becauſe Radius is one of the four Terms in the proportion; nor of adding the Log^s. of the ſecond and third together, according to the General Rule aforegoing; onely Subſtract the former figures of the firſt Log. from the ſecond Log. And in Subſtracting the laſt figure of the firſt Log. add 10 to the correſponding figure of the ſecond Log. *Viz.*

Say, 9 from 11, there remaines 2; This difference 2.03440, gives the Log. of the Fourth number enquired.

III. Caſe.

III. Case.

The Angles and *Hypothenuse* given, to find either of the Legs.

Example.

In the Triangle A B C,
There is given,
ACB 56° 15′ } AB required.
AC 108 }

The Operation.

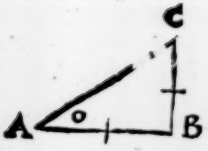
As Radius,	10.00000
To A C 108,	2.03342
So is S. A C B 56° 15′,	9.91984
To A B required, 90.	11.95325

In this Operation, the second and third Log^{s}. being added together, the first being Radius is easily Substracted, by cutting off the last figure towards the left hand, as is evident in the former Example.

IV. Case.

The Legs given, to find the Angles.

Example.



In the Triangle A B C.
There is given
A B 90 } B A C required.
B C 60 }

The

The Operation.

As A B 90	1.95424
To Radius	10.00000
So is B C 60	1.77815
To t. B A C required, 33° 41′	9.82391

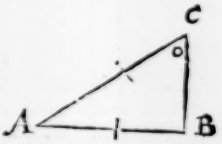
This Operation is performed as the Example in the second Case beforegoing.

V. Case.

The *Hypothenuse* and one of the Legs given, to find the Angles.

Example.

In the Triangle A B C,
There is given,
A C 108,
A B, 90, } A C B required.



The Operation.

As A C 108.	2.03342
To Radius,	10.00000
So is A B 90.	1.95424
To S. A C B required, 56° 26′	9.92082

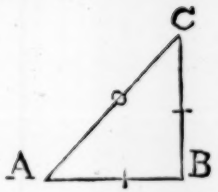
This is performed as the precedent Operation in the fourth Case.

VI. Case.

The Legs given, to find the *Hypothenuse*.

In the Triangle A B C
There is given,

A B 90 }
B C 60 } A C required.



This Case requires a double Operation.
1. By the 4th Case to find the Angles.
2. By the 2d Case to find the *Hypothenuse*.

The first Operation.

As A B 90	1.95424
To Radius	10.00000
So is B C 60	1.77815
To t. B A C, 33° 41′	9.82391

The second Operation.

As S. B A C 33° 41′	9.74398
To B C 60	1.77815
So is Radius	10.00000
To A C required, 108	2.03417

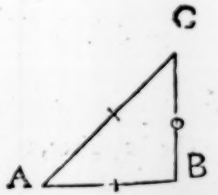
VII. Case.

The *Hypothenuse* and one of the Legs given, to find the other Leg.

Example.

In the Triangle A B C
There is given,

A C 108 }
A B 90 } B C required.



This

This Caſe likewiſe requires a double operation.

1. By the 5th Caſe to find the Angles.

2. By the 1ſt or 2d Caſe to find the Leg required.

The firſt Operation.

As A C 108	2.03342
To Radius	10.00000
So is A B 90	1.95424
To S. A C B 56° 26′	9.92082

The ſecond Operation.

As Radius	10.00000
To A C 108	2.03342
So is S. B A C 33° 34′	9.74265
To B C required, 59	✗1.77607

The ſixth and ſeventh Caſes beforegoing may be performed without the Canon of Sines and Tangents, by the 46 Prop. 1. *Euclid, viz.* That in Plain Right-angled Triangles, the ſquare of the *Hypothenuſe* is equal to the Sum of the ſquares of the two Legs.

Example of the 6th Caſe.

In the Triangle A B C
There is given,
A B 90 }
B C 60 } A C required,

Square the given Legs ſeverally, add their Squares together, the ſquare Root of that Sum is the *Hypothenuſe* required.

The Operation.

AB 90	BC 60	Square AB 8100
90	60	Square BC 3600
00	00	11.700 (108 AC req.
810	360	1
Square 8100	Square 3600	20) 17
		00
		208) 1700
		1664
		36

Otherwise by the Logarithms.

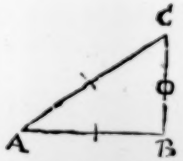
From the doubled Log. of the greater Leg, Subſtract the Log. of the leſs, and to the abſolute number anſwering to the difference of the Log^{s}. add the leſs Leg; half the Sum of theſe Log^{s}. of the ſaid Sum and leſs Leg, is the Log. of the *Hypothenuſe* required.

The Operation.

The greater Leg. AB 90 Log.	1.95424
The ſame again.	1.95424
The doubled Log.	3.90848
The leſs Leg. BC 60. Log. Subſtr.	1.77815
The abſolute Number 135	2.13033
The Sum. 195 Log.	2.29003
Leſs Leg. BC 60 Log.	1.77815
Sum.	4.06818
The *Hypothenuſe* AC 108 $\frac{1}{2}$ Sum,	2.03409

Example of the 7th. Caſe.

In the Triangle ABC
There is given,
AC 108 }
AB 90 } BC required.



From

From the ſquare of the *Hypothenuſe*, Subſtract the ſquare of the given Leg, the ſquare Root of the remainder is the Leg required.

The Operation.

A C 108	A B 90	Square A C 11664
108	90	Square A B 8100
864	00	Remainder 3564 (59
000	108	25
108	Square 8100	109) 1064
Squ. 11664		981
		83

Otherwiſe by the Logarithms.

Halfe the Sum of the Log^s. of the Sum, and of the difference of the *Hypothenuſe* and given Leg, is the Log. of the Leg required.

The Operation.

The *Hypothenuſe* A C 108		
The given Leg A B 90		
The Sum 198	Log.	2.29666
The Differ. 18	Log.	1.25527
	Sum	3.55193
The Leg B C 59 required, ½ Sum		1.77596

Sect.

SECT. III.

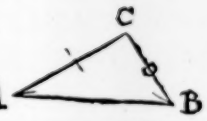
Of Oblique-angled Plain Triangles.

Case. I.

THE Angles and one of the Sides given, to find one of the other Sides.

Example.

In the Triangle A B C
There is given,
B A C 33° 45′
A B C 45 00
A C 40
} B C requir.



The Operation of this and the following Case, depends upon the second *Axiome* aforegoing.

The Operation.

	Co. Ar.
As S. A B C 45° 00′	0.15052
To Side A C 40	1.60206
So is S. B A C 33° 45′	9.74473
To Side B C required, 31.	*x* 1.49731

After the same manner you might find the Side A B if it were required.

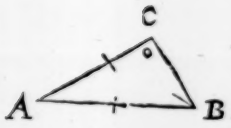
Case II.

Two Sides and an Angle opposite to one of them being given, to find the other opposite Angle.

Example.

Example.

In the Triangle A B C,
There is given
A B C 45° 00′
A B 100
A C 80
} A C B required, being Obtuſe.



1. In this Caſe, if the given Angle be Obtuſe, the Angle required is is Acute.

2. If the given Angle be Acute and Oppoſite to the greater of the given ſides, the required Angle is Acute.

3. If the given Angle be Acute and Oppoſite to the leaſt of the given Sides, it's doubtful whether the Angle ſought be Acute or Obtuſe, and ought to be determined before the Operation, as in the precedent *Example.*

The Operation.

	Co. Ar.
As Side A C 80	8.09691
To S. A B C 45° 00′	9.84948
So is Side A B 100	2.00000
To S. A C B required, 117° 54′	9.94639

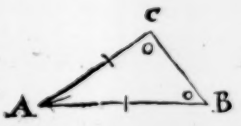
In this Operation the Table produces 62° 06′ for the Angle ſought, but becauſe it is Obtuſe you muſt take its Complement to 180°, *viz.* 117° 54′.

Caſe. III.

Two Sides and their contained Angle given, to find the other Angles.

Example.

In the Triangle A B C
There is given,
A B 25
A C 20
B A C 30 33° 45′
} A C B & A B C required.



The Operation of this Caſe depends upon the third *Axiom.*

The

The Operation.

The Side A B 25		180° 00′	
The Side A C 20	BAC	33 45	
The Sum of the Sides 45	Sum	146.15	
Their difference, 05	½ Sum	73.07	of the unknown Angles.

		Co. Ar.
As the Sum of the Sides A B and A C, 45	Log.	8.34679
To their Difference	5	0.69897
So is r. ½ Sum of the Opposite Angles 73°. 07′		10.51783
To t of their half Difference	20 06	9.56359

The half Difference added to the half Sum, gives the greater Angle; and Subſtracted, leaves the leſs.

The ½ Sum of the Angles	73° 07′
The ½ Difference	20 06
Added, gives A C B	93 13
Subſtracted, A B C	53 01

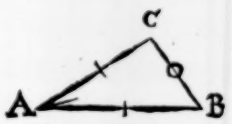
Caſe. IV.

Two Sides and their contained Angle given, to find the third Side.

Example.

In the Triangle A B C
There is given,

A B 335
A C 271 } BC required,
B A C 14° 40′



This Caſe requires a double Operation.

1. By the 3d Caſe, to find the Angles.
2. By the 1ſt Caſe, to find the Side required.

The

The first Operation.

	Co. Ar.
As the Sum of the Sides A B and A C 606 Log.	7.21753
To their Difference, ——— 64 ———	1.80618
So is t ½ Sum Angles ——— 82°40′ ———	10.89044
To t ½ their Difference ——— 39 22 ———	x9.91415

By which you will find the Angle A B C to be 43° 18′

The second Operation.

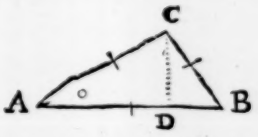
	Co. Ar.
As S. A B C 43° 18′ Log. ———	0.16379
To Side A C 271 ———	2.43296
So is S. B A C 14° 40′ ———	9.40345
To Side B C required 100 ———	x2.00020

V. Case.

Three Sides given, to find an Angle.

Example.

In the Triangle A B C.
There is given
A B 64
A C 47 } B A C required.
B C 34



The Resolution of this Case depends upon the 4th *Axiome*, reducing the Oblique-angled Triangle into two Right-angled Triangles, by letting fall the Perpendicular C D, upon the greater Side adjacent to the Angle sought, and requires a double Operation.

The Base is that Side upon which the Perpendicular falls.

1. To find the Segment of the Base, as A D,
2. By the 5th Case of Rectangulars, to find the Angle required.

The first Operation.

			Co. Ar.
A C 47	As the Base A B	64	Log. 8.19382
B C 34	To the Sum of the Sides AC & BC	81	1.90848
Sum, 81	So is the Difference	13	1.11394
Diff. 13	To a Segment of the Base	16	1.21624

The Base is 64
The Segment 16
Sum, 80

½ Sum 40, is A D the greater Segment of the Base, because adjacent to the greater Side A C.

The second Operation.

In the Triangle A C D, Right-angled at D,
There is given A D and A C, to find C A D or C A B.

As A C 47	Log.	1.67209
To Radius		10.00000
So is A D 40		1.60206
To sc. C A D 31° 40′		9.92997

CHAP.

CHAP. III.

Concerning the Doctrine of Spherical Triangles.

SECT. I.

Containing the Affections of Spherical Triangles, and their Axioms.

I.

A Spherical Triangle is that which is described on the surface of the Sphere.

2. The Sides of a Spherical Triangle are the Arches of three great Circles of the Sphere mutually intersecting each other.

3. The Measures of Spherical Triangles are Arches of great Circles, described from the Angular Point, between the Sides of the Angles, those sides being continued to Quadrants.

4. Those are said to be Great Circles which bisect the Sphere.

5. Those Circles which cut each other at Right-Angles, the one of them passeth through the Poles of the other, and the contrary.

6. In every Spherical Triangle each Side is less than a Semicircle.

7. In every Spherical Triangle any two Sides are together greater than the third.

8. The Sum of the Sides of a Spherical Triangle are leſs than two Semicircles.

9. If two Sides of a Spherical Triangle be equal to the Semicircle, the two Angles at the Baſe ſhall be equal to two right; if they be leſs than a Semicircle, the two Angles ſhall be leſs than two right: But if greater than a Semicircle, the two Angles ſhall be greater than two right.

10. The Sum of the three Angles of a Spherical Triangle are greater than two Right Angles, and leſs than ſix.

11. Two Angles of any Spherical Triangle, are greater than the difference between the third Angle and a Semicircle: Therefore,

12. Any Side being continued, the Exterior Angle is leſs than the two Interior oppoſite ones.

13. In any Spherical Triangle, the difference of the ſum of two Angles and a whole Circle, is greater than the difference of the third Angle and a Semicircle.

14. In any Spherical Triangle, one Side being produced, if the other two Sides be equal to a Semicircle, the outward Angle ſhall be equal to the inward oppoſite Angle upon the Side produced: If they be leſs than a Semicircle, the outward Angle ſhall be greater than the inward oppoſite Angle; If they be greater than a Semicircle, the outward Angle ſhall be leſs than the inward oppoſite Angle.

15. A Spherical Triangle is either Right or Oblique-Angled.

16. A Right-Angled Spherical Triangle, is that which hath one Right Angle at the leaſt.

17. The Legs of a Right-angled Spherical Triangle are of the ſame Affection with their oppoſite Angles.

18. In a Right-angled Spherical Triangle, if either Leg be a Quadrant, the *Hypothenuſe* ſhall be alſo a Quadrant; but if both the Legs ſhall be of the ſame affection, the *Hypothenuſe* ſhall be leſs than a Quadrant; or if different, then greater, and the contrary.

19. In a Right-angled Spherical Triangle, if either the Angles at the *Hypothenuſe* be a Right Angle, the *Hypothenuſe* ſhall be a Quadrant; but if both ſhall be of the ſame Affection, it ſhall be leſs; if of different, it ſhall be greater, and the contrary.

20. In a Right-angled Spherical Triangle, either of the Oblique Angles is greater than the Complement of the other, but leſs than the difference of the ſame Complement to a Semicircle.

21. An Oblique Spherical Triangle is either Acute or Obtuſe.

22. An Acute-angled Spherical Triangle hath all its Angles Acute.

23. An

23. An Obtuſe angled Spherical Triangle hath all its Angles either Obtuſe or mixt, *viz.* Acute or Obtuſe.

24. In any Spherical Triangle whoſe Angles are all Acute, each ſide is leſs than a Quadrant.

In all Spherical Triangles there are 28 Caſes. Sixteen in Rectangular, and twelve in Oblique-Angular. Whereof all the Rectangular, and ten of the Oblique-Angular may be reſolved by theſe two *Axiomes* following.

Ariome 1.

In all Spherical Rectangled Triangles, having the ſame acute Angle at the Baſe, the Sines of the *Hypothenuſa's* are proportional to the Sines of their Perpendiculars.

Ariome. 11.

In all Spherical Rectangled Triangles, having the ſame Acute Angle at the Baſe, the Sines of the Baſes, and the Tangents of the Perpendiculars are proportional.

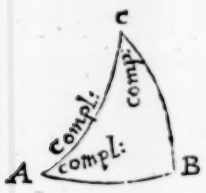
That all the Caſes of a Right-angled Spherical Triangle may be reſolved by theſe two *Axiomes*. The ſeveral parts of the Spherical Triangle propoſed, muſt ſometimes be continued to Quadrants, that ſo the Angles may be turned into Sides, the *Hypothenuſaes* into Baſes and Perpendiculars, and the contrary. By which means the Proportions, as to the parts of the Triangle given, in ſtead of Sines do ſometimes fall in Co-Sines: and ſometimes in Co-tangents in ſtead of Tangents. Such converſions as do for the moſt part change their Proportion, are noted with their Complements (*viz.*) the *Hypothenuſe*, and both the acute Angles; but the Sides containing the Right Angle are not ſo noted.

And theſe are called the five Circular parts of a Triangle amongſt the which, the right Angle is not reckoned, and therefore the two ſides which do contain it, are ſuppoſed to be joyned together.

Each of theſe Circular parts may by ſuppoſition be made the middle part, and then the two circular parts which are next to that middle part, are the Extreams Conjunct; the other two remote from the part aſſumed are the Extreams disjunct.

As in the Triangle A B C, if Comp. A C be made the middle part, Comp. A and Comp. C are the Extreams Conjunct, and the Sides A B and B C are the Extreams Disjunct; and ſo of the reſt, as in the Table following.

A Compl.



Mid. part.	*Extr. Conj.*	*Extr. Disj.*
Leg. A B	*Comp.* A *Leg.* B C	*Comp.* A C *Comp.* C
Comp. A	*Comp.* A C *Leg.* A B	*Comp.* C *Leg.* B C
Comp. A C	*Comp.* A *Comp.* C	*Leg.* A B *Leg.* B C
Comp. C	*Comp.* A C *Leg.* B C	*Comp.* A *Leg.* A B
Leg. B C	*Comp.* C *Leg.* A B	*Comp.* A. *Comp.* A C

The parts of a Right-angled Spherical Triangle being thus distinguished into five Circular parts, for the more ease in resolving of all Spherical Triangles, observe this Catholick and Universal Proposition invented by the Lord *Nepair*.

The Sine of the Middle part and Radius, are reciprocally proportional with the Tangents of the Extreams Conjunct, and the Co-Sines of the Extreams Disjunct.

That is, As Radius to the Tangent of one of the Extreams Conjunct, so is the Tangent of the other Extream Conjunct to the Sine of the Middle Part.

And also, As Radius to the Co-Sine of one of the Extreams Disjunct, so is the Co-Sine of the other Extream Disjunct, to the Sine of the Middle Part.

Therefore if the Middle Part be sought, the Radius must be in the first place; if either of the Extreams, the other Extream must be in the first place.

Only

Only note, That if the Middle Part, or either of the Extreams Conjunct be noted with its Complement in the Circular parts of the Triangle in ſtead of the Sine or Tangent, you muſt uſe the Co-Sine or Co-Tangent.

If either of the Extreams Disjunct be noted by its Complement in the Circular parts of the Triangle; in ſtead of the Co-Sine, you muſt uſe the Sine of ſuch Extream Disjunct.

That the Directions may be the better underſtood, there is in the Table following ſet down the Circular parts of a Triangle under their reſpective Titles, whether they be taken for the Middle part, or for the Extreams, Whether Conjunct or Disjunct; and unto thoſe parts there is prefixed the Sine and Co-Sine, the Tangent or Co-Tangent, as it ought to be by the former Rules.

Mid. Part.	*Extr. Conj.*	*Extr. Disj.*
Sine A B	*Co-Tan.* A *Tan.* B C	*Sine* A C *Sine* C
Co-Sine A	*Co-Tan.* A C *Tan.* A B	*Sine* C *Co-Sin.* B C
Co-Sin. A C	*Co-Tan.* A *Co-Tan.* C	*Co-Sin.* A B *Co-Sin.* B C
Co-Sin. C	*Co-Tan.* A C *Tan.* B C	*Sine* A *Co-Sin.* A B
Sine B C	*Co-Tan.* C *Tan.* A B	*Sine* A *Sine* A C

Axiome III.

In all Spherical Triangles, the Sines of their Sides are in direct proportion, to the Sines of their oppoſite Angles; and the contrary.

Axiome IV.

As the Sine of half the Sum of two Sides,
To the Sine of half their Difference;
So is the Co-Tangent of half the Contained Angle,
To the Tangent of half the Difference of the other Angles.

Again,

Again,

As the Co-Sine of half the Sum of the Sides,
To the Co-Sine of half their Difference;
So is the Co-Tangent of half the contained Angle,
To the Tangent of half the Sum of the other Angles.

Axiome. V.

As the Sine of half the Sum of two Angles,
To the Sine of half their Difference;
So is the Tangent of half the interjacent Side,
To the Tangent of half the Difference of the other Sides.

Again.

As the Co-Sine of half the Sum of the Angles,
To the Co-Sine of half their Difference;
So is the Tangent of half the interjacent Side,
To the Tangent of half the Sum of the other Sides.

Axiome VI.

As the Rectangle of the Sines of the containing Sides,
To the Square of Radius;
So is the Rectangle of the Sines of half the Sum of the three Sides, and of the Difference of the Base therefrom,
To the Square of the Co-Sine of half the Angle sought.

These things being premised, the several Cases shall be set down with their Analogies.

First, Of *Right-angled Triangles.*
Then, of *Oblique.*

SECT. II.

Of Right-Angled Spherical Triangles.

Case I.

A Leg, and an Angle opposite thereto, being given, to find the other Leg: if it be known, whether the *Hypothenuse* or other Angle be greater or less than a Quadrant.

Example.

In the Triangle A B C,
There is given,
B A C 23° 30′ } A B required.
B C, 17 43 }

The Operation.

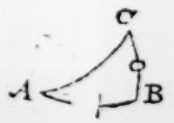
As Radius, ——————— Log. 10.00000
To tc. B A C 23° 30′ —— 10.36170
So is t. B C 17 43 ——— 9 50442
To s. A B required, 47° 19′ — *x* 9.86612

Case II.

A Leg and an adjacent Angle given, to find the other Leg.

Example.

In the Triangle A B C
There is given,
B A C 23° 30′ } B C required,
A B 47 19 }



The Operation.

As tc BAC 23° 30′ —— Log. 10.36170
To Radius —— 10.00000
So is S. AB 47° 19′ —— 9.86635
Tot. BC required, 17° 43′ —— 9.50465

Case III.

The Legs given, to find an Angle.

Example.

In the Triangle A B C,
There is given,
AB 47° 19′ } BAC required.
BC 17 43 }

The Operation.

As t. BC 17° 43′ —— Log. 9.50442
To Radius —— 10.00000
So is f. AB 47° 19′ —— 9.86635
To tc. BAC required 23° 30′ —— 10.36193

Case IV.

The *Hypothenuse* and a Leg given, to find the contained Angle.

Example.

In the Triangle ABC
There is given,
AC 49° 48′ } ACB required.
BC 17 43 }

The

The Operation.

As Radius	Log. 10.0 0000
To tc. A C 49° 48′	9.92689
So is t. B C 17° 43′	9.50442
To ſc. A C B required, 74° 20′	9.43131

Caſe. V.

A Leg and the adjacent Angle given, to find the *Hypothenuſe.*

Example.

In the Triangle A B C
There is given,
B A C 23° 30′ } A C required,
A B 47 19 }

The Operation.

As t. A B 47° 19′	Log. 10.03516
To Radius	10.00000
So is ſc. B A C 23° 30′	9.96240
To tc. A C required, 49° 47′	9.92724

Caſe. VI.

The *Hypothenuſe* and an Angle given, to find the Leg adjacent to the given Angle.

Example.

In the Triangle A B C
There is given,
A C B 74° 19′ } B C required
A C 49 48 }

The Operation.

As tc. A C 49° 49′ ———	Log. 9.92689
To Radius ———	10.00000
So is sc. A C B 74° 19′ ———	9.43188
To t. B C required, 17° 44′ ———	9.50499

Case. VII.

The Oblique Angles given, to find the *Hypothennse.*

Example.

In the Triangle A B C
There is given,
A C B 74° 19′
B A C 23 30 } A C required.

The Operation.

As Radius ———	Log. 10.00000
To tc. A C B 74° 19′ ———	9.44836
So is tc. B A C 23° 30′ ———	10.36170
To sc. A C required, 49° 47′ ———	9.81006

Case. VIII.

The *Hypothennse* and one of the Angles given, to find the other Angle.

Example.

In the Triangle A B C
There is given,
A C B 74° 19′
A C 49° 48′ } B A C required.

The

The Operation.

As tc. A C B 74° 19′ —— Log. 9.44836
To Radius —— 10.00000
So is ſc. A C 49° 48′ —— 9.80987
To ſ. tc. B A C required, 23° 30′ —— 10.36151

Caſe. IX.

The *Hypothenuſe* and an Angle given, to find the Leg oppoſite to the given Angle.

Example.

In the Triangle A B C,
There is given
B A C 23° 30′ } B C required,
A C 49 48 }

The Operation.

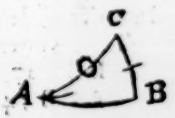
As Radius —— Log. 10.00000
To ſ. B A C 23° 30′ —— 9.60070
So is ſ. A C 49 48 —— 9.88298
To ſ. B C required, 17° 43′ —— 9.48368

Caſe X.

A Leg and an Angle oppoſite thereto being given, to find the *Hypothenuſe*; if it be known whether it, or the other Leg or unknown Angle be greater or leſs than a Quadrant.

Example.

In the Triangle A B C
There is given
B A C 23° 30′ } A C required.
B C 17 43 }



The Operation.

As s. BAC 23° 30′ ——— Log. 9.60070
To Radius ——— 10.00000
So is s. BC 17° 43′ ——— 9.48332
To s. AC required, 49° 45 ——— 9.88262

Case. XI.

The *Hypothenuse* and a Leg given, to find the Angle oppofite to the given Leg.

Example.

In the Triangle ABC
There is given,
AC 49° 48′ } BAC required.
BC 17 43 }

The Operation.

As s. AC 49° 48′ ——— Log. 9.88298
To Radius ——— 10.00000
So is s. BC 17° 43′ ——— 9.48332
To s. BAC required, 23° 28′ ——— 9.60034

Case XII.

A Leg and an Angle adjacent thereunto being given, to find the other Angle.

Example.

In the Triangle ABC
There is given
BC 17° 43′ } BAC, required.
ACB 74 19 }

The Operation.

As Radius	Log.	10.00000
To ſ. A C B 74° 19′		9.98352
So is ſc. B C 17 43		9.97890
To ſc. B A C required, 23 30		9.96242

Caſe XIII.

A Leg and an Angle oppoſite thereto being given, to find the other Angle; if it be known whether it, the other Leg, or the *Hypothenuſe* be greater or leſs than a Quadrant.

Example.

In the Triangle A B C
There is given
B A C 23° 30′ } A C B required,
B C 17 43 }

The Operation.

As ſc. B C 17° 43′	Log.	9.97890
To Radius		10.00000
So is ſc. B A C, 23° 30′		9.96240
To ſ. A C B required 74° 19′		9.98350

Caſe XIV.

The Oblique Angles given, to find either Leg.

Example.

In the Triangle A B C.
There is given
A C B 74° 19′ } B C required,
B A C 23 30 }

The

The Operation.

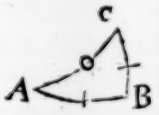
As ſ. A C B 47° 19′	Log. 9.98352
To Radius	10.00000
So is ſc. B A C 23° 30′	9.96242
To ſc. B C required, 17° 43′	9.97890

Caſe XV.

The Legs given, to find the *Hypothenuſe.*

Example.

In the Triangle A B C
There is given
A B 47° 19′ } A C required,
B C 17 43 }



The Operation.

As Radius	Log. 10.00000
To ſc. A B 47° 19′	9.83119
So is ſc. B C 17 43	9.97890
To ſc. A C required 49° 47′	9.81009

Caſe XVI.

The *Hypothenuſe* and a Leg given, to find the other Leg.

Example.

In the Triangle A B C
There is given
A C 49° 48′ } A B required,
B C 17 43 }

The Operation.

As sc. BC	17° 43′	Log. 9.97890
To Radius		10.00000
So is sc. AC	49° 48′	9.80987
To sc. AB required,	47° 21′	9.83097

SECT. III.

Of Oblique-angled Spherical Triangles.

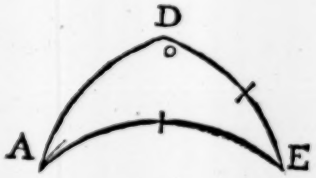
Case I.

To find the ..d an Angle oppofite to one of them, being given, to oppofite Angle; if it be known, whether the Angle fought be greater or leſs than a right-Angle.

Example.

In the Triangle ADE
There is given

AE 69° 47′ } ADE required,
DE 38 28 } being Obtuſe.
DAE 37 03 }



The Operation.

		Co. Ar.
As ſ. DE	38° 28′	Log. 0.20617
To ſ. DAE	37 03	9.77996
So is ſ. AE	69 47	9.97238
To ſ. ADE required,	114° 39′	9.95851

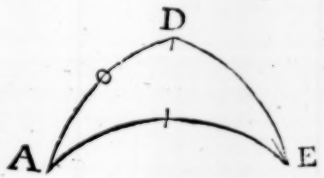
Case II.

Two Angles and a Side oppoſite to one of them being given, to find the other oppoſite Side; if it be known, whether it be greater or leſs than a Quadrant.

Example.

In the Triangle A D E,
There is given,

A D E 114° 38′ } A D required
A E D 45 00 } being leſs than
A E 69 47 } a Quadrant.



The Operation.

	Co. Ar.
As ſ. A D E 114° 38′ ——	Log. 0.04144
To ſ. A E 69 47 ——	9.97238
So is ſ. A E D 45 00 ——	9.84948
To ſ. A D required, 46° 53′ ——	*9.86330

The Reſolution of this and the former Caſe depends upon the third *Axiome.*

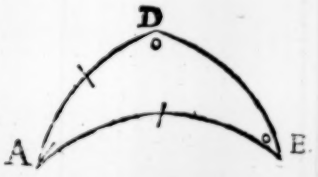
Case III.

Two Sides and their contained Angle being given, to find the other Angle.

Example.

In the Triangle A D E
There is given,

D A E 37° 03′ } A D E }
A E 69 47 } & } required.
A D 46 53 } A E D }



The Operation.

A E 69° 47′
A D 46 53
Sum, 116 40 ½ Sum 58° 20′
Differ. 22 54 ½ Differ. 11 27
D A E 37° 03′, half thereof is 18° 31′

		Co. Ar.
As s. ½ Z cr. A E and A D	58° 20′	Log. 0.07001
To s. ½ X cr.	11 27	9.29779
So is tc. ½ D A E	18 31	10.47506
To t. ½ X V V D and E	34 51	9.48286

		Co. Ar.
As sc. ½ Z cr. A E and A D	58° 20′	Log. 0.27986
To sc. ½ X cr.	11 27	9.99127
So is tc. ½ D A E	18 31	10.47506
To t. ½ Z V V D and E	79 49	10.74619

½ Z V V D and E 79° 49′
½ X V V 34 51
Sum, 114 40 A D E
Rem. 44 58 A E D } required.

Having by the fourth *Axiome*, found the half Sum and half-Difference of the Angles, if to that half Sum, you add the half-Difference, the Total is the greater Angle; and if from the half-Sum you Subſtract the half-Difference, the Remainder is the leſſer Angle ſought.

Note.

If the ſum of the two containing Sides exceed a Semicircle, then Subſtract each Side ſeverally from 180°, and proceed with thoſe Complements as with the Sides given in this Example afore-going, the Operation produces the Complements of the Angles ſought to a Semicircle.

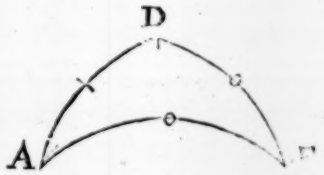
Case IV.

Two Angles and the interjacent Side being given, to find the other Sides.

Example.

In the Triangle A D E
There is given,

D A E 26° 23′ } A E
A D E 137 55 } & } required.
A D 81 50 } D E



The Operation.

A D E 137° 55′
D A E 26 23

Sum, 164 18 ½ Sum, 82° 09′
Differ. 111 32 ½ Diff. 55 46
A D 81 50 half thereof 40° 55′

Co. Ar.

As s. ½ Z *V V* A and D 82° 09′ —— Log. 0.00409
To s. ½ X *V V* —— 55 46 —— 9.91738
So is t. ½ A D —— 40 55 —— 9.93789
To t. ½ X cr. A E & D E 35 52 —— *x* 9.85937

Co. Ar.

As sc. ½ Z *V V* A and D 82° 09′ —— Log. 0.86461
To sc. ½ X *V V* —— 55 46 —— 9.75017
So is t. ½ A D 40 55 —— 9.93789
To t. ½ Z cr. A E and D E 74 21 —— 10.55267
½ Z cr. A E and D E 74° 21′
½ X cr. —— 35 52
Sum, —— 110 13 A E }
Rem. —— 38 29 D E } required.

This

This Case is wrought by the fifth *Axiome*; and the half Sum of the Sides added to the half Difference, gives the greater Side, and the half Difference substracted leaves the less.

Note,

If the Sum of the given Angles exceed a Semicircle, Substract each Angle from a Semicircle, and proceed with the Residues, the Operation will produce each Sides Compl. to 180°

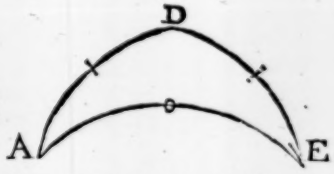
Case. V.

Two Sides and an Angle opposite to one of them being given, to find [illegible] side; if it be known, whether the other opposite Angle or the [illegible] be greater or less than a Quadrant.

Example.

In the Tr[illegible]
There is given,

A D 46° 53′	And A E required,	
D E 38 28	being less than a	
A E D 45 00	Quadrant.	



The Operation of this Case depends upon the third and fifth *Axioms.*

First, By the third *Axiome* find the Angle opposite to the other given Side.

Secondly, Having two Sides and their opposite Angles, you may find the third Side by the former part of the fifth *Axiome.*

The Operation.

		Co. Ar.
As s. A D	46° 53′	Log. 0.13670
To s. A E D	45 00	9.84948
So is s. D E	38 28	9.79383
To s. D A E	37 03	x9.78001

A E D

A D E	45° 00′	
D A E	37 03	
Sum,	82 03	½ Sum, 41° 01′
Difference,	07 57	½ Diff. 03 58

A D	46° 53′	
D E	38 28	
Diff.	08 25	½ Differ. 4° 12′

		Co. Ar.
As s. ½ X V V A and E	03° 58′	Log. 1.16004
To s. ½ Z V V	41 01	9.81709
So is t. ½ X cr. A D and D E	04 12	8.86590
To t. ½ A E required,	34 52	9.84303

34° 52′
34 52
Doubled, 69 44 A E required.

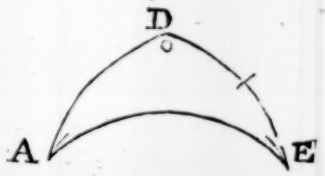
Case. VI.

Two Angles and a Side oppoſite to one of them being given, to find the third Angle; if it be known, whether the oppoſite Side or Angle required be greater or leſs than a Quadrant.

Example.

In the Triangle A D E
There is given

D A E	37° 03′	A D E required, being Obtuſe.
A E D	45 00	
E D	38 28	



The Reſolution of this Caſe depends upon the third and fourth *Axioms*.

Firſt,

First, By the third *Axiom* find the Side oppoſite to the other Angle.
Secondly, Having the two Angles and their oppoſite Sides, the third Angle may be found by the former part of the fourth *Axiome*.

The Operation.

			Co. Ar.
As ſ. DAE	37°	03′	Log. 0.22004
To ſ. DE	38	28	9.97383
So is ſ. AED	45	00	9.84945
To ſ. AD	46	53	x9.86335

AD	46°	53′		
DE	38	28		
Sum,	85	21	½ Sum	42° 40′
Diff.	08	25	½ Diff.	4 12

AED	45°	00′		
DAE	37	03		
Differ.	07	57	½ Diff.	3° 58′

			Co. Ar.
As ſ. ½ X cr. AD and DE	04°	12′	Log. 1.13527
To ſ. ½ Z cr.	42	40	9.83106
So is t. ½ X ν ν A and E	03	58	8.84100
To tc. ½ ADE required,	57	19	x9.80733
	57	19	
ADE	114	38	required.

Caſe. VII.

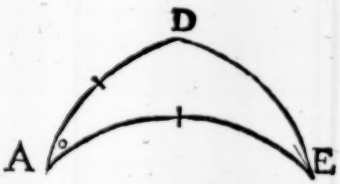
Two Sides and an Angle oppoſite to one of them being given, to find the contained Angle; if it be known, whether the other oppoſite Angle, or the Angle required, be Acute or Obtuſe.

Example.

Example.

In the Triangle A D E
There is given,

A E D 45° 00′ } D A E required,
A E 110 13 } being Acute.
A D 81 50 }



This Case is wrought by help of the third and fourth *Axioms*.
First, By the third *Axiome* to find the other oppoſite Angle.
Secondly, By the fourth *Axiome* to find the contained Angle.

The Operation.

C-

As ſ. A D 81° 50′ ——————
To ſ. A E D 45 00 ——————
So is ſ. A E 110 13 ——————
To ſ. A D E 137 55 required. —— — 9.82629

A D E 137° 55′
A E D 45 00
Differ. 92 45 ½ Diff. 46° 27′

A E 110° 13′
A D 81 50
Sum, 192 03 ½ Sum 96° 01′
Differ. 28 23 ½ Diff. 14 11

Co. Ar.

As ſ. ½ X ct^a. A E and A D 14° 11′ —— Log. 0.61079
To ſ. ½ Z ct^a. —————— 96 01 —— 9.99760
So is t. ½ X V V D and E 46 27 —— 10.02199
To tc. ½ D A E, required, 13 11 —— 10.63038
13 11
D A E 26 22 required.

Caſe

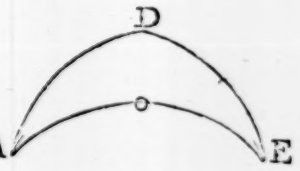
Case. VIII.

Two Angles and a Side oppoſite to one of them being given, to find the interjacent Side; if it be known, whether the other oppoſite Side, or Side ſought, be greater or leſs than a Quadrant.

Example.

In the Triangle A D E,
There is given,

A E D	45°	00′	} A E required
D A E	27	03	} being leſs than
D E	38	28	} a Quadrant.



This Caſe is reſolved by the third and fifth *Axioms*.
Firſt, By the third *Axiome* to find the other oppoſite Side.
Secondly, By the fifth *Axiome* to find the interjacent Side.

The Operation.

				Co. Ar.
As ſ. D A E	37°	03′	——	Log. 0.22003
To ſ. D E	38	28	——	9.79383
So is ſ. A E D	45	00	——	9.84948
To ſ. A D	46	53	——	x 9.86338

A E D	45°	00′	
D A E	37	03	
Sum,	82	03	½ Sum 41° 01′
Differ.	07	57	½ Diff. 3° 58′

A D	46°	53′	
D E	38	28	
Differ.	08	25	½ Diff. 04 12

Co. Ar.

As s. ½ X ν ν A and E 03° 58′ ——— Log. 1.16005
To s. ½ Z ν ν ——— 41 01 ——— 9.81709
So is t. ½ X cr. A D and D E 04° 12′ ——— 9.86590
To t. ½ A E, required, 34° 52′ ——— x 9.84304

34 52
A E 69 44 required.

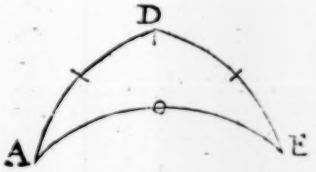
Case. IX.

Two Sides and their contained Angle being given, to find the third Side.

Example.

In the Triangle A D E
There is given,

A D E 137° 55′
A D 81 50
D E 38 28
} A E required.



The Resolution of this and the following Case is deduced from the Lord *Neipers Catholick Proposition* (the Oblique Triangle by a supposed perpendicular being reduced into two Rectangulars) by the ingenious Mr. *Collins* in his *Sector on a Quadrant*; whom in this I shall imitate.

The Operation.

As Radius ——— Log. 10.00000
To sc. A D E the contained Angle 137° 55′ ——— 9.87050
So is t. D E the Lesser Side ——— 38 28 ——— 9.90009
To t. of a fourth Arch ——— 30 31 ——— x 9.77059

If the contained Angle be less than 90°, Substract the fourth from the greater Side; but if it be greater than 90°, from its Complement to 180° the Remainder is the *Residual* Arch.

		Co. Ar.
As ſc. of the fourth Arch	30° 31′	Log. 0.06476
To ſc. of the Reſidual	67 39	9.58008
So is ſc. of the leſſer Side D E	38° 28′	9.89374
To ſc. of the Side required, A E	110 13	x9.53858

Caſe X.

Two Angles and the interjacent Side being given, to find the third Angle.

Example.

In the Triangle A D E
There is given,

A D E 114° 39′
D A E 37 03
A D 46 53
} A E D required,

The Operation.

As Radius		Log. 10.00000
To ſc. A D the interjacent Side	46° 53′	9.83473
So is t. D A E the leſſer Angle	37 03	9.87790
To t. of the fourth Arch	27 17	x9.71263

If the interjacent Side be more than a Quadrant, ſubſtract the fourth Arch from the greater Angle, if leſs, from the ſaid Angles Complement to 180°, the Remainder is the Reſidual Arch.

		Co. Ar.
As ſc. 4th. Arch	27° 17′	Log. 0.05123
To ſc. Reſidual Arch	38 04	9.89614
So is ſc. D A E the leſſer Ang.	37 03	9.90206
To ſc. A E D the Angle required	45 00	x9.84943

In this and the fore-going Case the Affection of the required Side or Angle, may be determined by the Residual Arch.

For if the contained Angle, or interjacent Side be less than a Quadrant, and the Residual Arch more, or when the contained Angle or interjacent Side is greater than a Quadrant, and the Residual Arch less; the Side or Angle required is greater than 90°, in all other Cases less.

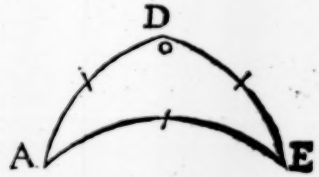
Case. XI.

Three Sides given, to find an Angle.

Example.

In the Triangle ADE
There is given,

AE 110° 13′
AD 81 50 } ADE required,
DE 38 28



The Resolution of this Case depends upon the sixth *Axiom*, and for the more speedy Operation, take this brief direction.

Add the three Sides together, and from their half Sum, substract the Side opposite to the Angle required.

Then to the Complements Arithmetical of the Logarithm-Sines of the containing Sides, add the Logarithm-Sines of the half Sum and Remainder: Half the total of these four Logarithms is the Sine-Complement of half the Angle required.

The Operation.

AD	81° 50′	The containing	S.	Co. Ar.	0.20616
DE	38 28	Sides.	S.	Co. Ar.	0.00442
AE	110 13	½ Sum, 115° 15′	S.		9.95639
Sum.	230 31	Rem. 05 02	S.		9.94317
½ Sum,	115 15			Sum,	19.11014
Remain.	05 02	sc. 68° 57′		½ Sum,	9.55507

Which being doubled, produces ADE 137° 54′ required.

Case

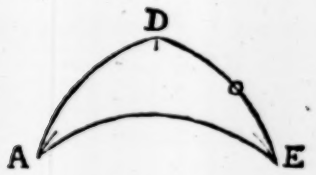
Case XII.

Three Angles given, to find a Side.

Example.

In the Triangle A D E
There is given

A D E 137° 55′
A E D 45 00 } D E required,
D A E 26 23



This Case is likewise performed by the sixth *Axiome*, the Angles being converted into Sides, and the Sides into Angles, by taking the Compl. of the greatest Angle to a Semicircle.

Compl. A D E	42° 05′	The adjacent	S.	Co. Ar.	0.17378
A E D	45 00	Angles.	S.	Co. Ar.	0.15051
D A E	26 23	½ Sum, 56° 44′	S.		9.92227
Sum,	113 58	Rem. 30 21	S.		9.70353
½ Sum,	56 44			Sum,	19.95009
Rem.	30 21	Sc. 19° 15′		½ Sum,	9.97502

Which being doubled, gives D E 38 30 required.

CHAP.

CHAP. IV.

The Doctrine of Plain Triangles applyed in PROBLEMS of Plain Sayling.

SECT. I.

The Application of Right-angled Triangles.

ALthough the Ground and Projection of the Plain Chart be erroneous, yet seeing it is most facile to the Learner; and may serve as an Introduction to what is more difficult, it shall not be here omitted.

Problem I.

The Course and distance given, to find the Difference of Latitude, and the Departure.

Example.

A Ship sailing N. E. by N. 372 minutes,
I demand her Difference, Latitude, and Departure. *Fig.* 1.

In

In the Triangle A B C,
A C repreſents the Diſtance Sailed.
A B the Diff. Latitude.
B C the Departure.
B A C the Angle of the Courſe from the Meridian.
A C B the Compl. of the Courſe.

The Operation.

For the Diff. Latitude.

As Radius		Log. 10.00000
To the Diſtance Sailed,	372 min.	2.57054
So is ſc. of the Courſe,	56° 15′	9.91985
To the Diff. Latitude	309 min.	x2.49039

For the Departure.

As Radius		Log. 10.00000
To the Diſtance Sailed,	372 min.	2.57054
So is ſ. Courſe,	33° 45′	9.74474
To the Departure	206 min.	x2.31528

Problem II.

The Courſe and Diff. Latitude being given, to find the Diſtance and Departure.

Example.

A Ship ſailing N. W. by N. until her Difference of Latitude be 309′ I demand her Diſtance and Departure.

Fig. 2.

The Operation.

For the Diſtance.

As ſc. of the Courſe	56° 15′	Log. 9.91984
To the Diff. Latitude	309 min.	2.48996
So is Radius,		10.00000
To the Diſt. ſailed,	371 min.	2.57012

For

For the Departure.

		Co. Ar.
As ſc. Courſe,	56° 15′	Log. 0.08016
To the Diff. Lat.	309 min.	2.48996
So is ſ. Courſe	33° 45′	9.74474
To the Departure	206 min.	2.31486

Problem. III.

The Courſe and Departure given, to find the Diſtance and Difference of Latitude.

Example.

A Ship ſailing S. E. by S. until her Departure be 206 min. I demand the Diſtance and Difference of Latitude. Fig. 3.

The Operation.

For the Diſtance.

As ſ. Courſe	33° 45′	Log. 9.74474
To the Departure	206 min.	2.31387
So is Radius		10.00000
To the Diſtance	370 min.	2.56913

For the Diff. Latitude.

		Co. Ar.
As ſ. Courſe	33° 45′	Log. 0.25526
To the Departure	206 min.	2.31387
So is ſc. Courſe	56° 15′	9.91985
To Diff. Lat.	309 min.	2.48898

Problem. IV.

The Diſtance and Difference of Latitude given, to find the Courſe and Departure.

Example.

Example.

A Ship Sails between the North and the East, 372 min. until her Difference Latitude be 309 min. I demand the Course and Departure.

The Operation. *Fig.* 4.

For the Course.

As the Distance sailed 372 min. Log 2.57054
To Radius ——— 10.00000
So is the Diff. Lat. 309 min. ——— 2.48996
To the fc. Course 33° 50′ ——— 9.91942

For the Departure.

As Radius ——— Log. 10.00000
To the Distance 372 min. ——— 2.57054
So is the Course 33° 50′ ——— 9.74568
To the Departure 207 min. ——— 2.31622

Problem. V.

The Distance and Departure given, to find the Course and Difference of Latitude.

Example.

A Ship Sailes between the South and the West, 372 min. until her Departure be 206 min. I demand the Course and Diff. Latitude.

Fig. 5.

The Operation.

For the Course.

As the Distance 372 min. Log. 2.57054
To Radius ——— 10.00000
So is the Departure 206 min. ——— 2.31387
To the Course 33° 37′ ——— 9.74333

For the Difference of Latitude.

As Radius ——————— Log. 10.00000
To the Diſtance 372 min. —— 2.57054
So is ſc. Courſe 56° 23′ ——— 9.92052
To the Diff. Lat. 309 min. —— 12.49106

Problem. VI.

The Difference, Latitude and Departure given, to find the Courſe and Diſtance.

Example.

A Ship ſayling between the South and the Weſt, until her Diff. Latitude be 309 min. and her Departure 206 min. I demand the Courſe and Diſtance,

Fig. 6.

The Operation.

For the Courſe.

As the Diff. Lat. 309 min. Log. 2.48996
To Radius ——————— 10.00000
So is Departure 206 min. —— 2.31387
To t. Courſe 33° 41′ —— 9.82391

For the Diſtance.

As ſ. Courſe —— 33° 41′ ——————— Log. 9.74398
To the Departure 206 min. ——————— 2.31387
So is Radius ——————————— 10.00000
To the Diſtance 371 min. 2.56989

Sect.

SECT. II.

The Doctrine of Oblique Triangles applyed in Problems of Sayling.

Problem. I.

TWO Ships sail from the same Port, the one sailes E. N. E. 40 min. the other E. by S. so far, until she find the first Ship bear N. W. by W. I demand the second Ships Distance from the Port, and the Distance between the two Ships.

Fig. 7

In the Triangle A D E
A represents the Port,
A D the E. N. E. Course, and A E the E. by S. Course.

The Operation.

To find the second Ships Distance from the Port.

			Co. Ar.
As s. A E D	22° 30′	Log.	0.41716
To A D	40 min.		1.60206
So s. A D E	123° 45′		9.91984
To A E	86 min.		1.93906

To find the Distance between the Ships.

			Co. Ar.
As s. A E D	22° 30′	Log.	0.41716
To A D	40 min.		1.60206
So is s. D A E	33° 45′		9.74474
To D E	58 min.		1.76396

Problem. II.

Suppose there are two Ports that lye East and West one from another; one Ship sails from the Westermost Port N. E. 41. min. the other sails from the Eastermost Port 80 min. and meets with the first Ship: I demand the Course steer'd by the second Ship, and the Distance between the two Ports.

Fig. 8.

Let A represent the Westermost Port,
E the Eastermost,
A D the Course and Distance of the first Ship,
D the Place where the Ships meet.

To find the second Ships Course.

The Operation.

		Co. Ar.
As D E	80 min. Log.	8.09691
To ſ. D A E	45° 00′	9.84948
So is A D	41 min.	1.61278
To ſ. A E D	21° 14′	9.55918

The Course is N. W. 68° 46′, or W. N. W. a little Westerly.

To find the Distance between the two Ships.

		Co. Ar.
As ſ. D A E	45° 00′ Log.	0.15052
To E D	80 min.	1.90309
So is ſ. A D E	113° 46′	9.96151
To A E	103 min.	2.01512

Problem. III.

Suppose two Ships set sail from a certain Road, the one sails S. by E. 20 min. the other S. S. W. 25 min. I demand their Bearing and Distance from each other.

Fig. 9.

In

In the Triangle A D E
A represents the Road,
A D the first Ships Course and Distance,
A E the second Ships Course and Distance.

The Operation.

To find the Bearing.

A E	25		180° 00′
A D	20	D A E	33 45
Sum,	45	Sum	146 15 A D E & A E D
Differ.	05	½ Sum	73 07 A D E & A E D

	Co. Ar.
As Z cr. A E and A D 45	Log. 8.34679
To their Differ. 05	0.69897
So is t. ½ Z V V D and E 73° 07′	10.51783
To t. ½ their Difference 20 06	x9.56359

½ Z V V 73° 07′
½ X V V 20 06
Sum, 93 13 A D E
53 01 A E D

The Bearing of the ships is E. N. E. ½ E. or W. S. W. ½ W.

To find their Distance.

	Co. Ar.
As s. A E D 53° 01′	Log. 0.09756
To A D 20 min.	1.30103
So is s D A E 33° 45′	9.74474
To D E 14 min.	x1.14333

Prob.

Problem. IV.

A Ship sayles from a certain Port, S. S. E. 60 min. and then sayles 72 min. more Easterly, but is forced back by foul weather 82 min. to the Port from whence she set sail; I demand what Course she steered from the second place to the third, and how she sailed back to the first Port.

Let A represent the Island,
E the second Place,
D the third Place.

The Operation.

To find the Course from the second Place to the third.

A D	82
A E	68
Sum,	150
Diff.	14

	Co. Ar.
As D E the Base 72 min.	Log. 8.14267
To Z cᵗ. A E and A D 150	2.17609
So is their Difference 14	1.14613
To a Segment of the Base, 29 min.	*1.46489

D E	72 min.
Segment	29
Diff.	43
½ Diff.	21 ½, or 21, 5. E B

As A E 68 min.	Log. 1.83251
To Radius	10.00000
So is E B 21° 5 min.	1.33244
To sc. A E B, or A E D, 71° 34′	9.49993

To

The Course from the second Place to the third, is N. E. 49° 04′ or N. E. ½ E. *ferè*.

To find the Course back to the Port.

		Co. Ar.
As A D	82 min.	Log. 8.08619
To ſ. A E D	71° 34′	9.97112
So is A E	68 min.	1.83251
To ſ. A D E	51° 53′	19.89582

The Course to the Port is N. W. 79° 03′, or W. by N. a little Westerly.

CHAP. V.

The Doctrine of Plain Right-angled Triangles, applyed in PROBLEMS of Mercators Sayling.

THE true Sea-Chart, commonly called *Mercators-Chart*, (but is indeed the useful Invention of our Countryman Mr. *Edward Wright*, although this Stranger hath almost got the Name and Praise thereof) performs the like Conclusions, and almost in the same manner, but with far more exactness than the Plain Chart, in all Places that have any considerable Latitude.

Problem I.

To find the Meridional Difference of Latitude, or the Difference of Latitude in Meridional Parts.

First, If one Place be under the Equinoctial, and the other in North or South Latitude, the Meridional parts (in the Table of Meridional parts) answering to the degrees and minutes of the Place, having Latitude, is the Meridional Diff. Latitude.

Example.

One place in the Latitude 37° 27′ North, the other under the Equinoctial, I demand the Different Latitude in Meridional parts.

Lat. 37° 27′ ——————— 24 26
24 26 is Meridional Diff. Latitude.

Secondly, If two places be both in North or both in South Latitude, Substract the Meridional parts of the less Latitude from those of the greater, the remainder is the Meridional Diff. Latitude.

Example 1.

	M. p^{ts}.
One place in the Latitude 37° 20′ N^{o}.	2417
The other in the Latitude 17 10 N^{o}.	1045
The Meridional Diff. Latitude	1372

Example 2.

	M. p^{ts}.
One place in the Latitude 45° 56′ S^{o}.	3109
The other in the Latitude 29 17 S^{o}.	1838
The Meridional Diff. Latitude	1271

Thirdly, If of the two places the one have North Latitude, the other South, add the Meridional parts of each Latitude together, the Sum is the Diff. Latitude in Meridional parts.

Example.

Example.

		M. p'.
One place in the Latitude	42° 17′ S°.	2804
The other in the Latitude	27 19 N°.	1703
The Meridional Diff. Latitude		4507

Problem II.

Both Latitudes, and the Difference of Longitude between any two places being given, to find the Course and Distance.

Example.

Admit the *Lizard* in the Latitude 50 degrees North, and the *Barbadoes* in the Latitude 13 deg. 12 min. North, the Difference of Longitude 54 deg. 57 min. West; I demand the Course and Distance.

In the Triangle A B C
A B represents the proper Difference of Latitude,
B C the Departure,
A C the Distance sailed,
B A C the Course,
A C B the Complement of the Course.

Fig. 11.

In the Triangle A B C,
A B represents the Meridional Diff. Latitude,
B C the Difference of Longitude,
B A C the Angle of the Course,
A C B the Complement of the Course.

This being understood, the Proportions are the same as in the Doctrine of Plain Right-angled Triangles.

The Difference of Longitude reduced to minutes, makes 3296 min.

To find the Meridional Difference of Latitude.

	M. p^t.
One place in the Latitude 50° 00′ N^.	3474
The other in the Latitude 13 12 N^.	0799
The Meridional Diff. Latitude,	2675

The Operation.

For the Course.

As the Merid. Diff. Lat. 2675 min. ——	Log. 3.42732
To Radius ——	10.00000
So is the Diff. Long. 3297 min. ——	3.51812
To t. Course —— 50° 57′ ——	10.09080

The Course is S. W. ½ W.

For the Distance.

Lat.	50°	00′
Lat.	13	12
Proper Diff. Lat.	36	48 which is 2208 min.

As sc. Course	39° 03′	Log. 9.79934
To proper Diff. Lat.	2208 min.	3.34400
So is Radius ——		10.00000
To the Distance ——	3505 min.	3.54466

Problem III.

Both Latitudes and the Course given, to find the Distance and Difference of Longitude.

Example.

A Ship sails from the *Lizard*, in the Latitude 50 deg. North, until she be in the Latitude 13 deg. 12 min. North, her Course S. W. 50 degrees, 57 min. or S. W. ½ W. somewhat Westerly; I demand the Distance and Difference of Longitude.

The

The proper Diff. Latitude is 2208 min.
The Meridional Diff. Lat. is 2675 min.

The Operation.

For the Diſtance.

As ſc. Courſe 39° 03′ —— Log. 9.79934
To the Diff. Lat. —— 2208 min. — 3.34400
So is Radius ———————— 10.00000
To the Diſtance —— 3505 min. — 3.54466

For the Difference of Longitude.

As Radius ———————— Log. 10.00000
To Meridional Difference of Latitude 2675 min. —— 3.42732
So is t. Courſe ———— 50° 57′ ——— 10.09086
To Difference of Longitude —— 3297 min. —— *3.51818

Problem. IV.

Both Latitudes and the Diſtance given, to find the Courſe and Difference of Longitude.

Example.

A Ship ſails from the Lat. 50 deg. North 3505 min. until ſhe be in the Latitude 13 deg. 12 min. North; I demand the Courſe and Difference of Longitude.

The Meridional Difference of Latitude is 2675 min.
The proper Difference of Latitude is 2208 min.

The Operation.

For the Course.

As the Distance ——— 3505 min. ——— Log. 3.54469
To Radius ——— 10.00000
So is the Difference of Lat. 2208 min. ——— 3.34402
To sc. Course ——— 39° 03′ ——— 9.79931

For the Difference of Longitude.

As Radius ——— Log. 10.00000
To the Merid. Diff. Lat. 2675 min. ——— 3.42732
So is t. Course ——— 50° 57′ ——— 10.09086
To Differ. of Long. 3297 min. ——— 3.51818

Problem. V.

One Latitude, the Course and Difference of Longitude being given, to find the other Latitude, and the Distance.

Example.

A Ship sails S. W. 50 deg. 57 min. or S. W. ½ W. somewhat more Westerly from the Latitude 50 deg. North, until the Difference of Longitude be 3297 min. I demand the other Latitude and Distance.

The Operation.

For the other Latitude.

As t. Course ——— 50° 57′ ——— 10.09086
To Difference of Long. ——— 3297 min. ——— 3.51812
So is Radius ——— 10.00000
To the Merid. Diff. Lat. — 2675 min. ——— 3.42726

The

	M. p'.
The Meridional parts answering to Lat. 50° North, are	3474
From which Substract, —— 2675 ——	2675
There remains ——	799

Against which in the Table of Meridional parts is Latitude 13° 12′ which is the Latitude of the place North.

For the Distance.

The proper Difference of Latitude is 2208 minutes.

As sc. Course —— 39° 03′ —— Log.	9.79934
To the Difference of Latitude 2208 min.	3.34400
So is Radius ——	10.00000
To the Distance —— 3505 min. ——	3.54466

Problem. VI.

One Laeitude, the Course and Distance given, to find the other Latitude and Difference of Longitude.

Example.

A Ship being in the Lacitude 50 deg. North, sails S. W. 50 degrees, 57 min. or S. W. ½ W. and somewhat Westerly 3505 min. I demand the other Latitude and Difference of Longitude.

The Operation.

For the Difference of Latitude.

As Radius —— Log.	10.00000
To the Distance —— 3505 min. ——	3.54469
So is sc. Course —— 39° 03′ ——	9.79934
To the Difference of Latitude 2208 min. ——	3.34403

The

The other Lat. is 13 deg. 12 min. North.

The Meridional Diff. Lat. is 2675.

For the Difference of Longitude.

As Radius ———————————	Log. 10.00000
To the Meridional Diff. Lat. 2675 min. ———	3.42732
So is t. Course ——— 50° 57′ ———	10.09086
To the Difference of Long. 3297 min. ———	✗3.51818

Problem. VII.

Two Places both in one Parallel or Latitude, and their Difference of Longitude being given, to find the Distance between them.

Example.

Suppose two places both in the Parallel or Latitude of 50 deg. and their Difference of Longitude 70 deg. I demand the Distance between them.

The Operation.

The Difference of Longitude in minutes is 4200.

As Radius ———————	Log.	10.00000
To Diff. Longitude	4200 min.	3.62325
So is sc. Latitude	40°	9.80807
To the Distance	2700 min.	3.43132

Problem. VIII.

Two Places, both in one Latitude, and their distance given, to find their Difference of Longitude.

Example.

Example.

Suppose two places both in the Latitude 50 degrees, and the Distance between 2700 minutes.
I demand the Difference of Longitude.

The Operation.

As sc. Latitude	40 deg.	Log. 9.80807
To the Distance	2700 min.	3.43136
So is Radius —— —— —— ——		10.00000
To the Diff. Long.	4200 min.	3.62329

Problem. IX.

Two Places situate both in one Parallel or Latitude, their Distance and Difference of Longitude being given, to find the Parallel of Latitude.

Example.

A Ship sailing due West, 2700 min.
Alters her Diff. Longitude 4200 min.
I demand what Latitude the Ship sails in,

The Operation.

As Diff. Longitude	4200 min.	Log. 3.62325
So Radius —— —— —— —— —— ——		10.00000
So is the Distance	2700 min.	3.43136
To sc. Latitude	40 deg.	9.80811

CHAP.

CHAP. VI.

The Doctrine of Spherical Triangles applyed in *Problems* of Great Circle Sayling.

ALthough it be hardly possible for a Ship exactly to trace out the Arch of a Great Circle, yet it may be of good advantage to keep conveniently near it, especially in a Parallel (East or West) Course.

Problem. I.

Two Places differing only in Longitude.

Example.

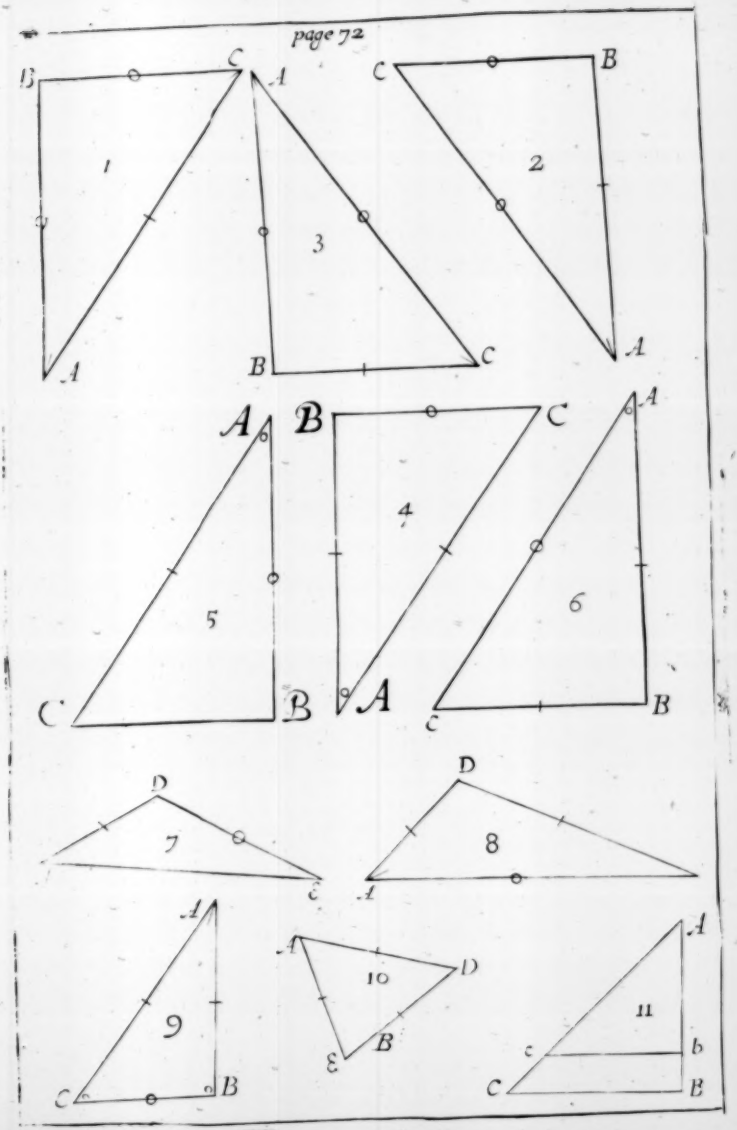
A Ship being in the Latitude 50 deg. North, is bound to a Port in the same Parallel whose Difference of Longitude Westerly is 47 deg. I demand the Angles of Position, the Distance in the Arch of a Great Circle, by what Latitudes and Longitudes the Arch shall pass, likewise the Course and Distance from place to place, according to *Mercator*.

Let A represent the first Place,
E the second. *Fig.* 12.

The Operation.

To find the Angles Position B A D and B E D.

The Oblique-angled Triangle A D E is reduced into two equal Right-angled Triangles A B D and E B D, the Side and Angles being equal; therefore in either of them there is given the *Hypothenuse*, and the


B
C
A
1
A
C
A
3
B
C
C
B
2
A
A
B
5
C
B
B
C
4
A
A
6
C
B
D
7
C
D
8
A
A
9
C
B
A
10
D
E
B
A
11
c
b
C
B

the Angle at D, to find the Angle at A or E.

In the Triangle A B D

As tc. A D B,	23° 30′ —— Log.	10.36170
To Radius —— —— —— —— ——		10.00000
So is ſc. A D	40 00 —— ——	9.88425
To tc. B A D	71 35 —— ——	9.52255

2. To find the Diſtance A E,

In the Triangle A B D.

As Radius —— —— —— —— —— ——	Log.	10.00000
To ſ. D A	40° 00′ —— —— —— ——	9.80807
So is ſ. A D B	23° 30′ —— —— —— ——	9.60070
To ſ. A B	14 51 —— —— —— ——	9.40877

A B 14° 51 being doubled, produces
A E 29° 42′ or 1782 min.

3. To find the Latitudes by which the Arch ſhall paſs at every five degrees of Longitude from A, repreſenting the firſt Port.

Firſt, You muſt find the greateſt Latitude by which the Arch paſſes,

In the Triangle A B D.

As tc. A D	40° 00′ — Log.	10.07619
To Radius —— —— —— —— ——		10.00000
So is ſc. A D B	23 30 —— ——	9.96240
To t. B D	37 45 —— ——	9.88621

The Compl. of B D (to 90°) 52° 25′ is the greateſt Latitude.

Secondly, To find the Latitude by which the Arch paſſes at every five degrees of Longitude from A, you muſt reſolve the ſeveral Right-angled Triangles B D a, B D c, B D e, *&c.*

Subſtracting five deg. from A D B 23° 30′
There remaines a D B 18° 30′
Subſtracting five deg. from 18° 30′
Remains B D c, 13° 30′

And ſo for the reſt, as follows in the Table.

a D B	18° 30′	In the Triangle a B D
B D c	13 30	To find by what Latitude the Point
B D e	08 30	(a) paſſes.
B D f	03 30	
B D g	01 30	As Radius —— Log. 10.00000
B D h	06 30	To tc. B D 37° 35′ —— 10.11371
B D i	11 30	So is ſc. a D B 18 30 —— 9.97696
B D k	16 30	To tc. D a 39 03 —— 10.09067
B D l	21 30	

The Complement of D a 50° 57′ North is the Latitude of the Point (a.)

After the ſame manner are found the Latitudes for the Points c, e, *&c.* in the ſubſequent Table.

	Long.	Lat.
A	00° 00′	50° 00′
a	05 00	50 57
c	10 00	51 39
e	15 00	52 07
f	20 00	52 22
g	25 00	52 24
h	30 00	52 14
i	35 00	51 51
k	40 00	51 15
l	45 00	50 24
E	47 00	50 00

Fourthly, Having the Latitudes and Longitudes, by which the Arch paſſes, you may find the Courſe and Diſtance from place to place by *Mercator*.

So to find the Courſe and Diſtance A a, There is given both Latitudes 50 degrees North, and 50 degrees, 57 minutes North.

And the Difference of Longitude, five deg. Weſt.

The Meridional Difference of Latitude is 90 minutes.

For

For the Courſe.

As Merid. Diff. Lat. 90 min.	Log. 1.95424
To Radius	10.00000
So is the Diff. of Long. 300 min.	2.47712
To t, Courſe——73° 18′ ——	10.52288

For the Diſtance.

As ſc. Courſe—— 16° 42′ ——	Log. 9.45843
To the Difference of Latitude 57 min. ——	1.75587
So is Radius ——	10.00000
To the Diſtance —— 198 min. ——	2.29744

After the ſame manner you will find the Courſes and Diſtances a c, c e, &c. as they follow in the Table.

Places.	Courſes.	Diſt.
From A to a	N.W. 73° 18′	198
From a to c	N.W. 77 24	192
From c to e	N.W. 81 28	189
From e to f	N.W. 85 14	180
From f to g	N.W. 89 25	196
From g to h	S.W. 86 56	187
From h to i	S.W. 82 47	183
From i to k	S.W. 79 03	189
From k to l	S.W. 75 04	198
From l to E	S.W. 72 25	79

But in regard moſt of the Courſes afore-found are ſo near the Weſt, you may ſail W. N. W. 913 min. until you are in the Latitude 55°, 50′ North; and then W. S. W. 913 min. farther, you will arrive at

your Port. By this means you will alter your Latitude almoſt ſix degrees, which is conſiderable, in reſpect of the benefit of Obſervation; beſides the Diſtance is but 44 min. more than that of a great Circle, and not above 13 min. more than the Parallel or Weſt Diſtance.

Problem. II.

Two Places differing both in Latitude and Longitude.

Example.

Suppoſe the two places to be, one in the Latitude 36° North, the other in the Latitude 50 deg. North, the Difference of Longitude between them 60 deg. Eaſterly: I demand the Angles of Poſition, the Diſtance in the Arch, the Latitudes and Longitudes, by which the Arch paſſes, and the Courſe and Diſtance from place to place, through thoſe Latitudes and Longitudes, according to the true Chart.

Let A repreſent the firſt Place,
E the ſecond. *Fig.* 13.

The Operation.

Firſt, To find the Angles of Poſition.

In the Triangle A D E.

AD	54° 00′		ADE	68° 00′	
DE	40 00		½ ADE	34 00	
Sum,	94 00	½ Sum,	47° 00′		
Diff.	14 00	½ Diff.	07 00		

			Co. Ar.
As ſ. ½ Z cr². AD and DE	47° 00′		Log. 0.13587
To ſ. ½ X cr².	07 00		9.08589
So tc. ½ ADE	34 00		10.17101
To t. ½ X ~ A and E	13 52		9.39277

Co. Ar.

			Co. Ar.
As ſc. ½ Z cr. AD and DE	47°	00′	Log. 0.16622
To ſc. ½ X cr.	07	00	9.99675
So is tc. ½ ADE	34	00	10.17101
To t. ½ Z *vv* A and E	65	08	10.33398

½ Z *vv*	65°	08′	
½ X *vv*	13	52	
Sum,	79	00	AED } The Angles of Poſition.
Diff.	51	16	DAE }

Secondly, To find the Diſtance.

In the Triangle ADE.

			Co. Ar.
As ſ. ADE	79°	00′	Log. 0.09895
To ſ. AD	54	00	9.90796
So is ſ. ADE	68	00	9.96716
To ſ. AE	49	50	*x* 9.88317

The Diſtance is 49 deg. 50 min. which reduced into minutes, makes 2990 minutes.

Thirdly, To find the Latitudes and Longitudes by which the Arch paſſes.

Firſt, Find the greateſt Latitude by which the Arch paſſes.

In the Right-angled Triangle ABD.

As Radius			Log. 10.00000
To ſ. AD	54°	00′	Log. 9.90796
So is ſ. ADB	51	16	9.89213
To ſ. DB	39	07	*x* 9.80009

DB is 39° 07′ whoſe Compl. 50° 53′ is the greateſt Latitude.

Secondly,

Secondly, To find the Vertical Angles A D B, and B D E.

In the Right-angled Triangle A B D.

As tc. B A D	—— 51° 16′ ——	Log.	9.90423
To Radius	——		10.00000
So is sc. A D	—— 54 00 ——		9.76922
To tc. A D B	— 53 46 ——		9.86499

From	A D E	68	00
Substract	A D B	53	46
Remains	B D E	14	14

Thirdly, To find the Latitudes by which the Arch passes at every five degrees of Longitude from A, you must resolve the several Right-angled Triangles, B D a, B D b, B D c, &c.

Substracting 5 deg. from	A D B	53° 46′,
There Remains	A D b	48 46.
Substracting 5 deg. from		48 46,
Remains	b D B	43 46.

So of the rest in the following Table.

B D *a*	48	46	B D *h*	13	46
B D *b*	43	46	B D *i*	08	46
B D *c*	38	46	B D *k*	03	46
B D *d*	33	46	B D *l*	01	14
B D *e*	28	46	B D *m*	06	14
B D *f*	23	46	B D *n*	11	14
B D *g*	18	46			

In the Triangle *a D B*, To find by what Latitude the Arch passes at the Point *a*.

A

As t. DB 39° 07′ —— Log. 9.91018
To Radius —— 10.00000
So is sc. aDB 48 46 —— 9.81897
To tc. aD — 50 59 —— 9.90879

Whose Compl. 39° 01′ is the Latitude at *a*.

After the same manner are found the Latitudes, of the several Points, *b*, *c*, *d*, *e*, &c. as in the subsequent Table.

	Latatitude.		Long.
A	36°	00′	00°
a	39	01	05
b	41	36	10
c	43	47	15
d	45	47	20
e	47	09	25
f	48	22	30
g	49	20	35
h	50	03	40
i	50	33	45
k	50	49	50
l	50	52	55
m	50	42	60
n	50	20	65
E	50	00	68

Fourthly, Having thus the Latitudes and Longitudes of the Arch, you may find the Courses and Distances from place to place, according to *Mercator*.

So to find the Course and Distance *A a*.

Both Latitudes are 36 deg. and 39 deg. 01 min.

The Difference of Longitude 5 deg.

The proper Differ. of Lat. 181 min.

The Merid. Diff. Lat. 228 minutes.

For the Course.

As Merid. Diff. Lat. 228 min. Log. 2.35793
To Radius —— 10.00000
So is Diff. Long. —— 300 min. —— 2.47712
To t. Course —— 52° 45′ —— 10.11919

For

For the Distance.

As sc. Course	52° 45′	Log.	9.78197
To Diff. Lat.	181 min.		2.25786
So is Radius			10.00000
To the Distance	299 min.		2.47589

After the same manner you may find the Courses and Distances, *a b*, *b c*, *c d*, &c. as they follow in the Table.

Places.				Courses.			Distances. min.
From	*A*	to	*a*	N E	52°	45′	299
From	*a*	to	*b*	N E	55	16	272
From	*b*	to	*c*	N E	59	19	257
From	*c*	to	*d*	N E	62	40	240
From	*d*	to	*e*	N E	65	56	226
From	*e*	to	*f*	N E	70	12	216
From	*f*	to	*g*	N E	73	39	206
From	*g*	to	*h*	N E	77	24	197
From	*h*	to	*i*	N E	81	05	893
From	*i*	to	*k*	N E	85	14	192
From	*k*	to	*l*	N E	89	02	178
From	*l*	to	*m*	S E	86	56	187
From	*m*	to	*n*	S E	83	20	189
From	*n*	to	*D*	S E	79	56	115

CHAP

CHAP. VII.

The Doctrine of the Sphere: Containing sundry *Astronomical Problems*, useful in the Art of Navigation.

SECT. I.

Of Astronomical Definitions.

THE *Poles of the World* are two fixed *Points* in the Heavens, Diametrically opposite to one another, the one visible in our Hemisphere called the North, or *Artick Pole*, noted with the Letter P. *Fig.* 14

The other, not seen of us, being in the Lower Hemisphere, called the South, or *Antartick Pole*, noted with S.

The Axis of the World is an imaginary *Line* drawn from Pole to Pole, about which the *Diurnal Motion* is performed from East to West; represented by P ≏ S.

The Meridians are Great Circles concurring and intersecting one another in the Poles of the World; as P E S, and P c S.

The Equinoctial, or *Equator*, is a *Great Circle*, 90 deg. distant from the Poles of the World, cutting the *Meridians* at Right-angles, and dividing the World into two parts, called the *North and South Hemispheres*; as E ≏ Q.

The Ecliptick is a *Great Circle* crossing the *Equinoctial* in the two opposite Points *Aries* and *Libra*, and making an Angle therewith (called its *Obliquity*) of 23 deg. 30 min.

This Circle is divided into 12 Signes, each containing 30 deg. whose Names and Characters follow.

Aries	♈	Which are called *Northern Signes.*
Taurus	♉	
Gemini	♊	
Cancer	♋	
Leo	♌	
Virgo	♍	
Libra	♎	These are called *Southern Signes.*
Scorpio	♏	
Sagitarius	♐	
Capricornus	♑	
Aquarius	♒	
Pisces	♓	

The Ecliptick is repesented by ♋ ♎ ♑.

The Zodiack, is a Zone having eight degrees of Latitude on either side of the *Ecliptick* in which space the Planets make their Revolutions. 'Tis divided and distinguished by the twelve Signs.

The Colures are two *Meridians*, dividing the *Equinoctial* and the *Ecliptick* into four equal parts, one of these passes by the *Equinoctial* Points, *Aries* and *Libra*, and is called the *Equinoctial Colure*, as P ♎ S.

The other by the beginning of *Cancer* and *Capricorn*, called the *Solstitial Colure*, P ♋, S ♑.

The Poles of the Ecliptick are two Points, 23° 30′ distant from the Poles of the World; as I and K.

The Tropicks are two small Circles, Parallel to the *Equinoctial*, and distant there-from 23° 30′, limiting the Suns greatest Declination.

The *Northern Tropick* passes by the beginning of *Cancer*, and is called the *Tropick of Cancer*; as ♋ a D.

The *Southern Tropick* passes by the beginning of *Capricorn*, and is called the *Tropick of Capricorn*, as A ♑ ♑.

The

The *Polar Circles* are two ſmall Circles parallel to the Equinoctial, and diſtant there-from 66° 30′, and from the Poles of the World 23° 30′.

That which is adjacent to the North Pole is called the *Artick Circle*, as G d I.

And the other the *Antartick Circle*, as K e N.

The *Zenith* and *Nadir* are two Points diametrically oppoſite.

The *Zenith* is the Vertical Point, or the Point right over our heads, as Z.

The *Nadir* is directly oppoſite thereto as N.

The *Azimuths*, or *Vertical Circles*, are Great Circles of the Sphere, concurring and interſecting each other, in the *Zenith* and *Nadir*; as Z f N.

The *Horizon* is a great Circle 90 degrees diſtant from the *Zenith* and *Nadir* cutting all *Azimuths* at Right-Angles, and dividing the World into two equal parts, the *Upper* and viſible *Hemiſphere*, and the *Lower* and inviſible. This Circle is repreſented by H a R.

The *Meridian* of a place, is that *Meridian* which paſſes by the *Zenith* and *Nadir* of the place; as P Z S N.

The *Almicanthars* or *Parallels* of *Altitude*, are ſmall Circles, Parallel to the *Horizon*, imagined to paſs through every degree and minute of the *Meridian*, between the *Zenith* and *Horizon*; as B a F.

Parallels of *Latitude* or *Declination*, are ſmall Circles: They are called *Parallels of Declination* in reſpect of the Sun or Stars; but in reſpect to the ſituation of the Earth are called *Parallels of Latitude*.

The *Latitude* of a place, is the height of the Pole above the *Horizon*, or the diſtance between the *Zenith* and the *Equinoctial*.

The *Latitude* of a Star is the Arch of a Circle contained between the Center of a Star and the *Ecliptick* Line, this Circle making right Angles with the *Ecliptick*; and is counted either Northward or Southward, according to the ſituation of the Star.

Longitude on the Earth is meaſured by an Arch of the *Equinoxial*, contained between the primary or firſt Meridian of that place where Longitude is aſſigned to begin, and the Meridian of any other place; counted alwayes Eaſterly.

The *Longitude* of a Star is that part of the Ecliptick, which is contained between the Stars place in the *Ecliptick*, and the beginning of *Aries*, counting them according to the ſucceſſion of the Signes.

Altitude of the Sun or Stars, is the Arch of an *Azimuth* contained betwixt the Center of the Sun or Star and the Horizon.

Aſcenſion is the riſing of any Star, or any part of the *Equinoctial* above the *Horizon*, and *Deſcenſion* is the ſetting thereof.

Right Aſcenſion is the number of Degrees and Minutes of the *Equinoxial* (counted from the beginning of *Aries*) which cometh to the *Meridian* with the Sun or Stars, or with any portion of the *Ecliptick*.

Oblique Aſcenſion, is an Arch of the *Equinoctial* between the beginning of *Aries*, and that part of the *Equinoctial* that riſeth with the Center of a Star, or with any portion of the *Ecliptick*, in an *Oblique Sphere*.

Oblique Deſcenſion is that part which ſets therewith.

Aſcenſional Difference is an Arch of Difference between the *Right* and *Oblique Aſcenſion*.

The *Amplitude* of the Sun, is the diſtance of the riſing or ſetting thereof, from the true Eaſt or weſt point of the *Horizon*.

The *Parallax* is the Difference between the true and apparent place of the Sun or Star; ſo the true place in reſpect of Altitude is in the Line A C E, or A D G, the Sun or Star being at C or D. *Fig.* 15

And the apparent place in the Line B C F, or B D H.

So the Angles of *Parallax* are A C B, or E C F; and A D B, or G D H.

In this Scheme, A B repreſents a Quadrant on the Earths ſuperficies.

A the Center of the Earth.

B any point of the Earths Surface.

Refraction

Fig. 12

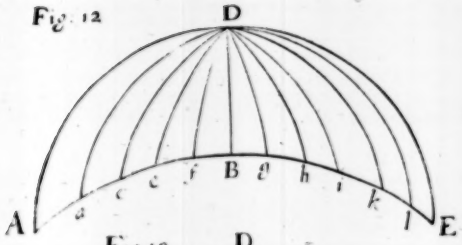
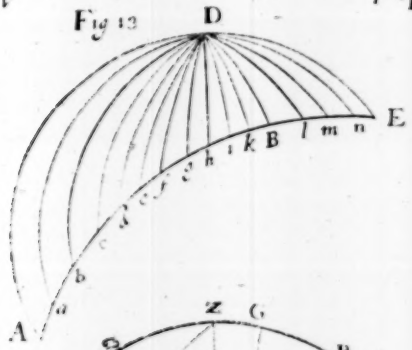


Fig 13



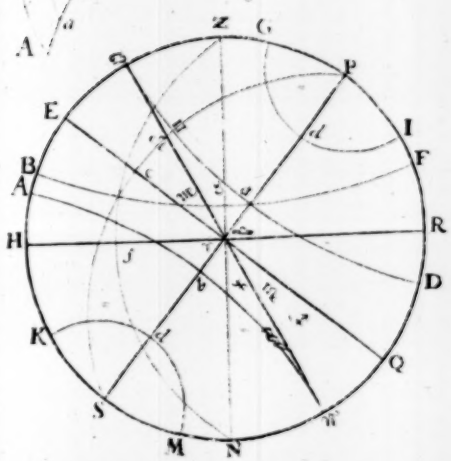


Fig 14

Refraction of the Stars, Observed by Tycho.

Alt.	Refract.	
0°	30′	00″
1	21	30
2	15	30
3	12	30
4	11	00
5	10	00
6	9	00
7	8	15
8	6	45
9	6	00
10	5	30
11	5	00
12	4	30
13	4	00
14	3	30
15	3	00
16	2	30
17	2	00
18	1	15
19	0	30
20	0	00

The *Refraction* is caused by the *Atmosphere*, or Vapourous thickness of the Air near the the Earths superficies, whereby the Sun and Stars seem alwayes to Rise sooner and Set later than really they do.

In the Latitude of 55 degrees and thereabouts, it is allowed to be as follows in the Table; although it varies by the weather.

And in more northern parts, it hath been observed much greater.

The use whereof is this.

Suppose the Altitude observed were 10 degrees; the correspondent refraction is 5 min. 30 seconds, which substracted from 10 deg. the remainder 9 deg. 54 min. 30 seconds, is the true Altitude.

SECT.

SECT. II.

Of Astronomical Problems.

Problem I.

THE Suns Place in the *Ecliptick*, and greateſt Declination being given, to find his preſent Declination.

Example 1.

The Suns Place being in 26° 41′ of *Taurus*, and his greateſt Declination, or the Angle of the *Ecliptick* with the *Equinoctial* 23° 30′; to find the preſent Declination. *Fig.* 16

In the Right-angled Spherical Triangle ♈ B C, There is given ♈ C the *Hypothenuſe* 56° 41′, the Suns Diſtance from *Aries*, and the Angle B ♈ C the greateſt Declination (by the 9th Caſe) to find the Oppoſite Leg B C, the Suns preſent Declination.

Therefore the Proportion and Operation is,

As Radius				Log. 10.00000
To ſ. B ♈ C	23°	30′	the Suns greateſt Declinat.	9.60070
So is ſ. ♈ C	56	41	the Suns Diſtance from ♈	9.92202
To ſ. B C	19	28	the preſent Declinat. N°.	*x*9.52272

Note, That the Suns Diſtance is alwayes accounted, from the neareſt of the Equinoctial Points, *Aries* or *Libra*; therefore if the Sun be in the Northern Signes, *Aries*, *Taurus* or *Gemini*; or in the Southern Signes, *Capricornus*, *Aquarius* or *Piſces*, his Diſtance is computed from *Aries*.

If his place be in the Northern Signes, *Cancer*, *Leo* or *Virgo*; or in the Southern Signes, *Libra*, *Scorpio* or *Sagittarius*, 'tis reckoned from *Libra*.

If

If the Sun be in the Northern Signes, his Declination is *Northerly*; if in the Southern Signes, *Southerly*.

Example 2.

The Suns place 22° 12′ of *Aquarius*, his greatest Declination (as before) 23° 30′; To find his present Declination.

Fig. 16

The Suns Distance from *Aries* is 37° 48′.

The Operation.

In the Right-angled Triangle, ♈ D F.

As Radius			Log.	10.00000
To s. D ♈ F	23°	30′	the greatest Declination	9.60070
So is s. ♈ F	37	48	the Distance from *Aries*	9.78739
To s, D F	14	08	the present Declination S°	9.38809

You may find the Suns place by the Tables in *Astronomia Carolina*.

Problem II.

The Suns place given, to find his Right Ascension.

Note.

The Suns greatest Declination is concluded by Mr. *Street* in his *Caroline* Tables, to be 23° 30′, therefore 'tis alwayes given.

Example 1.

The Suns place is 23° 41′ of *Taurus*.
To find the Right Ascension. *Fig.* 16

In the Right-angled Triangle ♈ B C, there is given the *Hypothenuse*, ♈ C 56° 41′ The Suns place from *Aries*.
The Angle B ♈ C 23° 30′ the greatest Declination (by the sixth Case) to find the adjacent Leg A B the Right Ascension.

The

The Operation.

As Radius				Log. 10.00000
To t. ♈ C	56°	41′	the Suns Long. from ♈	10.18224
So is sc. B ♈ C	23	30	the greatest Declination	9.96240
To t. A B	54	22	the Right Ascen. from ♈	10.14464

Example 2.

The Suns place is 22° 12′ of *Aquarius*,
To find the Right Ascension. *Fig.* 16

The Operation.

In the Right-angled Triangle ♈ D F.

As Radius				Log. 10.00000
To t. ♈ F	37°	48′	the Suns Long. from ♈	9.88968
So is sc. D ♈ F	23	30	the greatest Declination	9.96240
To t. ♈ D	35	25	the R. Asc. from the next Equinoctial Point.	9.85208

This Proportion finds the Right Ascension from the neareſt Equinoctial Point, as you account the Longitude in the Operation. But the Right Ascention is to be reckoned from *Aries*, according to the Order or Succeſſion of the Signes.

Therefore in this laſt *Example*, the Complement of 35° 25′, to 360°, which is 324° 35′, is the Right Ascention ſought.

Problem. III.

The Suns Declination given, to find his place or Longitude from *Aries*.

Example 1.

The Suns Declination is 19 deg. 30 min. North, encreaſing.
To find his place. *Fig.* 16

In

In the Right-angled Triangle ♈ B C.
There is given, the Leg, B C 19° 30′, the Suns present Declination.
The opposite Angle B ♈ C 23° 30′, the greatest Declination.
And the *Hppothenuse* ♈ C required (by the 10th Case) being the Suns Distance from *Aries* or *Libra*.

The Operation.

As s.	B ♈ C	23° 30′	the greatest Declination	Log. 9.60070
To	Radius			10.00000
So s.	B C	19 30	the present Declination	9.52349
T s.	♈ C	56 49	of *Taurus*.	9.92279

Which 56° 49′ reduced into Signes, is 1ˢ 26° 49′,
or 26° 49′ of *Taurus*.

If the Suns Declination be North, and increasing, this proportion finds the Suns Distance from *Aries*, if decreasing, from *Libra*, in the Northern Signes.

If the Suns Declination be South, and increasing, from *Libra*; If decreasing from *Aries*, among the Southern Signes.

Example 2.

The Suns Declination is 14° 10′ South, decreasing.
To find the Longitude from *Aries*.

Fig. 16

The Operation.

In the Triangle ♈ D F.

As s.	D ♈ F,	23° 30′	the greatest Declination.	9.60070
To	Radius			10.00000
So is s.	D F	14 10	the present Declination.	9.38871
To s.	♈ F	37 51	the Distance from ♈	9.78801

The Compl. of 37° 51′, to 360° is 322° 09′,
Which reduced into Signes, is 10ˢ, 22°, 09′, or 22° 09′ of ♒.

Problem. IV.

The Suns Declination given, To find the Right-Aſcenſion.

Example 1.

The Suns Declination is 19° 30′ North increaſing.
To find his Right Aſcenſion.

Fig. 16

In the Right-Angled Triangle ♈ B C,

There is given, the Leg B C 19° 30′, the Suns preſent Declination.
And the oppoſite Angle, B ♈ C 23° 30′, the greateſt Declination (by the firſt Caſe) to find the Leg ♈ B the Right Aſcenſion.

The Operation.

As Radius				Log. 10.00000
To tc. B ♈ C	23°	30′	the greateſt Declination	10.36170
So is t. B C	19	30	the preſent Declination	9.54015
To ſ. ♈ B	54	32	the Right Aſcen. from ♈	ſ 9.90185

The ſame caution which was given for the right accounting the Suns Place in the third *Problem*, ſerves for the Right Aſcenſion, only as that was given in Signes, Degrees and Minutes. This muſt be given in Degrees and Minutes from *Aries*.

Example 2.

The Suns Declination is 14° 10′ South, decreaſing.
To find the Right Aſcenſion.

Fig. 16

The

The Operation.

In the Right-angled Triangle, ♈ D F.

As Radius					Log. 10.00000
To tc. D ♈ F	23°	30′	the Suns greateſt Declinat.		10.36170
So is t. D F	14	10	the preſent Declination		9.40212
To ſ. ♈ F	35	29	the Right Aſcenſion		*9.76382

The Complement of 35° 29′, to 360°, is 224° 31′
The Right Aſcenſion from *Aries*.

Problem. V.

The Latitude of a Place, and the Suns Declination being given, To find the Aſcenſional Difference.

Example.

In the Latitude 51° 32′, the Suns declination being 20° 12′, To find the Aſcentional Difference.

In the Right-angled Triangle a b c,
There is given, the Leg, b c, 20° 12′, the Suns Declination,
And the oppoſite Angle b a c, 38° 28′, the Compl. of the Latitude, or the Angle between the Equinoctial and Horizon; (by the firſt Caſe) To find the other Leg, a b, the Aſcenſional Difference.

Fig. 17

The Operation.

As Radius					Log. 10.00000
To tc. b a c,	38°	28′	the Complement of the Lat.		10.09991
So is t. b c.	20	12	the Suns Declination,		9.56576
To ſ. a b	27	35	the Aſcenſional Difference		*9.66567

Problem. VI.

To find the Oblique Ascension or Descension.

First, Find the *Ascensional Difference* by the fifth *Problem*, and the *Right Ascension* by the fourth *Problem*.

Secondly, If the Suns Declination be Northerly, the *Ascensional Difference Substracted* from the *Right Ascension*, leaves the *Oblique Ascension*, and added to the *Right Ascension*, gives the *Oblique Descension*.

Thirdly, If the Suns Declination be Southerly, the *Ascentional Difference* added to the *Right Ascension*, gives the *Oblique Ascention*; and and substracted there-from, leaves the *Oblique Descension*.

Note,

If the *Right Ascension* be less than the *Ascentional Difference*, add 360° to the *Right Ascension*, and then Substract it there-from; Or if the sum of the *Right Ascension* and *Ascensional Difference* exceeds 360°, reject 360°, the Remainder is the *Oblique Ascension* or *Descension* required.

Problem. VII.

To find the time of the *Suns Rising*, or *Setting*, and consequently the *Length* of the *Day* or *Night*.

First, Find the *Ascensional Difference*, by the fifth *Problem*, which reduced into hours and minutes of time, by allowing for every 15° one hour, and for every deg. less than fifteen, 4 min. of time, and for every 15 min. one minute of time.

Secondly, If the *Suns Declination* be Northerly, the *Ascensional Difference* added to six hours, gives the time of *Suns Setting*.

And substracted there-from, leaves the time of *Sun Rising*.

On the contrary, If the *Suns Declination* be Southerly, the *Ascensional Difference* added to six hours, gives the time of *Sun-Rising*, and substracted there-from, the time of *Sun-Setting*.

Thirdly,

Thirdly, If you double the time of *Sun-Setting*, it gives you the *Length* of the *Day*; And the time of *Sun-Riſe* doubled, the *Length* of the *Night*.

Example 1.

In the Latitude 51 deg. 32 min. North, the *Suns Declination* 20 deg. 12 min. North.
And the *Aſcenſional Difference*, 27° 35′, which reduced into time makes 1 hour, 50 minutes.

	ho.	min.
Therefore the time of *Sun-Setting* is	7	50
The time of *Sun-Riſing*,	4	10
The *Length* of the *Day*,	15	40
The *Length* of the *Night*,	8	20

Example 2.

In the Latitude 51 deg. 32 min. the *Declination* 20 deg. 12 min. South.
And the *Aſcenſional Difference* 27 deg. 35 min. which makes (as before 1 hour, 50 minutes of time.

	ho.	min,
The time of *Sun-Riſing*	7	50
The time of *Setting*,	4	10
The *Length* of the *Day*.	8	20
The *Length* of the *Night*.	15	40

Problem. VIII.

The *Latitude* of a Place, and the *Suns Declination* being given, To find the *Suns Amplitude*.

Example.

In the Latitude 51 deg. 32 min. the *Suns Declination* being 20° 12′, To find the *Amplitude*.

In the Right-angled Triangle a b c, There is given the Leg b c, 20° 12′, and The oppoſite Angle b a c, 38° 28, (By the 19th Caſe) to find the *Hypothenuſe* a c, the *Amplitude*.

Fig. 17

The Operation.

As ſ. b a c,	38°	28′	the Compl. of the Lat.	9.79383
To Radius				10.00000
So is ſ. b c,	20	12	the Declination	9.53829
To ſ. a c,	33	43	the *Amplitude*.	9.74446

If the Suns *Declination* be Northerly, the *Amplitude* is to the Northward of the Eaſt or Weſt; if the *Declination* be Southerly, to the Southward.

Problem. IX.

The *Latitude* of the Place and the *Suns Declination* being given, To find at what time the Sun ſhall be due Eaſt or Weſt.

Example.

In the Lat. 51° 32′ North, The Suns *Declination*, 20° 22′ North, To find at what time the Sun ſhall be due Eaſt or Weſt.

In the Right-angled Triangle a d e, There is given, the Leg d e, 20° 12′, and the oppoſite Angle d a e, 51° 32′ (by the 1 Caſe) To find the Leg a e, the time from ſix.

Fig. 17

The Operation.

As Radius				10.00000
To tc. d a e,	51°	32′	the *Latitude*	9.90009
So is r. d e	20	12	the *Declination*,	9.56576
To ſ. a e,	16	59	the *Diſtance from ſix.*	*x*9.46585

which

Which being reduced into time, makes one hour eight minutes *ferè*, which added to six hours, gives 7 hours, 8 min. at which time the Sun comes to the East; And substracted from 6 hours, leaves 4 hours, 52 min. the time of his being in the *West Azimuth* or *Prime Vertical*.

Problem. X.

The *Latitude* of the Place and the Suns *Declination* bhing given, To find the *Suns Altitude*, being in the East or West *Azimuth* or *Prime Vertical*.

Example.

The Lat. 51° 32′ North, the *Declination*, 20° 12′ North, To find the *Suns Altitude*, being due East or West.

In the Right-angled Triangle a d e, There is given, the Leg, d e, 20° 12′ and The oppofite Angle d a e, 51° 32′ (by the 10th Case) To find the *Hypothenuse* a d.

Fig. 17

The Operation.

As ſ. d a e,	51°	32′	the *Latitude*	9.89374
To Radius				10.00000
So is ſ. d e,	20	12	the *Declination*	9.53819
To ſ. a d,	26	10	the *Alt.* in the *Prime Vert.*	9.64445

Problem XI.

The *Latitude* of a place and the *Suns Declination* being given, To find his *Altitude* at ſix of the Clock.

Example.

In the Lat. 51° 32′ North, the *Declination* 23° 30′ North, To find the *Suns Altitude* at ſix.

In

In the Right-angled Triangle a b c, There is given, the *Hypothenuse* a c, 23° 30′; and the Angle b a c, 51° 32′, (by the 9th Case) to find the *Opposite Leg* b c.

Fig. 15

The Operation.

As Radius				Log. 10.00000
To s. a c	23°	30′	the Declination	9.60070
So is s. b a c	51	32	the Latitude	9.89374
To s. b c	18	11	the Altitude at six,	*x* 9.49444

Problem. XII.

The Latitude of a place and the Suns Declination being given, to find his *Azimuth* at Six.

Example.

In the Latitude 51° 32′ North, the Declination 23° 30′ North, To find the Suns *Azimuth* at six of the Clock.

In the Right-angled Triangle a b c, There is given, the *Hypothenuse* a c, 23° 30′, and the Angle b a c 51 deg. 32 min. (by the sixth Case) To find the adjacent Leg a b.

The Operation.

As Radius				Log. 10.00000
To t. a c	23°	30′	the Declination	9.63830
So is sc. b a c	51	32	the Latitude	9.79383
To t. a b	15	08	the *Azimuth* from the N°.	*x* 9.43213

Problem XIII.

The Latitude of the place, and the Suns Altitude and Declination being given, To find his *Azimuth*.

Example.

Example 1.

In the Latitude 51 deg. 32 min. North, the Declination 23 deg. 30′ North, the Altitude 49 deg. 40 min. To find the Suns *Azimuth*.

In the Oblique-angled Triangle D P Z, there is given the three Sides Z P, 38 deg. 28 min. the Compl. of the Latitude P D 66 deg. 30 min. the Compl. of the Declination, or the Suns Diſtance from the Elevated Poſe, and D Z 40 deg. 20 min. the Compl. of the Altitude, (by the 11th Caſe) to find the Angle D Z P, the *Suns Azimuth* from the North.

Fig. 18

The Operation.

The Legs	A D	40°	20′	Sine	——	Co. Ar.	0.18894
	D E	38	28	Sine	——	Co. Ar.	0.20617
The Baſe	A E	66	30	½ Sum	72° 39′	Sine	Log.	9.97978
Sum		145	18	Rem.	06 09	Sine		9.02639
½ Sum		72	39	——	——	——	Sum	19.40128
Rem.		06	09	ſ.	59° 52′	——	½ Sum,	9.70064

Which doubled 59 52 produces

The Suns *Azimuth* 119 44 from the North.

Example 2.

In the Lat. 51 deg. 32 North, the Suns Declination is 15 degrees, 16 minutes South; and his Altitude, 19 deg. 37 min. To find his *Azimuth* from the North.

Fig. 19

The Operation.

In the Triangle D P Z,
There is given, P Z 38 deg. 28 min.
D Z 70 deg. 23 min. D P 105 deg. 16 min. and D Z P required.

The Legs	∠ A D	70° 23′	Sine ——		Co. Ar.	0.02597
	∠ D E	38 28	Sine ——		Co. Ar.	0.20617

The Base	A E	105 16	½ Snm	107° 03′	Sine Log.	9.98048
Sum,		214 07	Rem.	01 47	Sine	8.49304
½ Sum,		107 03			Sum,	18.70566
Rem.		01 47	ſc.	76 59	½ Sum.	9.35275
		Which doubled		76 59	produces	
		The Suns *Azimuth*		153 58	from the North.	

Example 3.

In the Latitude 51 degrees 32 minutes South, the Suns Declination is 23 degrees 30 minutes South, and his Altitude 49 degrees 40 minutes; To find his *Azimuth* from the South.

In the Triangle D P Z, D muſt repreſent the South Pole; Then there is given P Z 38 degrees 28 minutes, the Complement of the Latitude; D Z 40 degrees 20 minutes, the Complement of the Altitude; P D 66 degrees 30 minutes, the Complement of the Declination, or the Suns Diſtance from the Elevated (or South) Pole; To find P D Z, the Suns *Azimuth* from the South.

Fig. 18

The Operation is the ſame with the firſt *Example*, onely, as the *Azimuth* there was accounted from the North, this finds it from the South part of the Horizon, which is 119 degrees 44 minutes.

Example 4.

In the Latitude 51 degrees 32 minutes South, the Suns Declination is 15 degrees 16 minutes North, and his Altitude 19 degrees 37 minutes; To find his *Azimuth* from the South.

In the Triangle D P Z, P repreſents the South Pole, as in the former *Example*. *Fig.* 19

Then

Then there is given P Z 38 degrees 28 minutes, D Z 70 degrees 23 minutes, P D 105 degrees 16 minutes; and D Z P required.

Fig. 19

The Operation is the same with the second *Example*, only the *Azimuth* found is to be accounted from the South, which will be found 153 degrees 58 minutes.

Problem. XIV.

The Latitude of the Place, the Suns Declination and Altitude being given; To find the Hour of the Day.

Example 1.

In the Latitude 51 degrees 32 minutes North, the Suns Declination is 23 deg. 30 min. North, and his Altitude 49 deg. 40 min. To find the hour from Noon.

In the Triangle D P Z, There is given P Z 38 degrees 28 minutes, D Z 40 degrees 20 minutes, D P 66 degrees 30 minutes; and D P Z the hour from Noon required.

Fig. 18

The Operation.

The Legs	D P	66°	30′	Sine			Co. Ar.	0.03760
	P Z	38	28	Sine			Co. Ar.	0.20617
The Base	D Z	40	20	½ Sum	72°	39′ Sine	Log.	9.97978
Sum,		145	18	Rem.	32	13 Sine		9.72683
½ Sum,		72	39				Sum,	19.95038
Rem.		32	13	Sc.	19	11	½ Sum,	9.97519

The Double of 19 degrees 11 minutes is, 38 degrees 22 minutes, which being reduced into time, gives 2 hours 33 minutes from noon; So that the hour of the day is either 1 hour 53 minutes *P. M.* or Afternoon, or 9 hours 27 minutes *A. M.* or before Noon.

Example 2.

In the Latitude 51 deg. 32 minutes North, the Suns Declination 15 degrees 16 minutes South, and his Altitude 19 degrees 37 minutes; To find the hour *P. M.* or Afternoon.

In the Triangle D P Z, There is given, the three Sides, P Z 38 deg. 28 min. D Z 70 deg. 23 min. P D 105 deg. 16 min. and D P Z required.

Fig. 19

The Operation.

The Legs	P D	105°	16′	Sine		Co. Ar.	0.01560
	P Z	38	27	Sine		Co. Ar.	0.20617
The Base	D Z	70	23	½ Sum,	107° 03′	Log.	9.98048
Sum,		214	07	Rem.	36 40		9.77609
½ Sum		107	03				19.97834
Rem.		36	40	Sc.	12° 44′		9.98917

Which doubled, produces 25 deg. 28 min. and that reduced into time, makes 1 hour 42 minutes, *ferè*.

Problem. XV.

The Latitude of a place, the Suns Declination, and the hour of the day given, to find the Suns Altitude.

Example.

In the Lat. 51° 32′ North, the Suns *Declination* is 23° 30′ North, the hour, 1ho. 53 min.

To find the *Suns Altitude*.

1 Hour 53 minutes reduced, makes 18 degrees 15 minutes.

In

In the Triangle D P Z, There is given, the two Sides P Z 38° 28′, D P 66° 30′, and the contained Angle D P Z 28° 15′, and the third Side D Z required.

Fig. 18

The Operation.

As Radius				Log. 10.00000
To sc. D P Z	28°	15′	the contained Angle,	9.94492
So is t. P Z	38	28	the lesser Side	9.90009
To t.	34	59	a fourth Arch.	*9.84501

From the other side P D.	66°	30′
Substract the fourth Arch,	34	59
The Rem. is the Residual Arch,	31	31

				Co. Ar.
As sc.	34°	59′	the fourth Arch	0.08655
To sc.	31	31	the Residual Arch,	9.93069
So sc. P Z	38	28	the Lesser Side	9.89374
To sc. D Z	35	27	the Side sought	*9.91098

Whose Compl. 54 33 is the Altitude required.

Problem. XVI.

The Latitude of a Place, the Suns Declination, and the Hour given, To find the Suns *Azimuth*.

Example.

In the Latitude 51 deg. 32 min. North, the Suns Declination is 15 deg. 16 min. South, and the Hour 10^{ho} 18′ in the morning; To find the Suns *Azimuth*.

The time from noon is 1 hour 42 min.
Which reduced, is 25 deg. 30 min.

In.

In the Triangle D P Z; There is given, the two Sides P Z 38 degrees 28 minutes, P D, 105 deg. 16 min. and the contained Angle D P Z 25 degrees 30 minutes. To find one of the opposite Angles, *viz.* P D Z.

Fig. 19

The Operation.

P D,	105°	16′				
P Z,	38	28				
Sum,	143	44	½ Sum,	71°	52′	} D P Z 25° 30′
Diff.	66	48	½ Diff.	33	24	} the ½ 12° 45′.

			Co. Ar.
As s. ½ Z cr'. D P and P Z,	71°	52′	0.02212
To s. ½ X cr'.	33	24	9.74074
So is tc. ½ D P Z	12	45	10.64536
To t. ½ X ∨∨ P D Z and P Z D	68	39	10.40822

			Co. Ar.
As sc. ½ Z cr'. D P and P Z	71°	52′	0.50692
To sc. ½ X cr'.	33	24	9.92152
So is tc. ½ D P Z	12	45	10.64536
To t. ½ Z ∨∨ P D Z and P Z D	85	10	11.07380

½ Z ∨∨	85°	10′
½ X ∨∨	68	39
Sum,	153	49 D Z P required.

Which is the Suns *Azimuth* from the North.

Problem. XVII.

The Latitude of a Place, the Suns Altitude and *Azimuth* given; to find the hour.

Example.

Example.

In the Latitude 51 deg. 32 min. the Suns Altitude is 49 degrees 40 min. His *Azimuth* 119 deg. 44 min. from the North; To find the hour *P. M.*

In the Triangle D P Z, There is given, the two Sides D Z 40 deg. 20 min. P Z 38 deg. 28 min. and the contained Angle D Z P 119 deg. 44 min. and the oppoſite Angle D P Z required.

Fig. 18

The Operation.

D Z	40° 20′			
P Z	38 28			
Sum,	78 48	½ Sum, 39° 24′	} D Z P 119° 44′	½ 59° 52′
Diff.	01 52	½ Diff. 00 56	}	

		Co. Ar.
As ſ. ½ Z cr. D Z and P Z	39° 24′	0.19741
To ſ. ½ X cr.	00 56	8.21189
So is tc. ½ D Z P	59 52	9.76377
To t. ½ X *v v* P D Z and D P Z	00 51	*x* 8.17307

		Co. Ar.
As ſc. ½ Z cr. D Z and P Z	39° 24′	0.11197
To ſc. ½ X cr.	00 56	9.99994
So is tc. D Z P	59 52	9.76377
To t. ½ Z *v v* P D Z and D P Z	36 54	*x* 9.87568

½ Z *v v*	36° 54′		
½ X *v v*	00 51		
Sum,	37 45	D P Z required.	

Note, D P Z is the greater Angle becauſe oppoſite to the greater Side D Z, 37 degrees 45 minutes Reduced, makes the time 2 hours, 31 minutes *P. M.*

Problem. XVIII.

The *Latitude* and *Longitude* of a fixed Star being given, To find the *Right-Aſcenſion* and *Declination*.

Example.

The Longitude of *Caſtor* is 15 deg. 33 min. of *Cancer*, and his Latitude 10 deg. 02 min. North; to find his Right Aſcenſion and Declination.

In the Oblique Triangle D I P, There is given, the two Sides, I P 23 deg. 30 min. the Diſtance between the *Pole* of the *Equinoctial*, and the Pole of the *Ecliptick*, I D 79 deg. 58 min. the Complement of the Latitude; and the contained Angle D I P 15 deg. 33. min. the Longitude from *Cancer*; To find one of the oppoſite Angles, D P I, the Complement to 180 deg. of the Right-Aſcenſion from *Cancer*; and the third Side D P, the Complement of Declination.

Fig. 20

The Operation.

For the Right Aſcenſion.

I D	79°	58′			
I P	23	30			
Sum,	103	28	½ Sum,	51° 44′	} D I P 15° 33′, ½ D I P 7° 46′.
Diff.	56	28	½ Rem.	28 14	

			Co. Ar.
As ſ. ½ Z cr². I D and I P,	51°	44′	0.10505
To ſ. ½ X cr².	28	14	9.67492
So is tc. ½ D I P	07	46	10.86521
To t. ½ X ∨ ∨ D P I, and I D P	77	14	10.64518

A

Fig 16

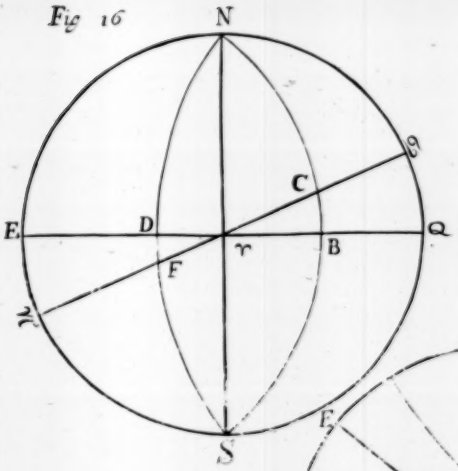


Fig 15

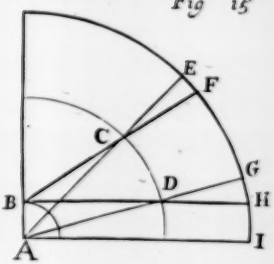


Fig 17

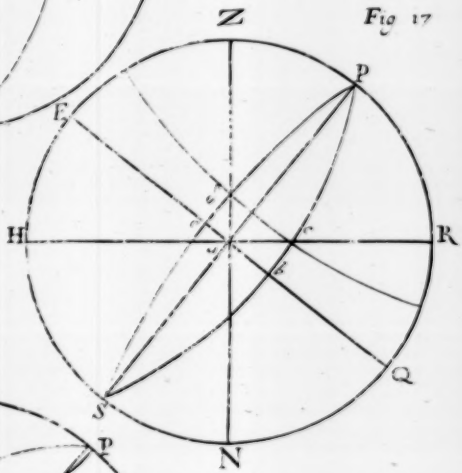
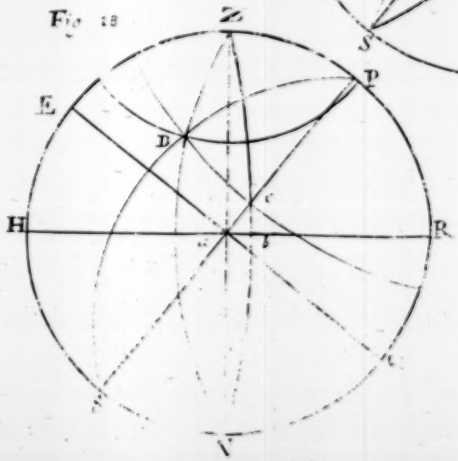


Fig 18



			Co. Ar.
As ſc. ½Z cr.	ID and IP	51° 44′	0.20808
To ſc. ½X cr.		28 14	9.94499
So is tc. ½DIP		07 46	10.80521
To t. ½Z VV	DPI and IDP	84 31	11.01828

½Z VV 84° 31′
½X VV 77 14
Sum, 161 45 DPI. Whoſe

Compl. to 180° is 18° 15′, the *Right Aſcenſion* from *Cancer*; the *Right Aſcenſion* of *Cancer* is 90°, and therefore the *Right Aſcenſion* from *Aries* is 108° 15′.

For the *Declination*.

			Co. Ar.
As ſ. DPI,	161° 45′	the Compl. of the Right Aſcen.	0.50423
To ſ. DI	79 58	the Compl. of Latitude,	9.99331
So is ſ. DIP	15 33	the Longitude from *Cancer*	9.42826
To ſ. DP	57 28	the Compl. of Declination.	9.92580

Whoſe Compl. 32 32 is the Declination Northerly.

Problem. XIX.

The Right Aſcenſion and Declination of a fixed Star being given; To the Longitude and Latitude thereof.

Example.

The Right Aſcenſion of *Caſtor* is 108° 15′, and his Declination 32° 32′ North; To find his Longitude and Latitude.

In the Triangle IDP, there is given; the two Sides IP, 23 deg. 30 min. PD 57 deg. 28 min. and the contained Angle DPI 161 deg. 45 min. To find the oppoſite Angle DIP, and the third Side DI.

Fig. 20

The Operation.

To find the Longitude.

P D,	57° 28′				
I P,	23 30				
Sum,	80 58	½ Sum,	40° 29′	} DPI	161° 45′
Diff.	33 58	½ Diff.	16 59	} the ½ DPI	80° 52′

		Co. Ar.
As s. ½ Z cr. PD and IP,	40° 29′	0.18760
To s. ½ X cr.	16 59	9.46552
So is tc. ½ DPI	80 52	9.20621
To t. ½ X VV DIP and IPD	04 08	8.85933

		Co. Ar.
As sc. ½ Z cr. PD and IP	40° 29′	0.11874
To sc. ½ X cr.	16 59	9.98063
So is tc. ½ DPI	80 52	9.20621
To t. ½ Z VV DIP and IDP	11 25	9.30558

½ Z VV	11° 25′	
½ X VV	04 08	
Sum,	15 33	DIP the Longitude from *Cancer*.

To find the Latitude.

				Co. Ar.
As s. DIP	15° 33′	the Longitude from *Cancer*		0.57174
To s. DP	57 28	the Compl. of the Declination,		9.92587
So is s. DPI	161 45	the Compl. of Right Aſcenſion,		9.49577
To s. DI	79 58	the Compl. of the Latitude.		9.99338

Prob.

Problem. XX.

The Distance of a *Planet*, *Comet* or *New Star*, from two known fixed Stars being given; To find the unknown *Stars* Longitude and Latitude.

Example.

The unknown *Stars* Distance from the *Swans Beak* is 49 deg. 05 min. and from *Perseus's Side* 88 deg. 57 min. To find the Longitude and Latitude.

The Long.	Of the *Swans Beak*	♍ 26° 36′	Lat.	49° 12′	N°.
	Of *Perseus's Side*	♉ 27 12		30° 05	N°.

1. In the Triangle A D I there is given, the two Sides A I 40 deg. 58 min. the Complement of the Latitude of the *Swans Beak*; D I 59 deg. 55 min. the Complement of the Latitude of *Perseus's Side*; the contained Angle A I D 120 deg. 23 min. the Difference of Longitude between the two *Stars* and the *Opposite Angle* D A E, and the Side A D required.

Fig. 21

The Operation.

		Co. Ar.
As s. ; Z cr¹. A I and D I	50° 26′	0.11301
To s. ; X cr¹.	09 28	9.21610
So is tc. ; D A I	60 11	9.75822
To t. ; X *V V* D A I and A D I	07 01	*9.08733

		Co. Ar.
As sc. ; Z cr¹. A I and D I	50° 26′	0.19588
To sc. ; X cr¹.	09 28	9.99404
So is tc. ; D A I	60 11	9.75822
To t. ; Z *V V* D A I and A D I	41 35	*9.94814

The Angle C A I is 48° 36′.

		Co. Ar.
As ſ. D A I ——	48° 36′ ——	0.12487
To ſ. D I ——	59 55 ——	9.93716
So is ſ. A I D ——	120 23 ——	9.93584
To ſ. A D ——	84 20 ——	9.99787

2. In the Triangle *A D B* there is given, the three Sides *A D* 84° 20′ the Diſtance between the two known Stars, A B 49 deg. 05 the unknown Stars Diſtance from the *Swans Beak*, *B D* 88 deg. 57 min. the Diſtance from *Perſeus's Side*; and the Angle *A B D* required.

Fig. 21

The Operation.

A D	84° 20′	Sine			Co. Ar.	0.00213
A B	49 05	Sine			Co. Ar.	0.12167
B D	88 57	½ Sum	111° 11′	Sine		9.96961
Sum,	222 22	Rem.	22 14	Sine		9.57793
½ Sum,	111 11				Sum,	19.67134
Rem.	22 14	Sc.	46° 46′	½ Sum,		9.83567

Which being doubled, makes 93° 32′ the Angle A B D, which being added to the Angle D A I, the Sum is the Angle B A I 142° 08′

3. In the Triangle A B I, there is given the two Sides A I 40 deg. 58 min. A B 49 deg. 05 min. the contained Angle B A I 142 deg. 08 min. and the oppoſite Angle A I B, the Difference of Longitude between the unknown *Star* and the *Swans Beak*, and the Side B I, the Complement of the unknown *Stars* Latitude required.

Fig. 21

The Operation.

			Co. Ar.
As ſ. ½ Z cr. A I and A B	45° 01′		0.15039
To ſ. ½ X cr. —— ——	04 03 ——	——	8.84897
So is tc. ½ B A I ——	71 04 ——	——	9.53533
Tot. ½ X ∨ ∨ A B I and A I B	01 57 ——	——	8.53479

As

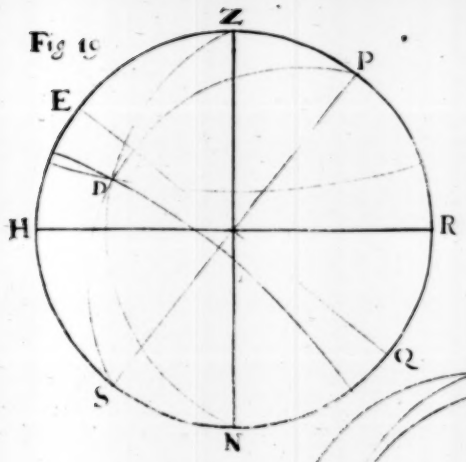


Fig 19

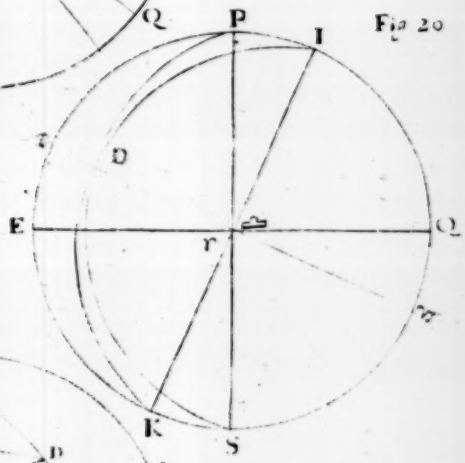


Fig 20

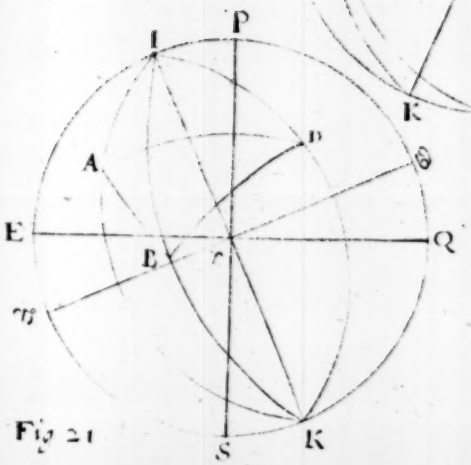


Fig 21

		Co. Ar.
As sc. ½ Z cr^a. A I and A B	45° 01′	0.15064
To sc. ½ X cr^a. ———	04 03	9.99891
So is tc. ½ B A I ———	71 04	9.53533
To t. ½ Z ∨∨ A B I and A I B	25 49	x9.68488

The Angle A I B is 27 deg. 46 min. which added to the Longitude of the *Swans Beak* ♑ 26 deg. 39 minutes, makes the unknown *Stars* Longitude to be ♒ 24 degrees 25 minutes.

		Co. Ar.
As s. A I B ———	27° 46′ ———	0.33173
To s. A B ———	49 05 ———	9.87833
So is s. B A I ———	142 08 ———	9.78804
To s. B I ———	84 39 ———	x9.99810

Whose Complement 05 degrees, 21 minutes, is the unknown *Stars* Latitude Northerly.

Problem. XXI.

The *Meridian Altitude* of an unknown *Star* or *Planet*, and the Distance from a known *fixed Star* being given; to find the unknown *Stars* Latitude and Longitude.

Example.

In the Latitude 51 degrees, 32 minutes North, the *Meridian Altitude* of an *unknown Star* is 30 degrees, 36 minutes, and his distance from the *Star* in *Cepheus's Girdle* is 84 degrees, 32 minutes; To find his *Longitude* and *Latitude*.

The *Meridian Altitude* of the Star being given, his *Declination* is also given.

For the *Meridian Altitude* substracted from the Complement of the *Latitude* 38 degrees 22 minutes, There remains, 7 degrees 52 minutes, the *Declination* South.

First, Therefore in the Triangle A O P, there is given, the three Sides, O P, 20 degrees 52 minutes, the *known Stars Distance* from the

the *North Pole*, A P 97 degrees, 52 min. the *unknown Stars Diſtance* therefrom, A O 84 deg. 32 min. the *Diſtance* between the two *Stars*; and the Angle A P O required, being the *Difference* of *Longitude* between the two *Stars*.

Fig. 22

The Operation.

O P	20° 52′	Sine	Co. Ar.	0.44831
A P	97 52	Sine	Co. Ar.	0.00409
½ Snm	101 36	Sine		9.99104
Rem.	17 06	Sine		9.46841
			Sum,	19.91185
	Sc. 25° 23′		½ Sum	9.95592

Which doubled, is 50 degrees 45 minutes, the Angle A P O.

The *Right Aſcenſion* of *Cepheus*'s *Girdle* is, 321 degrees, 02 minutes, to which adding 50 degrees 46 minutes, produceth the *Right Aſcenſion* of the *unknown Star*, 11 degrees 48 minutes.

Secondly, Then having the unknown *Stars Right Aſcenſion*, and *Declination*, you may find his *Longitude* and *Latitude* by *Problem* 19.

Problem. XXII.

Having the *Latitude* of the place, the Suns *Right Aſcenſion*, and the *Altitude* of a *known fixed Star*; to find the *hour* of the *Night*.

Example.

In the *Latitude* 51 deg. 32 min. the *Suns Right Aſcenſion* being 228 degrees, 45 minutes, and the *Altitude* of *Aldebran* 38 deg. 58 min. To find the *hour* of the *Night*.

The *Right Aſcenſion* of *Aldebran* is 64 degrees, 10 minutes, and his *Declination* 15 degrees, 46 minutes.

In

In the Triangle A P Z, there is given the three Sides P Z 38 deg. 28 min. the Complement of the *Latitude*; A Z 51 deg. 02 min. the Complement of the *Stars Altitude*; A P 74 deg. 14 min. the Compl. of his *Declination*; to find the Angle A P Z the Difference of his *Right Aſcenſion* between the *Medium Cœli* and *Aldebran*.

Fig. 23

The Operation.

A P	Sine	74°	14′	Co. Ar.	0.01665
P Z	Sine	38	28	Co. Ar.	0.20617
½ Sum	Sine	81	52		9.99561
Rem.	Sine	30	50		9.70973
				Sum,	19.92816
	Sc.	22°	59′	½ Sum,	9.96408

Which doubled, produces 45 degrees 58 minutes.

This ſubſtracted from the *Right Aſcenſion* of *Aldebran*, leaves 18 deg. 12 min. the *Right Aſcenſion* of the *Mid Heaven*. Add 360 degrees to 18 degrees 12 minutes, and from the Sum ſubſtract the Suns *Right Aſcenſion* 228 deg. 35 min. the Remainder 149 deg. 27 min. reduced to time, makes 9 hours, 57 minutes, 48 seconds, the *hour* of the *Night* ſought.

Problem XXIII.

The *Azimuth* and *Altitude* of a *known Star* being given, to find the *Latitude* of the Place.

Example.

The *Altitude* of *Aldebran*, is 38 degrees 58 minutes, and his *Azimuth* S. E. 61 deg. 05 min. To find the *Latitude* of the Place.

In the Triangle A P Z, there is given two Sides; A Z 51 deg. 02 min. the Compl. of the *Stars Altitude*, A P 74 deg. 14 min. the Compl. of his *Declination*; and the oppoſite Angle A Z P, 118 deg. 55 min. the *Azimuth* from the South; and the third Side P Z required, being the Compl. of the *Latitude*. *Fig.* 23

The

The Operation.

				Co. Ar.
As s. A P	74°	14′		0.01665
To s. A Z P	118	55		9.94217
So is s. A Z	51	02		9.89071
To sc. A P Z	45	00		x9.84953

			Co. Ar.
As t. ½ X V V A Z P and A P Z	36°	57′	0.22104
To s. ½ Z V V	81	57	9.99570
So is t. ½ X cr. A P and A Z	11	36	9.31233
To t. ½ P Z	18	40	x9.52907

Which being doubled, produces 57 deg. 20 min. Whose Compl. 52 deg. 40 min. is the Latitude Northerly.

Problem. XXIV.

Two *unequal Altitudes* of the *Sun* taken in one day, with the *time* between the *Observations*, and the *Suns Declination* being given; To find the *Latitude* of the Place of *Observation*.

Example.

The two *Altitudes* are 43 deg. 06 min. and 56 deg. 34 min. the *time* between the *Observations* is two *hours*, and the *Suns Declination* 20 degrees, 14 minutes North; To find the *Latitude* of the *Place*.

In the Right-angled Triangle A B P, There is given the *Hypothenuse* A P, 69 degrees 46 minutes, the Compl. of the *Declination*, the *Angle* A P B 15 degrees, half the *time* between the *Observations*, and the opposite *Leg* A B required.

Fig. 24

The

The Operation.

As Radius			Log. 10.00000
To ſ. A P B	15°	00′	9.41300
So is ſ. A P	69	46	9.97234
To ſ. A B	14	03	*9.38534

Which being doubled, gives A E 28 degrees, 06 minutes.

Secondly, In the *Oblique Angled Triangle* A P E, there is given, the two Sides, A E, 28 deg. 06 min. E P 69 deg. 46 min. the oppoſite *Angle* A P E 30 deg. 00 min. and the other oppoſite *Angle* A E P required.

Fig. 24

The Operation.

			Co. Ar.
As ſ. A E	28°	06′	0.32697
To ſ. A P E	30	00	9.69897
So is ſ. E P	69	46	9.97234
To ſ. E A P	84	54	*9.99828

Thirdly, In the *Oblique Angled Triangle* A Z E, there is given the three Sides A Z, 33 deg. 26 min. the Compl. of the greater *Altitude*, E Z 46 deg. 54 min. the Compl. of the leſſer A E 28 deg. 06 min. and the *Angle* E A Z. required.

Fig. 24

The Operation.

A Z	Sine	33°	26′	Co. Ar.	0.25887
A E	Sine	28	06	Co. Ar.	0.32697
½ Sum	Sine	54	13	Log.	9.90515
Rem.	Sine	07	19		9.10501
				Sum,	19.60000
	Sc.	50	52	½ Sum,	9.80000

Which doubled, produces E A Z 101 deg. 44 min. From which ſubſtracting E A P 84 deg. 54 min. there remains P A Z 16 deg. 50 min.

Fourthly, In the *Oblique-Angled Triangle* A P Z, there is given, the two *Sides* A P 69 deg. 46 min. A Z 33 deg. 26 min. the contained *Angle*, P A Z, 16 deg. 50 min. and the third *Side* P Z required.

Fig. 24

The Operation.

As Radius			Log. 10.00000
To ſc. P A Z	16°	50′	9.98098
So is t. A Z	33	26	9.81968
To t. of a fourth Arch	32	17	x9.80066

			Co. Ar.
As ſc. of the fourth Arch,	32°	17′	0.07293
To ſc. of the reſidual,	37	29	9.89956
So is ſc. A Z	33	26	9.92144
To ſc. P Z	38	26	x9.89393

Whoſe Compl. 51° 34′ is the Latitude Northerly.

Problem XXV.

Two unequal *Altitudes* of the *Sun*, and the *Correſpondent Azimuths* taken in one day, and the *Suns Declination* being given; to find the *Latitude* of the *Place of Obſervation*.

Example.

The *firſt Altitude* is 43 deg. 06 min. and the *Correſpondent Azimuth* 65 deg. 16 min. S. E. The *ſecond Altitude* 56 deg. 35 min. the *Azimuth* 26 deg. and the *Suns Declination* is 20 deg. 14 min. North: To find the *Latitude* of the *Place*.

Firſt, In the *Oblique-Angled Triangle* A E Z, there is given, the two *Sides* A Z 33 deg. 26 min. E Z 46 deg. 54 min. the contained *Angle* A Z E 39 deg. 16 min. the *Difference* of the *Azimuths*; and *Angle* E A Z, and the *third Side* A E required.

Fig. 24

The

The Operation.

		Co. Ar
As ſ. ½ Z cr. AZ and EZ,	40° 10′	0.19043
To ſ. ½ X cr.	06 44	9.06911
So is tc. ½ AZE	19 38	10.44765
To t. ½ X ∨ ∨ EAZ and AEZ	27 00	×9.70719

		Co. Ar.
As ſc. ½ Z cr. AZ and EZ	40° 10′	0.11681
To ſc. ½ X cr.	06 44	9.99700
So is tc. ½ AZE	19 38	10.44765
To t. ½ Z ∨ ∨ EAZ and AEZ	74 39	10.56146

The Angle EAZ is 101° 39′.

		Co. Ar.
As ſ. EAZ	101° 39′	0.00904
To ſ. EZ	46 54	9.86342
So is ſ. AZE	39 16	9.80136
To ſ. AE	28 09	×9.67382

Secondly, In the *Right-angled Triangle* ABP there is given the *Hypothenuſe* AP 69 deg. 46 min. the *Leg* AB 14 deg. 04 min. the half of AE; and the *Adjacent Angle* BAP required.

Fig. 24

The Operation.

As Radius		10.00000
To tc. AP	69° 46′	9.56654
So is t. AB	14 04	9.39892
To ſc. BAP	84 42	×8.96546

From the *Angle* EAZ 101 deg. 39. min. ſubſtract the *Angle* EAP 84 deg. 42 min. there remains the *Angle* PAZ, 16 deg. 57 min.

Thirdly, In the *Oblique-Angled Triangle* PAZ, there is given the two *Sides* AP 69 deg. 46 min. AZ 33 deg. 26 min. the contained *Angle* PAZ 16 deg. 57 min. and the third *Side* PZ required.

Fig. 24

The Operation.

As Radius			Log. 1000 000
To sc. P A Z	16°	57′	9.98071
So is t. A Z	33	26	9.81968
To t. of a fourth Arch	32°	16′	*9.80039
			Co. Ar.
As sc. of the fourth Arch	32	16	0.07285
To sc. of the Residual	37	30	9.89947
So is sc. A Z	33	26	9.92144
To sc. P Z	38	28	*9.89376

Whose Compl. 51° 32′ is the Latitude North.

SECT. III.

Containing some general Astronomical Theories.

Of the Ptolomaick System.

THE *Ptolemaick System* is that which was first invented; and supposeth the Earth to be Fixed as the Center of the World, and that all the Celestial Bodies move round the same in their Diurnal and Annual Revolutions.

The World is supposed to be divided principally into two parts, Elementary and Celestial.

The Elementary admits of four Divisions:

The first is the *Earth*.

The second is the *Water*; both which make one entire Body or Globe, whereon we dwell.

The third is the *Air*, encompassing the *Earth*.

And the fourth is the *Fire*; which according to the Opinion of Philosophers is contained in that space between the *Air* and the Sphere of the *Moon*; As you may see in the following Figure.

The

Fig 22

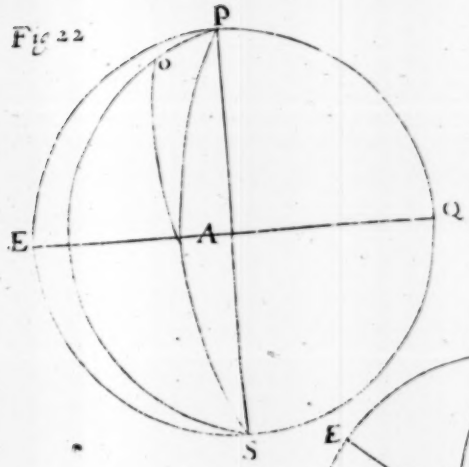


Fig 23

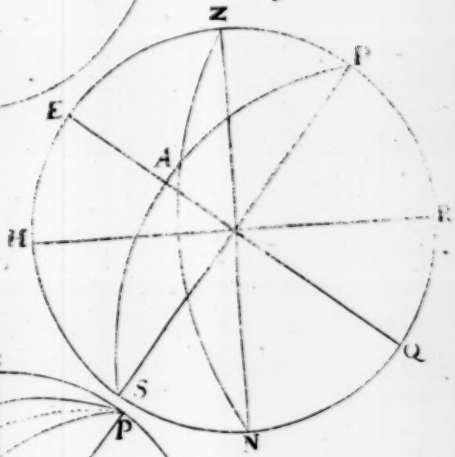
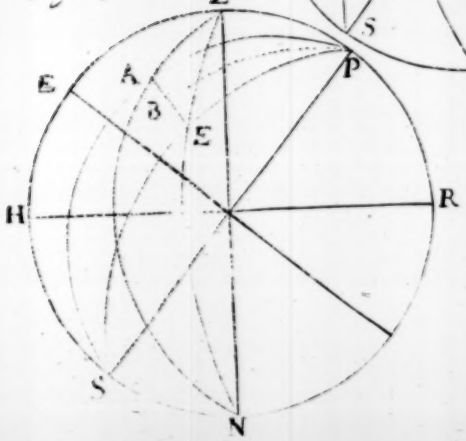


Fig 24



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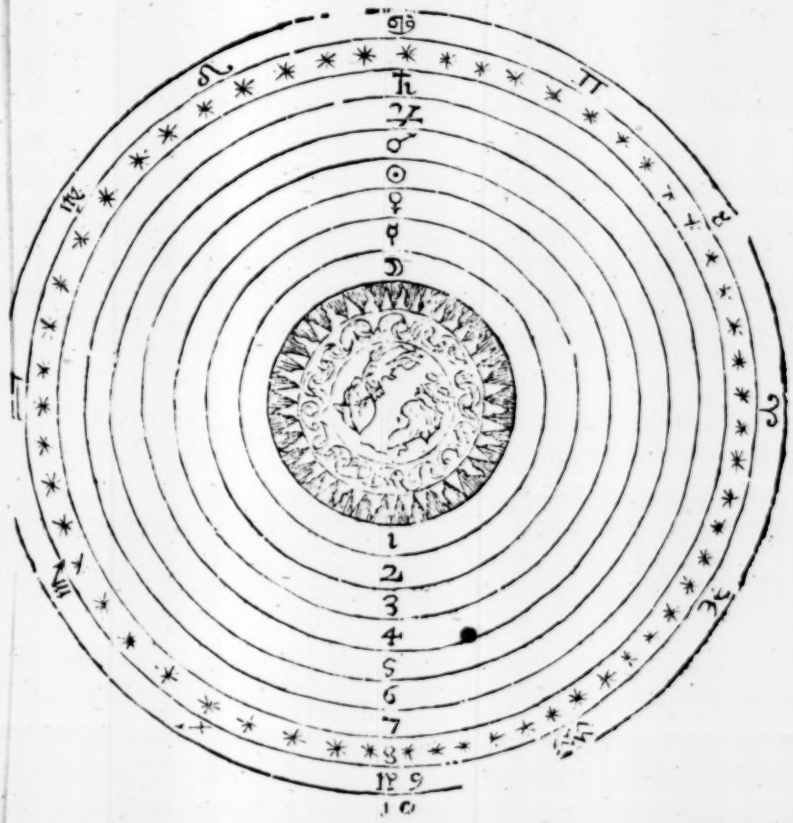
The Figure of the Ptolomaick Systeme.



These four Elements are subject to a continual Change and Alteration one into another; according to the Proverb,

Omnia sub-Lunaria Mutabilia.

The Celestial part is that which is without these Elementary parts, void

void of all Changes; and is by the Antient *Aſtronomers* divided into ten Parts or Heavens.

The firſt of which, next to the Region of *Fire*, is the Heaven or Orb of the *Moon*.

The ſecond of *Mercury*.
The third of *Venus*.
The fourth of the *Sun*.
The fifth of *Mars*.
The ſixth of *Jupiter*.
The ſeventh of *Saturn*.
The eighth of the *Fixed Stars*.
The ninth is called the *Cryſtaline Heaven*.
The tenth the *Primum Mobile*.

The Magnitude of theſe Heavens are known by their Courſes, which thoſe great Bodies within them make round the Poles of the *Zodiack*.

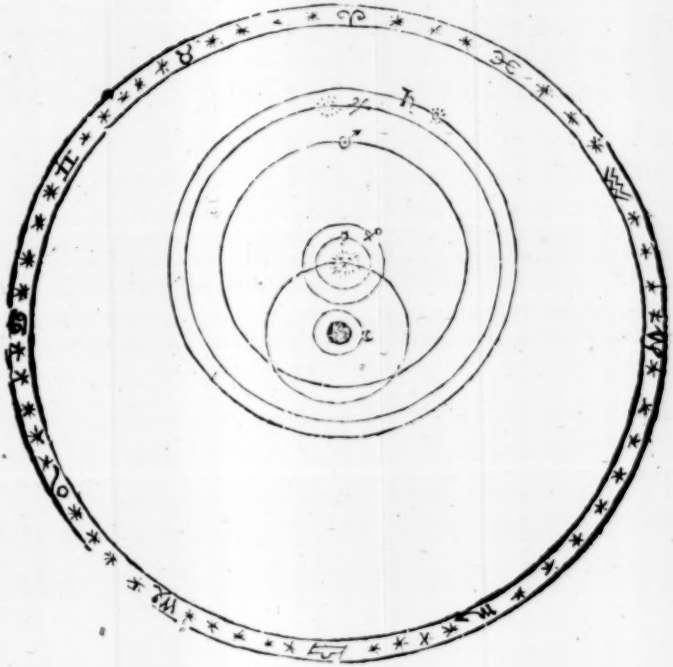
The *Moon* runneth through the Heaven, by her own natural Courſe, from *Weſt* to *Eaſt* in 27 Dayes, 8 Hours.

Mercury in 88 Dayes.
Venus in 225 Dayes.
And the *Sun* in a Year.
Mars in two Years.
Jupiter in 12 Years.
Saturn in 30 Years.

The *Eighth Heaven* perfects its Courſe, according to the affirmation of *Tycho Brahe*, in 25400 Years.

Theſe Heavens are turned about upon the *Axis* of the World by the tenth Heaven, which is the *Primum Mobile* or *Firſt Mover*, by which motion is cauſed Day and Night, and the daily riſing and ſetting of the Heavenly Lights.

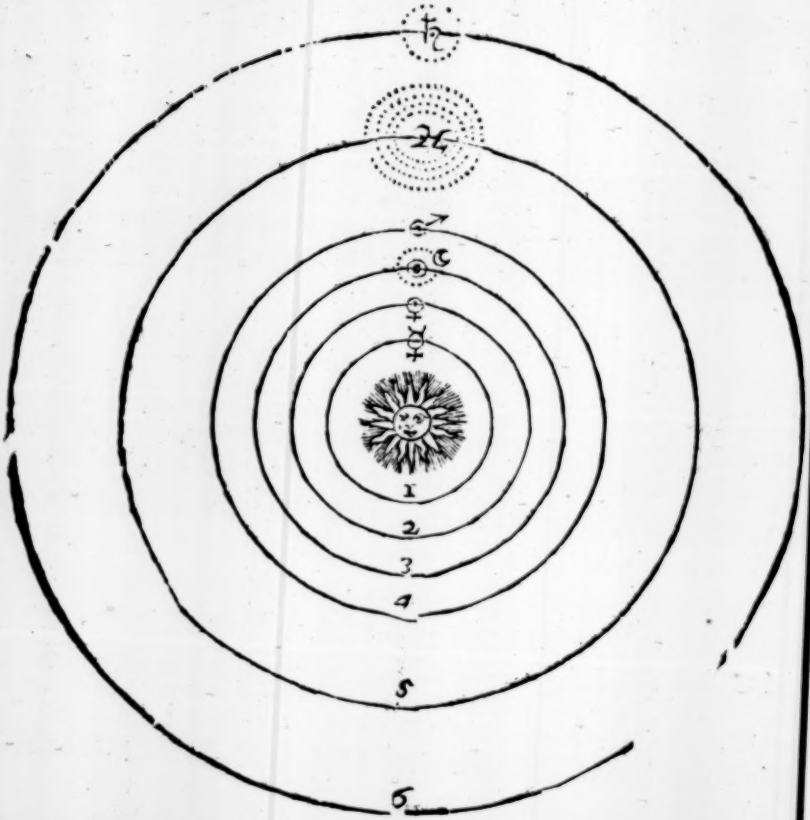
The Tychonean Systeme.



This *Hypotheſis* derives its Name from the Author thereof, *Tycho Brahe*, a Noble Man of *Denmark*, the moſt famous *Aſtronomical* Obſervator in the World in his dayes; who by his own Obſervations did rectifie the places of moſt of the *Fixed Stars* which appeared in that *Horizon* wherein he lived. This famous man, according to his preſent apprehenſion, framed this *Hypotheſis* of the Heavenly Motions, wherein he ſuppoſeth That *Venus*, *Mercury*, and all the other *Planets* (except the *Moon*) in their Motion, reſpect the *Sun* as their Center; and that *Saturn*, in Oppoſition to the *Sun*, is nearer to the Earth than *Venus*,

Venus in *Apogeon*; and that *Mars* in Oppoſition is nearer the Earth than the *Sun* it ſelf: as may appear in the ſaid *Hypotheſis*.

The Copernican Syſteme.



This *Hypotheſis* was firſt invented and framed by *Copernicus*, a famous *Aſtronomer* of *Germany*, who lived in the Year 1500, who ſuppoſed,

1. That

1. That the Sun is placed in the middeſt of the World, in or about the Center of the Sphere of the fixed Stars, and hath no Circular motion, but Central only.

2. The primary Planets are each of them in their proper Syſtems moved about the Sun, and accompliſh their Periodical Revolutions moſt exactly in their determinate and appointed times.

3. That the Earth is one of the Planets, and with her annual motion about the *Sun* deſcribeth her Orb in the middle between the Orbs of *Mars* and *Venus*.

4. That the ſecondary Planets are ordinarily moved about the primary Planets, reſpecting their Bodies for their common Nodes or Centers.

5. That the ſecondary Planet, the *Moon*, is moved about the Earth as her Center; where, by reaſon of the annual motion of the Earth, ſhe hath not only relation to the Earth, but by conſequence to the *Sun*, as have the other Planets.

6. That as this Primary Planet, the Earth, is environed with the Sphere of the *Moon*, ſo are ſome (if not all) the other Primary Planets, who have in like manner their Moons or Concomitants encompaſſing them.

The Motion of the Planetary Syſtem.

Firſt, The *Sun* hath only a Rotation from *Weſt* to *Eaſt*, upon his own Axis, in the ſpace of twenty ſix dayes, or thereabouts.

Secondly, The Planet *Mercury* performs his Revolution about the *Sun* in eighty eight dayes; which is noted in the Scheme with the figure 1 ☿.

Thirdly, The Revolution of *Venus* in 225 dayes; noted by the figure 2 ♀.

Fourthly, The Revolution of the *Earth* with the *Moon*, in one year; noted by the Circle 3.

Fifthly, The Revolution of *Mars* in two years, noted by 4 ♂.

Sixthly, The Revolution of *Jupiter*, with his four Companions, in 12 years, noted with 5 ♃.

Seventhly, The Revolution of *Saturn*, with his Ring and Moon, in 30 years; noted by 6 ♄.

The *Moon* circumvolveth the Earth every moneth; *Jupiter*'s four Attendants him, in time correſponding their diſtances from him,

The *first*, and next him in one day 18 hours.
The ſecond next without that, in 3 dayes 13 hours.
The third in 7 dayes 4 hours.
And the fourth and outmoſt in 16 dayes 8 hours.

Saturns Moon moves about him in 16 dayes, and all from *Weſt* to *Eaſt*, according to their Revolutions about the *Sun*.

Saturn, *Jupiter*, *Mars*, the *Earth*, *Venus* and *Mercury* (whoſe Revolutions reſpect the *Sun* only) are called *Primary Planets*.

The reſt (that move again) about *Saturn*, *Jupiter* and the *Earth*, *Secondary*.

The *Earth* hath a Revolution upon her *Equinoctial Poles*, in 24 hours, from *Weſt to Eaſt*.

The *Secondary Planets* are all of them much leſs in Magnitude than their *Primary*, and all the *Planets* together, much leſs than the *Sun*, from whom they all receive their Light, Virtue, and Principal Power of Motion.

Far without the *Planetary Syſtem* are placed all the *Fixed Stars*, in ſeveral Diſtances, but all unto us incommenſurable. The *Paralax* of the *Earths Orb* being inſenſible in any of their Places.

The *Golden Number* or *Prime*, is a Circular revolution of 19 Years, in which tearm of years it hath been antiently ſuppoſed, that the *Sun* and *Moon* do make all the varirty of *Aſpects* one to another.

The *Cycle of the Sun* maketh its Revolution in 28 years, becauſe in that time all the variety of the *Dominical Letters* and *Leap-years* are expired, and the 29th year the *Cycle* doth begin again; which number is to find out the *Dominical Letter* for any year paſt, preſent, or to come.

The *Roman Indiction* conſiſteth of 15 years, and is ſet down in the Charters and Writings of the *Protonotaries* of the Pope of *Rome*; for once in 15 years the Nations were to pay Tribute to the *Romans*.

The *Epact* is a Number never exceeding 30 dayes; it is the 11 dayes and ſix hours, which added to the *Lunar* Year, being 354 dayes, do make it equal to the *Solar* Year, which is 365 dayes.

The *Leap-Year* is every fourth Year, which hath one day more in it than another, this day is made up in four years, by the odd ſix hours that is over and above 365 dayes, which day is added at the end of *February*; So that *February* every *Leap-Year* hath twenty nine dayes, and in it are two *Dominical Letters*; the firſt ſerving from the firſt of *January*, until the 25 of *February*; and then the other Letter takes place and ſerves to the Years end. And here note that the *Prime* and

and *Dominical Letter*, and the *Cycle of the Sun*, changeth the firſt of *January*, and the *Epact* the firſt day of *March*; the *Number of Direction* the 22 of *March*, and the *Roman Indiction* the firſt of *September*.

Memorial Verſes on the Eccleſiaſtical and Civil Kalender, &c. By Mr. T.S.

To know if it be Leap-Year.

Divide the Year by 4; *What's left ſhall be*
For Leap-Year 0, *for paſt* 1, 2, *or* 3.

HERE you may omit the Hundreds and alſo the Twenties of the Year of the Lord; and only divide the reſidue by 4.

For Example.

Anno 1667, omitting the Hundreds and alſo the 3 Scores, I divide the Reſidue, which is 7, by 4; and there remaineth 3, which ſhews it is the Third after Leap-Year.

To find the Dominical Letter.

Divide the Year, its 4th, and 4, *by* 7;
What's left ſubſtract from 7; *the Litter's given.*
A 1. B 2. C 3. D 4. E 5. F 6. G 7.

Example.

Of the Year of Chriſt	1667
The 4th part (omitting fraction) is	416
To both which I add the number	4
The Sum is.	2087

Which divided by 7, there is left 1, which ſubſtracted from 7, the laſt remainder

remainder 6, ſhews that the Dominical Letter for the Year, 1667 is the ſixth in order of the Alphabet, that is F.

But the Leap-year hath two Dominical Letters; The latter found by this Rule, ſerveth from St. *Matthias* Day to the Years End; and for finding *Eaſter*: The former (next following in order from A to G, and beginning again at A) ſerveth from the *New-Year* unto St. *Matthias*.

For the Golden Number, Cycle of the Sun, and Indiction.

When 1, 9, 3, *to th'Year hath added been,*
Divide by 19, 28, 15.

Example.

To 1667, I Add 1; the ſum 1668 I divide by 19, and there remaineth 15, which is the *Golden Number* for the Year 1667.

Again, to 1667, I add 9, and the ſum 1676 I divide by 28, the reſidue 24 is the *Cycle of the Sun*, Anno 1667.

Laſtly, To 1667, I add 3, the ſum 1670 divided by 15, the remainder 5 is the *Indiction* for 1667.

The Prime or Golden Number being given; To find the Epact.

Divide by 3; *for each one left add* 10;
30 *reject*: *the Prime makes Epact then.*

Example.

Anno 1667, The *Golden Number* 15 I divide by 3, and there is left 0; therefore ten times 0, which is 0, added to 15, the ſum is 15, the *Epact Anno* 1667.

By

By the nineteen Epacts, to find the Day of Easter Limit from the beginning of March inclusively.

The Epacts take from 47, but two
The greatest take from 77: 'twill do.

Example.

Anno 1667. The Epact being 15, I substract it from 47, and the residue 32 is *Easter-Limit*, Anno 1667, that is *April* 1, reckoned from the beginning of *March* inclusively.

But when the Epact is 28 or 29, it must be substracted from 77, that so the Limit may remain. And the next following Sunday after the Limit is alwayes Easter-Day.

Easter-Limit, and the Dominical Letter being given; To find Easter-Day.

The Letter more by 4 from Limit take;
What's left from neareſt Sevens, ſhall Eaſter make.

Or thus,

Take the number of the given Letter more by 4 from the given Limit, and the residue from the neareſt greater sum of Sevens; the last remainer added to the Limit; the Sum, or its excess above 31, is Easter-Day in *March* or *April*.

Example.

Anno 1667. The Letter 6 more by 4, is 10, which taken from the Limit 32, the Residue is 22; this taken from the neareſt greater Sum of Sevens, 28, there remaineth 6; which added to the Limit 32, the Sum is 38, the excess of which above 31, is 7. Therefore the 7th of *April*, *Anno* 1667, is Easter-Day.

For

For the Dayes of the Months on which the Sun entereth the twelve Signs.

Twice 9, *twice* 10, 4 *Twelves*, 11
Then 10, *then* 9, *then* 8 *or* 7.

Anno 1700. ☉ in

♈.	♉.	♊.	♋.	♌.	♍.	♎.	♏.	♐.	♑.	♒.	♓.
Mar.	Apr.	May.	Jun.	Jul.	Aug.	Sep.	Oct.	Nov.	Dec.	Jan.	Feb.
9.	9.	10.	10.	12.	12.	12.	12.	11.	10.	9.	8.

For the Degree of the Suns Place on any Day.

From the Day of the Month on which the Suns Place is required, if you may, or else from the sum of that and 30, substract the day of his enterance into the Sign of that Month; the Remainer shall be the Degree of his Place in that or the next preceding Sign.

For the Age of the Moon, or day of Change.

Janus 0, 2, 1, 2, 3, 4, 5, 6,
8, 8, 10, 10, *these to the Epact fix:*
The Sum (*bate* 30) *to the Month-Day add*;
Or take from 30: *Age*; *or Change is had.*

Or thus, Add to the Epact, in

Jan.	Feb.	Mar.	Apr.	May.	Jun.	Jul.	Aug.	Sept.	Oct.	Nov.	Dec.
0.	2.	1.	2.	3.	4.	5.	6.	8.	8.	10.	10.

The Sum, if it be less than 30; or else the Excess above 30; added to the Day of the given Month (rejecting 30 if need be) gives the Age of of the Moon that Day; but Substracted from 30, leaves the Day of the Change in or from the beginning of that Month.

For the Day of the Full Moon; Add or Substract 15, to or from the day of the Change.

Example

Example.

1. For the Age of the *Moon*, *Anno* 1667, *May* 29, the number for the Month 3, added to the *Epact* 15, makes 18; which added to 29 (rejecting 30 from the ſum) gives 17, the *Age* of the *Moon* required.

2. For the day of the *Change* (or *New-Moon*) in *May* 1667, the *Epact* 15, with the Month 3, makes 18, (as afore) which ſubſtracted from 30, the Reſidue 12 is the day of the *New-Moon* in *May*, 1667.

3. The ſum of 12 and 15, is 27, the day of the *Full-Moon* in *May* 1667

To find the Day of the New-Moon, and the Enterance of the Sun into the Signs, for Time Paſt or to Come.

312, 131, ——————

Paſt Add, to Come Subſtract; for Moon and Sun.

Or thus.

For every 312 years Paſt, add 1 day to the time of the *New-Moon* found as above: For 312 years to Come, Subſtract 1 day.

Likewiſe, for 131 years paſt, a day is to be Added to the former account of the Suns Entrance; And for 131 years to Come, Subſtracted.

To find the Diſtance of the Sun from the Nodes of the Moon perpetually in all Lunations; Remember,

Year 17 *hundred*, *Node*, *Sine* 4, *Degree* 27, 3, 800, 43.

1. Take the Interval between the given time and 1700 Compleat, in years and dayes; allowing 12 Months to the Year, and 30 dayes to a Moneth: and the account will ſuffice for this work.

2. Multiply the years of the Interval by 43, and divide the Product by 800: the Reſidue multiply by 9; then take the half of this Product

and

and distinguish the last figure from the rest by a Point: So have you the degrees and 10th parts of a degree, answerable to the years of Interval. Also multiply the dayes of the Interval by 43, and divide by 800; this Quotient shews the degrees, and the remainer divided by 80, the 10th parts of a degree, of the Motion for the dayes of the Interval. Then Collect the former and latter degrees and 10ths into one sum, and reduce it into Signs, Degrees and Tenths.

3. For time afore 1700 Compleat, Add the Signs, Degrees and Tenths thus found to 4s, 27°, 3 10ths; but for time after 1700 Compleat, Substract them from 4s 27°, 3 10ths, and the Sum or Remainer shall be for the place of ☊; Adding one degree for the tenths if they exceed 5, else rejecting them.

Always in Additions, omit Cycles (to wit, 12s, or 360°.) But in Substractions, Add one Cycle if need be, to the Number from which you are to Substract.

Next, by the Common Rule for 1700, without any correction for time past or to come, find the Sign and Degree of the Suns place, and substract the last found place of ☊ from it: The residue is the Distance of ☉ from ☊ required.

The Limits of Eclipses of the Sun and Moon, in Degrees from ☊ or ☋.

Within 16 *the Sun, and* 10 *the Moon, Suffer Eclipse; Above* 18, 12, *none.*

To find the Length of the Dayes and Nights in the Lat. of 52°, for ever

To 15; 1; 1, 16; 2, 6; 3; 1; 2; 3; 4 *hours*; 4 *and half agree.*

To the given distances of the Sun from the next Æquinoctial Point, the answerable hours are these; to 15°, 1 hour; to 1 Sign, 2 hours; to 1s, 16°, 3 hours; to 2s, 6°, 4 hours; and to 3s, 4 hours and a half: which hours added to 12, the sum is from the Vernal Æquinox to the Autumnal

the

Autumnal, the just length of the Day, but from the Autumnal to the Vernal the length of the Night in those Distances.

And for all other intermediate distances of ☉ from the Æquinoctial Points; the Proportion is; As 15, 16 or 20°, to 60′; or as 20 to 30′; So are the degrees of the excess of the intermediate distances above 0°, 15° 1°, 16°, or 2°, 6°, and not exceeding 2° 26°, to the minutes of the Length of the Day or Night above 12, 13, 14, 15, or 16 hours: Always allowing 4 Degrees or Dayes afore and after the Ingress into ♋ and ♑ for Solstice.

The Length of the Day and Night taken together is 24 hours, from which if the one be substracted, there will remain the other; And,

Half the Length of the { Night, / Day, } is the time of { Sun Rising. / Sun Setting.

To find the Hour of the Moons coming to South; and High-Water at London.

The Moons Age Multiply by 4; *Divide*
By 5 *for Southing*: *Add* 3 *for the Tyde.*

But when the Age of ☽ exceeds 15 dayes, you may reject 15; As in this *Example.*

Anno 1667 *May* 29th, the Age of ☽ being 17 dayes, I reject 15, and the residue 2 multiplied by 4 makes 8, which divided by 5, the Quotient is 1 3/5, the hour of ☽ Southing; to which I add 3h, and the Sum is, 4 3/5, or 4h 36′, the time of Full-Sea at *London.*

But it is here to be noted, that by manifest experience it is found, that when the Moon is in either of the Quarters, that then the Tides do not hold out their full time, but is High-Water sooner than is found by the Rule; which may partly be occasioned by the weakness of the Tyde, at such a time, and the length of the River: for by the foregoing Rule you may find, That when the Moon is 7 Dayes old, the time of High-Water will be at 9 of the Clock, when upon true Observation it will be found to be an hour sooner; and therefore to know the true time of High-Water, you must substract some minutes from the time found by the precedent Rule, according to the Age of the Moon, as you may plainly see in the annexed Table.

The Moons Age.					H	M
1	14	16	29		0	0
2	13	17	28		0	5
3	12	18	27	Subtract.	0	10
4	11	19	26		0	20
5	10	20	25		0	30
6	9	21	24		0	45
7	8	22	23		1	00

Example.

The Moon being 7 dayes old, it is high Tyde (by the Rule) at *London* at 9 of the Clock; then in this Table look for the Figure 7, which is in the first Column, and right against it in the two last Columns, under the Title of hour and minute, you will find one hour, which must be substracted from the hour found by the Rule, and the Remainer is 8, the true time of High Water.

A Table shewing the time of the Moons coming to South any Day of her Age.

Moons Age.		Moons South.	
0	0	0	0
1	16	0	48
2	17	1	36
3	18	2	24
4	19	3	12
5	20	4	00
6	21	4	48
7	22	5	36
8	23	6	24
9	24	7	12
10	25	8	00
11	26	8	48
12	27	9	36
13	28	10	24
14	29	11	12
15	30	12	00

The Use of the Table, to find the time of the Moons coming to South. The first and second Column shew the Days of the Moons Age; in the third and fourth the hour and minute of the Moons coming to South.

Example.

The Moon being 10 dayes old, I would know at what time the Moon will be South; I find 10 under the Title of the Moons Age in the first Column, and right against it in the third and fourth Columns, you have 8 hours 00′, which sheweth that the Moon being 10 dayes old, cometh to South at 8 a Clock and no minutes, unto which if you add the time of flowing at Full & Change, the sum will be the time of Full Sea at the same place. As here at *London*, the time of flowing at Full and Change is at 3 of the Clock, which you are to add to the Moons Southing, and the sum is 11, which is the time of High-Water when the Moon is 10 dayes old.

To find the Hour of the Night by the Shadow of the Moon upon a Sun-Dial.

First find her coming to South (as before) then see how many hours and minutes the shadow wants of the hour of 12; which hours and minutes take from the hour and minute of the Moons coming to South, and the remainer is the hour of the Night; but if the shadow be past the hour of 12, then you must add so many hours and minutes as the shadow is past 12 to the hour and minute of the Moons coming to South, and that will be the hour of the Night.

Example.

On the 26 of *November* 1669 I find the Moon to be 13 dayes old, and therefore she comes to South at 10 a Clock and 24 min. past; and suppose the same night you look upon a Sun-Dial, and should find the shadow to be half an hour past 9, which wants 2 hours and a half of the 12 a Clock Line; which 2 hours and half being taken from 10 hours 24 minutes, the time of Moons Southing, the remainder will be 7 of the Clock and fifty four minutes, which is the time of the Night desired.

Again, suppose the same night the shadow of the Moon on the Dial had fallen on the hour of 1, that is one hour past the Line of 12, and therefore an hour must be added to the Moons coming to South, and that is the hour of the Night, which is 11 of the Clock and 24 minuts.

CHAP. VIII.

Of the *MARINERS COMPAS.*

Of the Variation of the Compaſs, and the probable Cauſes thereof; Some Obſervations to find the Variation; the Deſcription and Uſe of the *Azimuth-Compaſs*; of the *Univerſal Ring-Dial*; of the *Variation-Compaſs.*

SECT. I.

Of the Original Diſcovery and Invention of the Mariners Compaſs, and the Excellency thereof.

THIS marvellous and moſt uſeful Inſtrument, called the *Mariners Compaſs*, is juſtly ranked amongſt the greateſt Wonders that this World affords, and deſerves well to be underſtood by all that are Students and Practitioners in the Art of Navigation; for without the help thereof, it were impoſſible to trace out the unbeaten Paths of the Ocean, for the procuring Trade and Traffique beyond the Seas to remote parts of the World; and by the means thereof the Glorious Goſpel hath been tranſmitted into the moſt dark corners of the Earth.

As to the Original Inventer hereof, Modern Hiſtorians do ſomewhat vary; ſome attribute the Invention thereof to one *John Goia* (or *Flavia Goia*,

Goia, as others ſtile him) of *Amalphi* in *Campania*, in the Kingdom of *Naples*, who only accomodated the Superficies thereof with eight Points, that is, four Cardinal, and four Colateral; and ſo left the Improvement of this Invention, to be attempted by Poſterity. But *Polidore Virgil*, an *Italian*, who ſearched moſt diligently for ſuch Inventions, could never hear of this Opinion, as he confeſſeth in the latter end of his third Book, *De Inventoribus Rerum*. But ſome do ſeem to aſſert, that the finding thereof is more Modern, and hardly to be proved that it hath been in uſe in theſe parts of the World full 300 Years. Others do entitle the Invention thereof to the Poople of *China*. Doctor *Gilbert* in his Book *De Magnete*, aſſerts, That *Paulus Venetus* tranſported it firſt into *Italy*, in the Year 1260, having learned it from the *Chineſes*. And *Ludi Vertomanus* affirms, That when he was in the *Eaſt Indies*, about the year 1500 he ſaw the Pilot of a Ship direct his Courſe by a Compaſs, faſhioned and framed as thoſe which now are commonly uſed.

And Mr. *Barlow*, in his Book entituled, *The Navigators Supply*, Anno 1597, relateth a Story of two *Eaſt Indians* that he had perſonal conference with (one of them was of *Mamilia*, in the Iſle of *Luzon*, the other of *Miaco* of *Japan*) who declared, that in ſtead of our Compaſs, they uſe a Magnetical Needle of ſix inches and longer, upon a Pin in a Diſh of white *China*-Earth filled with Water, in the bottom whereof they have two croſs Lines, for the four principal Winds, the reſt of the Diviſions being left to the skill of their Pilots. Alſo he there relates, that the *Portugals* in their firſt diſcoveries of the *Eaſt-Indies*, got a Pilot of *Melinde* that brought them from thence in thirty three dayes, within the ſight of *Calecute*; and even then they had the uſe of the Compaſs, the Card, and the ſounding Line.

Philander in his Annotations upon *Vitruvius* ſheweth, That ſome men deem'd it not a New but an Old Invention, and took it to be a *Nautical* Inſtrument, which is called by *Plautus*, *in Trinummo & Mercatore*, by the Name of *Verſoria*. But this, *Adrian Turnebus* in no caſe will allow, affirming it rather to be a kind of Tackle, wherewith they turned their Sail, which is ſuppoſed to be the Bow-Line, that is now commonly uſed in theſe dayes. But let the Invention be attributed to whom it will, 'tis manifeſtly known to have received its abſolute perfection in theſe parts of the World, but more particularly the compleating of this Invention is due to the People of *Antwerp* and *Bruges*; and alſo to our own Nation, by annexing to the Compaſs twenty four ſubordinate Winds or Points: and alſo on the Limb thereof 306 degrees, which are numbred from North and South,

South, towards the East and west, 10, 20, 30, &c. So that it appeareth that every Point containeth 11° 15′. Upon the North Point thereof is a *Flower-deluce*, to distinguish it from the rest of the Points.

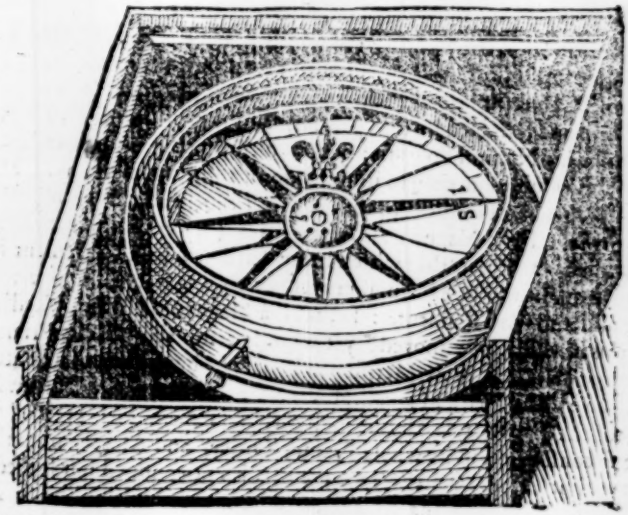
Before the Invention of this rare Instrument, men were directed in their Voyages by certain Stars they took notice of, especially the *Pleiades*, or seven Stars, by *Charles* his *Wain*, and the two Stars in the Tail of the little *Bear*, which were therefore called *Load-stars*. Also Travellers in the Desarts of *Arabia*, and those of *Tartaria*, were also guided by some fixed Stars in the night time, to steer their Courses in those pathless, disordered, and unhospitable wayes. So Seamen were directed by the like Heavenly Guides, in the untractable Wilderness of Waters and un-beaten Pathes of the Ocean, before this excellent Artifice was discovered: But if the Sky happened to be sullied with Mists, and the Stars to be muffled with Clouds, then the most Experienced Mariner was at a loss, and was constrained to come to an Anchor, or to lie by, to wait the appearance of his Cœlestial Directors; and if you consult *Pliny*, he will tell you also of the Inhabitants of *Taprobana*, now called *Sumatra*, because they could not behold the *Pole-Star* to Sail by, carried certain Birds to Sea, which they did often let fly. And as those Birds by natural instinct applyed their flight alwayes to Land; So the Mariners directed their Course after them, &c.

To these and the like Difficulties were men exposed before the Invention of this marvellous Instrument. But by this unparallel'd Gem Posterity is secured with a noble Remedy, against this grand Inconvenience; and a method discovered, as by an immediate Messenger from Heaven to steer an infallible Course in the most gloomy nights, and tumultuous Seas and by the Providence of the Almighty be safely conducted to the desired Port.

Yet this worthy Instrument is not so absolutely perfect by that acquired virtue it receives from the *Load-Stone*, but that it requires some improvements, because it doth not conform it self to the true Meridian in all places; but varies and distorts it self in some places more, in some less, from the direct position of the true North and South, which multiplies and enforces the Seamans distractions, and enwraps him oftentimes in difficult and dangerous Errors. A Discourse of the Variation, and of the probable Conjectures of the Natural Cause thereof, is fully handled in that which follows. I thought it necessary (for method sake) to subjoyn the Figure of the *Mariners Compass*.

The

The Figure of the Mariners COMPASS.



SECT. II.

A Diſcourſe of the Variation of the Compaſs, and of the Natural Cauſe thereof; with Obſervations of the Variation.

THE *Variation* of the *Compaſs*, is an Angle intercepted between the Magnetical and the true Meridian, the Horizon determining its Quantity and Quality. Theſe Meridians ſometimes are co-incident, and in ſuch places there can be no *Variation*; ſometimes again they are different

different: and then the Hemiſphere wherein the Northern extreamity of the Needle lyes, denominates its Quality; for if it be to the Eaſtward, then it is called Eaſterly Variation, if to the weſtward, then Weſterly.

And for the Reaſons of the Natural Cauſe of the Variation, I hope, firſt of all that it will be granted (by the Judicious) that the great Globe of the Earth whereon we move, is a Magnetical Body; and daily experience doth manifeſtly prove, if you take but notice of the Univerſal conformity of the Compaſs, to near one and the ſame Poſition to the North and South Poles of the World, the which is thereunto commanded by the Magnetical and Diſponent Faculty of the great Magnet, the Earth, by whoſe Magnetick vigor, paſſing from her Meridional parts to the Poles, ſhe is held and ſuſtained in that poſture, and not to be removed by any force from her Natural Poſition: yet if ſuch a thing were poſſible, certainly ſhe would return again unto her former ſeat and place, as all Magnetical Bodies and Needles do, that receive *Virtue* and *Strength* from the *Load-Stone*. For a Magnetical Body is ſtil'd, (not only that which hath a power attractive, but that which being ſcituated in a convenient Medium by an Intrinſique Natural propenſity diſpoſeth it ſelf to one invariable and and fixed Reſidence: ſo that if a Magnetical Body, Needle or Compaſs be violently removed, yet would it not abandon its Primitive Points, or ſwerve from its Meridional Polarity, but return to its natural ſcituation: And ſuch a Magnetical Virtue is diffuſed through the whole Body of the Earth, whereby it conſtantly addreſſeth it ſelf to the Poles, being ſo conſtituted in its whole Frame, Order, and Aſpect, unto theſe Points; that the Attractive Vigor thereof, is not confined nor locked up within its inward Cels and Receſſes, or circumſcribed within the circumference of its own ſurface, but diſpla'd at intermediate diſtances, notwithſtanding the interpoſition of the Water, Air and other interjacent Bodies whatſoever, though never ſo ſolid, through all which it doth excite, and tranſplant its Magnetical Virtue, into all Bodies fitly qualified within and without it; and effecting this in an abſtruce and indiſcernable way, the which we may ſee viſibly performed by the *Load-Stone*: For theſe Effluviums penetrate all Bodies, and attaque all Objects capable of their vigorous and active excitation; as is apparently manifeſt in all Magnetical Needles and Compaſſes, having received ſtrength from the *Load-Stone*; (but more eſpecially in the Inclinatory Needle) that the direction and ſcituation they do then aſſume, is not abſolutely from its own Natural propenſity to that poſition, originally reſulting from themſelves; but is derivative, and contracted from the powerful command of the Magnetick

netick Efflux of the earth, and by their mutual entwining and complication, carry away the Needle as their Captive, and place it according to her natural position. But several learned men, and great Philosophers, are at a great contest about this matter; for *Grandamicus*, a learned French man, in his Magnetical Tractate, *De Immobilitate Terræ*, doth affirm, That the Virtue of the Magnet, and all Magnetical Bodies, is purely immaterial, and a bare simple quality, and that it proceeds intrinsecally from the proper form of the Load-stone, as he hath delivered in the third Chapter of the said Book, Page 48. The which assertion, is much questioned by that learned and experimental Philosopher, Dr. *Power*, in his Book of experimental Philosophy, from *page* 157 to *page* 161, where he doth affirm, That the Magnetical Effluviums, do not proceed intrinsecally from the Stone, but are certain extrinsecal Particles, which approaching to the Stone, and finding congruous Pores and Inlets therein, are channel'd through it: And having acquired a motion thereby, do continue their current so far, till being repulsed by the Ambient Air, and they recoyl again, and return in a Vortical Motion, and so continue their revolution for ever, through the Body of the Magnet; which he doth there endeavour to prove by several Arguments.

And for the further Demonstration of this probable Truth, (that the cause of the Variation is clearly from the Magnatism of the Earth) I shall present a notable Experiment that may be performed by the Magnet.

Take a Vigorous Magnet, and let it be converted into a Spherical Body, and having found its Poles, delineate the same with Meridians, the Equinoctial and Parallels; then take a small Magnetical Needle on a Pin, and if you apply this Needle to the Equinoctial of the said Stone, the Needle will lye parallel to the Axis thereof; and if you move it towards either Pole, the Needle will immediately encline towards the said Pole, according as you move it, until you come to the Pole, then will one part of the Needle point directly to the very Pole of the stone.

But if this Spherical Magnet shall have a part of it excavated, as admit about the 45th Parallel; then if you move the Needle about the Stone as before, so soon as it shall draw near to the Limb of this Excavation, 'twill in its course of moving, suddenly alter, and encline to one of the solid Sides, not at all respecting the aforesaid Poles: And this deflection is called, The *Variation of the Needle*; and the greater will this Variation be, the Nearer it approacheth to the Poles: for whereas

before the Excavation, each Side being a like potent, the Needle enclined according to his natural position, but meeting with this accident in Nature (that is to say) the Excavation, it will convert it self to the more solid Side, rejecting the imperfect and defective, and so much the more powerfully, by how much the defective part hath left of its Magnetical Vigorous Substance.

And as it is with this Little, so likewise with the greater Magnet, the Earth, whose solid Magnetical parts, are great Continents, the defective and Excavated, the deep and vast Channel of the Sea; and therefore the cause of Variation, may be the inequality of the Earth, variously disposed, and differently mixed with the Sea; and all the different Emission of its strength and Magnetical Vigor, from the more eminent and gibbous; and from the hollow and Excavated parts thereof; for the Needle naturally endeavours to conform unto the Meridian, but being detracted, is driven and distorted that way, where the greater and more powerful parts of the Earth are scituated.

To this may be added, That the Variation proceedeth not only from some eminent terrestrial Knobs or Excrescencies, which appear like so many Wens upon the face of the Earth, as also from many magnetical Veins of the Earth, collaterally respecting the Needle, but likewise from the different accumulation of the Earth, disposed unto the Poles, lying under the Sea and Waters; which affect the Needle with a greater or lesser variation, according to the Vigor or Impotency of the Subterraneous Lines, or the entire or broken Body of the Magnetical Fabrick under it; as it is observable from several Load-stones placed at the bottom of any Water; for a Needle upon the surface, will variously conform it self, according to the vigor or imbecility of the Loadstones under it.

The Globe of the Earth is known to be very uneven, and unequally mixed with many materials, differing from a Magnetical quality, having great and stony Mountains, large Vallies, deep Seas, long and high Continents and Promontories, with mighty scattered Rocks of Load-stones, of Iron Mines, and other Magnetical matters.

And whereas it is manifestly apparent, that there's a certain Mutation or alteration of the Variation; I shall forbear to mention any thing of the probable Conjectures of the natural Cause thereof, but leave it to the discussion of time, and shall here present you with most of the publick Observations that have been made (of the Variation of the Compass) near the City of *London*, for near these hundreds years last past.

Mr. Burrows *his Observation of the Variation, made at* Lime-house, October the 16th, 1580.

Before Noon.				After Noon.						
Suns Alt.		Mag. Azim.		Suns Alt.		Mag. Azim.		Variation.		
Gr.	min.	Gr.	min.	Gr.	min.	Gr.	min.	Gr. min.	sec.	
17	00	52	35	17	00	30	00	11 17	30	Mean
18	00	50	08	18	00	27	45	11 11	30	Variation
19	00	47	30	19	00	24	30	11 30	00	on 11°
20	00	45	00	20	00	22	15	11 22	30	17′ 30″
21	00	42	15	21	00	19	30	11 22	30	from the
22	00	38	00	22	00	15	30	11 15	00	North
23	00	34	40	23	00	12	00	11 20	00	East-
24	00	29	35	24	00	07	00	11 17	30	ward.
25	00	22	36	25	00	00	08	11 14	00	

Mr. Gunter's *Observations, made at* Lime-house, June 13. Anno 1622. *Afternoon.*

Sun's Alt.		Mag. Azim.		Sun's Azim.		Variation.		
Gr.	min.	Gr.	min.	Gr.	min.	Gr.	min.	
19	00	82	02	75	52	06	10	
18	05	80	50	74	44	06	06	
17	34	80	00	74	06	05	54	Variation. 06° 15′ Eastward.
17	00	79	15	73	20	05	55	
16	18	78	12	72	32	05	40	
16	00	77	50	72	10	05	40	
10	10	71	02	64	49	06	13	
09	52	70	12	64	25	05	47	

So that it is here Observed, that in the Interval of the Observations made by Mr. *Burrows* and Mr. *Gunter*, in 42 years, the evident Diminution hath been 5 degrees.

Mr. Gillibrand's *Observations, made at* Deptford, Anno 1634. June 12. before Noon.

Alt. Sol. Vera.		Azim. Mag.		Azim. Sol.		Variation.	
Gr.	min.	Gr.	min.	Gr.	min.	Gr.	min.
44	45	106	00	110	06	04	06
46	30	109	00	113	10	04	10
48	31	113	00	117	01	04	01
50	54	118	00	122	03	04	03

In

In the Afternoon the ſame day.

Alt. Sol. Vera.		Azim. Mag.		Azim. Sol.		Variation.	
Gr.	min.	Gr.	min.	Gr.	min.	Gr.	min.
44	37	114	00	109	35	04	07
40	48	108	00	103	50	04	10
38	46	105	00	100	48	04	12
36	43	102	00	097	56	04	04
34	32	099	00	095	00	04	00
32	10	096	00	091	55	04	05

The mean of which Obſervation is 04° 04′ Eaſtward.

Obſervations made by Mr. *Gillibrand* at *Pauls Cray* in *Kent*, *July* 4. 1634. Afternoon.

Vera Alt. Sol.		Azim. Mag.		Azim. Sol.		Variation.	
Gr.	min.	Gr.	mim.	Gr.	min.	Gr.	min.
40	55	111	30	107	30	04	00
40	01	110	00	106	05	03	55
39	41	109	30	105	34	03	56
38	42	108	00	104	05	03	55
35	32	103	30	99	32	03	58
34	49	102	30	98	32	03	58
33	41	101	00	97	00	04	00
32	57	100	00	96	02	03	58
32	09	99	00	94	58	04	02
31	25	98	00	94	00	04	00
30	39	97	00	93	01	03	59
29	29	95	30	91	31	03	59
27	51	93	30	89	28	04	02

The mean Variation is about 4° Eaſtward.

So that here alſo may be noted, that the ſenſible diminution of the Variation in 54 years (from the time of Mr *Burrows* Obſervations) is more than 7 degrees.

Observations made by *John Seller*, at the *Hermitage* near *London*, with a Quadrant of 6 foot Radius, for the Altitude : and an Instrument of two foot Radius for the *Azimuth*, taken in the year, 1666. Lat. 51 deg. 32 min.

June the 4th. 1666, *in the Forenoon.*

Suns Alt.		Suns Azim.		Mag. Azim		Variation.	
°	′	°	′	°	′	°	′
26	00	84	36	85	00	00	24
27	30	86	26	87	00	00	34

June the 13th. 1666. *in the Afternoon.*

08	24	62	31	62	00	00	31
08	09	61	51	61	30	00	21
07	38	61	29	60	45	00	44
07	07	60	47	60	00	00	47

June the 14th. 1666. *in the Forenoon.*

29	30	88	40	89	30	00	50
31	20	91	03	91	30	00	27

The mean of these Observations is 34 minutes Westerly.

May the 28*th.* 1670, in the Afternoon, taken by the Worshipful, Sr. *Nicholas Millet*, at his house at *Battersey*.

24	30	83	54	81	40	1	54
20	30	78	44	76	35	2	09
17	03	74	32	72	18	2	14
15	42	72	54	70	40	2	14
13	36	70	18	68	10	2	00
11	11	67	14	65	15	1	59
10	11	75	58	63	45	2	13

The mean Variation is 2′ 06″ Westerly.

Sect.

SECT. III.

The Description and Use of the Azimuth Compass.

THis Compass doth derive its Name from its Use, being principally to find the *Magnetical Azimuth* of the Sun, and is in several respects like unto another Compass, only with such necessary things added as are most convenient for that purpose.

Upon the round Box wherein are the Fly and Needle, is fastened a broad circle of Brass, the one half of the Limb thereof is divided into 90 degrees, numbred from the middle of the said divisions both wayes, with 10, 20, 30, *&c.* unto 45 degrees: Which degrees are also subdivided into minutes by *Diagonal* Lines, and by certain *Excentrick Circles* intersecting one another: but these Degrees are drawn from the opposite part of the Limb whereon the Index moveth and cutteth those degrees in time of Observation; and on this Index is erected a sight, which for conveniency is to fall down with an hinge, and to set up upon occasion; and from the top of this Sight, down to the middle of the Index, is fastened a thrid or lute string, to shew the shadow of the Sun upon a Line that is on the middle of the said Index.

And by this meanes of placing the Index upon the Circumference, the the Degrees come to be as large again as they would be if it mooved upon the Center; the Truth hereof is evidently demonstrated in the third Book of *Euclid. Prop.* 20. *Theor.* 18.

This broad Circle is crossed at right Angles with two strings, and commonly from the terminations of these strings, are drawn four small black lines on the inside of the Box, for the rectifying the Instrument in time of Observation, by the four Lines that are also drawn at right Angles on the Superficies of the Fly.

This Compass being thus fitted, is hung in strong brass Rings, and those also fastened into a square Wainscot Box fit for that purpose; which you may more plainly perceive in this following Figure.

The figure of the Azimuth Com=pas

The Uſe of the Azimuth Compaſs in time of Obſervation.

Firſt, You muſt rectifie the braſs Limb on the edge of the Box (by the Needle and Fly within the Box) according as the nature of the Obſervation doth require; For if the Obſervation be in the Forenoon, then you muſt put the Center of the Index upon the Weſt point of the Card or Fly within the Box; and ſo that the four lines on the edge of the Card, and the four lines by the inſide of the Box, do alwayes concur.

The Inſtrument being thus rectified, turn the Index towards the Sun, until the ſhadow of the *Hypothenuſal* thread do fall directly into the very ſlit of the ſight that is on the Index, and alſo upon a ſtrait Line that is in the

the middle of the Index; then at the ſame time will the inner edge of the Index cut the degree and minutes of the Suns Magnetical Azimuth, from the North or South part of the Meridian, being judiciouſly conſidered.

As for Example.

Suppoſe the Inſtrument be rectified as before is ſhewed, for an Obſervation in the forenoon, and that the Index ſhould cut at ten degrees upon the Limb to the Northward of the Eaſt, then is the Azimuth of the Sun 80 degrees from the North part of the Meridian, or elſe 100 degrees from the South part thereof. So likewiſe if the Index had cut 10 degrees to the Southwards of the Eaſt, then would the Azimuth be 80 degrees from the South, and 100 from the North part of the Meridian.

And here alſo Obſerve, That the Compaſs ſtanding in this poſition, and if the Azimuth of the Sun be leſs than 45 deg. from the South part of the Meridian, and you turn the Index toward the Sun, it will then go off the diviſions on the Limb, and there can be no uſe made thereof as it now ſtands.

Therefore you muſt turn the Inſtrument juſt one Quadrant, or quarter of the Compaſs, (*viz.*) place the Center of the Index on the North or South point of the Card, according to the Suns poſition from you, and then the edge thereof will cut the degree of the Suns Azimuth, from the North or South part of the Inſtrument, as before. That which is ſaid as to the uſe of the Azimuth Compaſs, when the Sun is on the Eaſt ſide, the like is to be underſtood with the ſame reaſon, when he is on the Weſt ſide of the Meridian.

And alſo note, That the Obſervations of the Suns Azimuth are beſt when the Sun is not very high above the Horizon, not exceeding 15 or 20 degrees; which Obſervations, when they are ſo taken, are the moſt true, becauſe the motion of the Sun, both to his Altitude, as well as to his Azimuth, is more eaſily diſcovered.

To take an Amplitude by the Azimuth Compaſs.

If the Amplitude be taken in the morning at the riſing of the Sun, then you muſt turn the Center of the Index right over the Weſt point of the Fly, and rectifie the Inſtrument by the Lines within the Box, to the Lines on the Fly.

Then looking through the ſight, turn the Index towards the Sun, un-

till you cut the Body of the Sun with the thread; at the ſame time will the edge of the Index ſhew the degree of the Suns Magnetical Amplitude, upon the Limb of the Inſtrument, from the Eaſt, either Northerly, or Southerly.

But if you take the Amplitude in the afternoon, at the ſetting of the Sun, then you muſt turn the Index over the Eaſt point of the Fly, and proceed as before.

Having found the Magnetical Azimuth or Amplitude by the Compaſs, find the Suns Azimuth by *Problem* 12. *Chap.* 7. and the Suns Amplitude by *Problem* 8. *Chap.* 7.

Then find the difference between the Suns Azimuth or Amplitude and the Magnetical Azimuth or Amplitude, by Subſtracting one from the other. This Difference is the Variation of the Compaſs. And to know whether the Variation be Eaſterly or Weſterly, obſerve the following Rules.

Rules for caſting the Variation.

1. By the Obſervation of the Azimuth;

In the Forenoon.

1. If the Angle of the Suns Azimuth (by Calculation) from the North part of the Meridian, be greater than the Magnetical Azimuth, (by Obſervation) then is the Variation Eaſterly.

2. If the Angle of the Suns Azimuth, from the North part of the Meridian, be leſs than the Magnetical, then is the Variation Weſterly.

In the Afternoon.

3. If the Suns Azimuth, from the North part of the Meridian, be greater than the Magnetical, then is the Variation Weſterly.

4. If the Suns Azimuth, from the North part of the Meridian, be leſs than the Magnetical, then is the Variation Eaſterly.

Example 1.

Suppoſe on the fourth of *June* 1669, in the forenoon, (the Suns Declination being 23° 22′ North, in the North Lattitude of 51° 32′) I ſet the Sun with my Azimuth Compaſs, and find his Magnetical Azimuth to be 86° 04′ from the North, being 25° 58′ above the Horizon; at the ſame time the Suns true Azimuth by Calculation, is 84° 30′ from the North part of the Meridian.

The

The difference of these Azimuths (which is the Variation) is 01° 34′; I demand which way the Compass varies?

Answ. Westerly; because that Observation being made in the forenoon, and I find the Suns true Azimuth (from the North part of the Meridian) to be less than the Magnetical, according to the second Rule afore-going.

Example 2.

Admit that in the afternoon, at the same time that I find the Suns true Azimuth to be 102° 00′, I find his Magnetical to be 96° 00′ from the North.

The difference is 09° 00′, I demand which way the Compass varies?

Answ. Westerly; because the Observation being made in the Afternoon, I find the Suns Azimuth from the North, to be greater than the Magnetical, according to the third Rule.

Note, These four Rules for casting the Variation, by Observation of the Suns Azimuth, are as well practizable in South as in North Latitudes, the Suns Declination being either Northerly or Southerly.

2. By the Observation of the Amplitude.

At Sun-Rising.

1. If the Suns Amplitude be nearer to the North part of the Meridian than the Magnetical, then is the Variation Westerly.
2. If the Suns Amplitude be farther from the North part of the Meridian than the Magnetical, then is the Variation Easterly.

At Sun-Setting.

3. If the Suns Amplitude be nearer to the North part of the Meridian than the Magnetical, then is the Variation Easterly.
4. If the Suns Amplitude be farther from the North part of the Meridian than the Magnetical, then is the Variation Westerly.

Example.

Admit that by the Azimuth Compass, at Sun-setting, I find the Mag-

netical Amplitude to be 19 deg. 00 min. and the Suns true Amplitude to be 24 deg. 00 min. from the West Northerly; I demand which way the Compass Varies?

Answ. Easterly; because by an Observation at Sun-setting, the Suns Amplitude is nearer to the North, than the Magnetical according to the third Rule.

Having, by the former Rules, found the Quantity and Quality of the Variation, it yet remains there be some Directions for Rectifying the Course.

The manner that I shall here set down, is performed by a Compass-Card (having degrees on the Limb) and a pair of Compasses, which though it be mechanical, yet it's facile and demonstrative, and in my Opinion, exact enough for Nautical Uses, how ever any one may use the Pen if he please.

But before we deliver the Rule for Operation, it will not be amiss, for plainness sake, to give these Cautions.

1. That when a man directly beholds the North part of the Horizon, the East is on the right-hand, and the West on his left; and therefore when the North point of the Compass (and consequently all the other points) vary from the true North or Meridian to the Eastward, then the Variation is reckoned to the right-hand; and for the same reason, if the Variation be Westerly, its accounted to the left.

2. That in the Use of the Compass-Card, you must alwayes observe, that you place the Course or Point on which you steer right from you, supposing the eye to be in the Center of the Card, directly beholding the Course lying right before you.

The Rule.

Take the quantity of the Variation in degrees, from the Limb of the Chard, between the Compasses, (the Chard lying before you, as is directed) placing one foot in the Rumb or Course; if the Variation be Easterly, turn the other foot towards the Right-hand, but if it be Westerly, to the left; the number of degrees in which the point of the Compass stayes, shews the true Course from the North or South, either Easterly or Westerly, the Quantity and Quality of the Variation being allowed.

As for Example.

1. Let the Magnetical Rumb, or Point of the Compass, be North-East,

East, and the Variation 10 degrees Easterly, I demand the true Rumb?

The Card lying, as is directed, take the extent of 10 degrees, between the Compasses, and place it from the North-East towards the right hand, because the Variation is Easterly, that shews the true Course to the North-East 55 degrees.

2. Let the Course, by the Compass be West and by South (*i. e.*) S. W. 78 deg. 45 min. and the Variation 10 degrees Easterly, as before, I demand the true Rumb?

Take the extent of 10 degrees between your Compasses, and place it from W. and by S. towards the right hand, it shews the true Rumb to be S. W. 88 deg. 45 min.

3. Let the Magnetical Rumb be West, and the Variation 10 deg. Easterly, I demand the true Course?

Take the extent of 10 degrees, as before, set it off from the West towards the right hand, it gives the true Rumb North-West 80 degrees 00 minutes.

4. Let the Magnetical Rumb be N. N. W. the Variation 10 deg. Westerly, I demand the true Rumb?

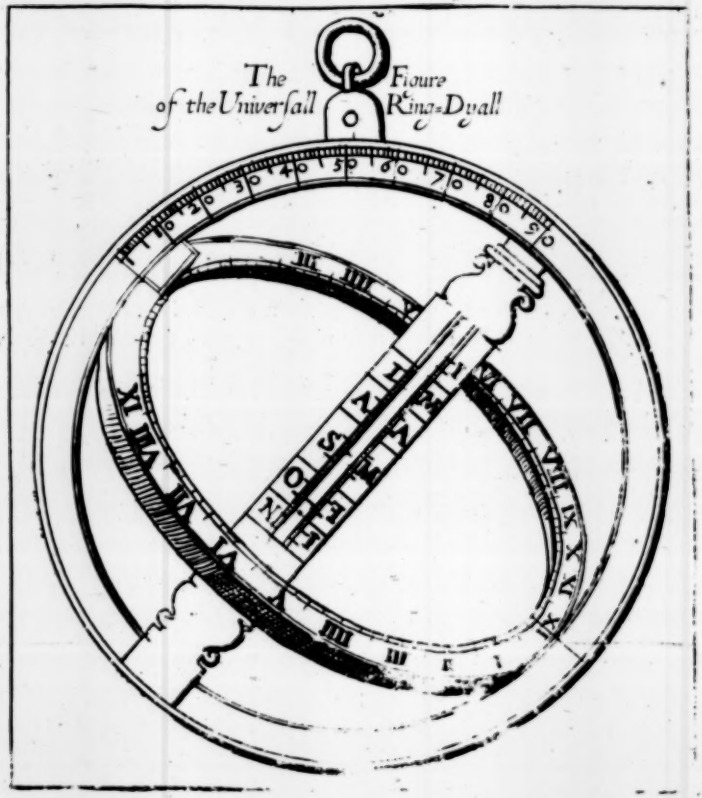
Take the extent of 10 deg. place it from the N. N. W. towards the left hand, because the Variation is westerly, it gives the true Rumb N. W. 32 deg. 30 min.

5. Let the Course, by the Compass, be West, the Variation 10 deg. Westerly, I demand the true Course?

Take the quantity of the Variation 10 degrees, place it from the West towards the left hand, which shews the true Rumb to S. W. 80 degrees.

SECT. IV.

The Description of the Universal Ring-Dial.



This

THis Inſtrument conſiſts chiefly of two Rings, cloſely fitting within each other, and a Bridge, and is made either of Braſs or Silver.

The outtermoſt Ring repreſents the Meridian of the Place, and on the foreſide, has one of its upper Quadrants divided into 90 Degrees; likewiſe on the back-ſide a Semi-circle is divided into the like number of degrees from the Hole or Center in the Circumference; on the Convexity of this Ring is fitted a Nut (with a Wyer Ring to it) having a ſmall Line drawn in the middle of it to remove to any of the degrees on the fore ſide.

The inner Ring, (when they are open at Right Angles) repreſents the Equinoctial Circle, on the inſide of which is drawn a Line in very midſt, and thereon are divided the hours into halves and quarters, and are numbred with their proper figures on the upper ſide of this Ring.

The Bridge repreſents the Axis of the World, in the middle whereof there is cut a long ſlit, on whoſe edges, upon one ſide, are placed the Dayes of the Month, on the other the degrees of the Suns Declination; upon the Bridge is contrived a ſliding Nut, which directs a ſmall Plate moving within the ſlit; this Plate is croſſed with a fine diviſion, and in the midſt thereof is drill'd a ſmall hole.

The Uſe of the Ring-Dial.

To find the Hour of the Day.

Place the hole that is in the ſmall plate in the Bridge, to the day of the month, or the Suns Declination, and ſet the Nut upon the Convexity of the outer Ring, to the degrees of the places Latitude (whether Northerly or Southerly) on the foreſide of the Ring; open the Rings to Right Angles, and then having your Inſtrument on your finger, turn the upper end of the Bridge towards the elevated Pole, and place the flat ſide of the Bridge againſt the Sun, that his Rays may the better tranſpierce the little hole; then turn the Inſtrument to the Sun, until the Sun-beams (by the little hole) fall exactly upon the Line drawn on the inſide of the Equinoctial or inner Ring, then is ſhewn the Hour of the Day exactly, according to the capacity of the Inſtrument.

The dividing the degrees of the Suns Declination on the Bridge of this Inſtrument (which I purpoſely omitted) is Geometrically deſcribed by the worthy Mr. *Edward Wright*, in his *Correction of Errors*, who, I think,

think was the firſt contriver of this Univerſal Dial, although differing from this here diſcourſed of.

To find the Suns Altitude.

To perform this, you muſt firſt ſet the Line in the midſt of the Nur, upon the outer Ring, to the beginning of the degrees on the foreſide of the ſame, then put a pin in the Center Hole, and hanging your Dial upon your finger, turn the edge of the outer Ring towards the Sun, ſo as the ſhadow of the Pin may fall upon the diviſions on the back-ſide; the degrees cut by the ſhadow is the Suns Altitude.

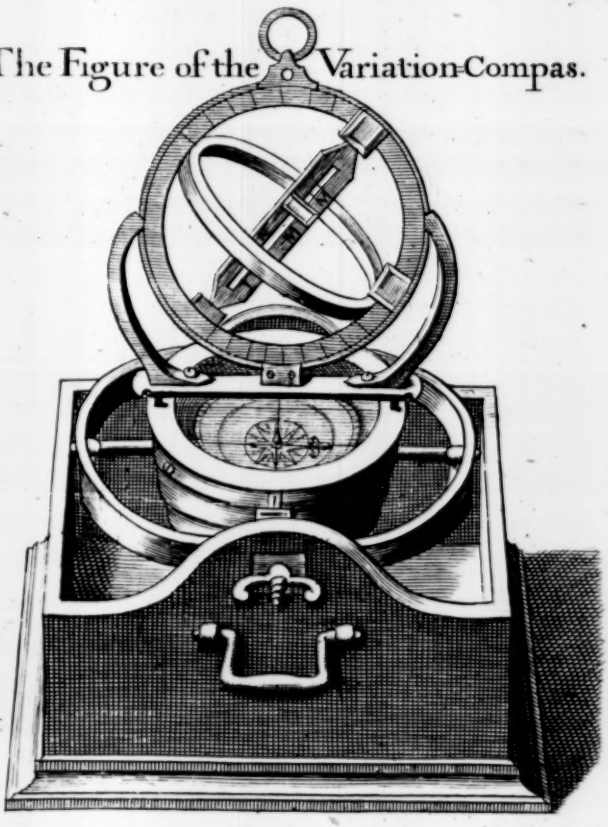
SECT. V.

Of the Variation Compaſs.

THis Inſtrument derives its name from its excellent uſe in *Navigation*, becauſe it finds the variation of the Compaſs at any time when the Sun ſhines, immediately by *inſpection only*, without the trouble of any *Calculation*.

This Compaſs hath a Card divided into 360 degrees, numbred from the North and South with 10, 20, 30, *&c.* On the inſide the Box is drawn four black Lines; over two of theſe Lines, on the outſide of the Box, is fitted a ſtrong Plate of Braſs with two Supporters, by which a *Univerſal Ring Dial* is faſtned to the Compaſs-Box; this *Ring Dial* is the ſame with the laſt deſcribed, only much larger, and with this difference, That whereas in that, the *upper Quadrant* was divided; in this, the *lower Quadrant* is ſo divided, to rectifie it to the Latitude of the place, by a Tooth proceeding from the Braſs Plate on which it ſtands.

The Figure of the Variation-Compas.



To find the Variation by the Variation-Compaſs.

Put the hole in the Bridge to the day of the Moneth, and opening the Rings at Right-Angles, bring the Latitude of the Place to the Tooth upon the Plate; then turn the Compaſs towards the Sun, until you find the hour of the Day, according to the Directions in the Uſe of the Ring-Dial. Then caſt your Eye upon the North Point of the Needle, and if it con-

cur with the black Line within the Box, there is no Variation; but if it ſwerve to the Eaſtward, the Variation is Eaſterly; if to the Weſtward, Weſterly; and the degrees on the Chard cut by the Black Line, ſhew the quantity of the Variation.

Example.

Suppoſe that my Compaſs being rectified to the Latitude of the Place, and fitted according to directions, I find the hour of the Day, and at the ſame time I perceive the North Point of the Needle to ſwerve from the Black Line 10 degrees towards the Eaſt; Therefore I conclude the Compaſs varies 10 degrees Eaſterly.

CHAP. IX.

Containing the Uſe of theſe Inſtruments.

The Croſs-Staffe, the Quadrant, the Croſs-bow Quadrant, the Plow, the Removing Quadrant; likewiſe how to find the Latitude of a Place by the Meridian, Altitude and Declination; and the Uſe of the Nocturnal and Moon-Dial.

The Figure of the Crosſ-Staff, and the the manner of Obſervation.

SECT. I.

The Deſcription and Uſe of the Crols-Staff.

This

This Inſtrument is of ſome Antiquity in Navigation, and is commonly uſed at Sea, to take the Altitude of the Sun or Stars, which it performs with ſufficient exactneſs, eſpecially if it be leſs than 60 degrees; but if it exceed 60, it is not ſo certain, by reaſon of the length of the Croſs, and the ſmallneſs of the graduations on the Staff.

The Staff is made ſtreight, four-ſquare, and commonly of Box or Pear-Tree, and graduated on the ſeveral Sides with degrees and minutes.

The Croſſes, uſually four, are commonly made of the ſame Wood with the Staff, of a convenient breadth, and of length proportional to the Graduations, fitted to ſlide evenly upon the Staff, without jogging.

On one ſide of the Staff, the Graduations begin about three degrees, and proceeding towards the Center, or eye-end, encreaſe by every ten minutes, to ten degrees, and this ſide is called the ten-ſide, and the Croſs thereto belonging (the ſhorteſt of the four) the ten-Croſs, whoſe half legnth (if rightly made, and the Staff truly divided) ſhall reach on this ſide from 10°, unto 9° 12′, and his whole length from 10°, to 8° 31′.

On another ſide of the Staff, the diviſions begin at about ten degrees, and increaſe upward to 30 degrees; this is called the thirty-ſide, and its Croſs the thirty-Croſs, whoſe half length ſhould reach on this ſide from thirty degrees to 23 deg. 52 min. and the whole length from 30 deg. to 19. deg. 47 min.

On another ſide the Graduations begin about 20 deg. and encreaſe toward the eye-end of the Staff to 60 deg. this is named the ſixty-ſide, and the Croſs peculiar to this Side, is called the ſixty-Croſs, whoſe half length ought to reach on this ſide from 60 deg. to 40 deg. 13 min. and the whole length from 60 deg. to 30 deg.

The remaining and fourth Side, hath the diviſions beginning at 30 deg. and increaſing upwards to 90 deg. from thence it is named the ninty-ſide, and his Croſs (the longeſt) the ninty-Croſs, whoſe half length muſt reach from 90 deg. to 53 deg. 07 min. or from the Center of the Staff, to 90 deg. and the whole length from 90 deg. to 36 deg. 52 min.

Sometimes the ſeveral Sides of the Staff are numbred likewiſe with their Complements to 90 deg. in ſmall figures, *viz.* at 90 deg. ſtand 00°, againſt 80° 10°, at 70° ſtands 20°, and ſo of the reſt.

The Uſe of this is to take the Complement of the Altitude, or Zenith diſtance from the Staff, without Subſtraction. There

There are two wayes principally for the graduating a Crofs-Staff, one by Geometrical Projection, the other by Arithmetical Calculation. I will give you an Example of the latter, by which you may divide any Staff, or at leaſt be able to examine one that is already graduated.

Example of the ſixty Croſs.

Suppoſe the length of the ſixty Croſs to be 10 $\frac{3}{10}$ inches, and the half length 5 $\frac{1}{10}$ inches, I deſire to know the diſtance of 45° 30′ from the Center of the Staff proportional to this length of the Croſs. Take $\frac{1}{2}$ of 45° 30′, that is 22° 45′.

The Proportion is,

	Co. Ar.
As the Tangent of 22° 45′ ——	10.37742
is to the $\frac{1}{2}$ length of the Croſs 5 $\frac{1}{10}$ inches ——	0.70757
ſo is Radius ——	
to the diſtance required 12. 16 inches ——	1.08499

This gives the diſtance from the Center of the Staff to the diviſion, repreſenting 45° 30′, to be 12. 16 (or $\frac{16}{100}$) inches.

But if you do purpoſe to Graduate a Staff, the more ready and expedite way, is to divide the half length of the Croſs into 100 or 1000 equal parts, and taking only the Tangent Complement of half the Angle required out of a Canon of natural Tangents, gives the diſtance required.

Example.

Suppoſe, as before, the $\frac{1}{2}$ length of the 60 Croſs, to 5, 1 inches, and its required to know the diſtance from the Center, to 45° 30′.

The half length of the Croſs being divided into 1000 equal parts, (or into as many as conveniency admits of, the reſt ſupputated by eſtimation) look into the Tables of natural Tangents, for the Tangent Complement of 22 degrees 45 minutes (the half of 45 degrees 30 minutes) and you will find 238472 ; then cutting off two figures towards the right hand, the remainder 2384, ſhews the number of equal parts (whereof the half Croſs contains 1000) which muſt be taken, to ſet off the diſtance from the Center to 45° 30′, that is twice the half length of the Croſs, and 384 parts more.

The

The like you may perform for any other degree, to every tenth or fifth minute, or leſs, according as the Staff will admit of the diviſions, and as you ſee in the example of this Croſs, ſo the like may be performed for any Croſs of what length ſoever.

The Uſe of the Croſs-Staff.

To take a forward Obſervation of the Suns Meridian Altitude at Sea.

When you do intend to take the *Meridian Altitude* at Sea, in reference to the obtaining of the places Latitude, it is convenient that you be preparing your ſelf for your *Obſervation*, ſome competent time before noon, and conſider what the Suns *greateſt Altitude* may be that day; accordingly to uſe thoſe *Croſſes* that may be moſt pertinent to your purpoſe.

As ſuppoſe the *Meridian Altitude* for that day be judged to be 20 degrees, then uſe the thirty ſide of the Staff, and the thirty Croſs; if you think 'twill be 30 degrees, then take the ſixty Croſs; but if it be eſtimated to exceed both, then the ninty Croſs is moſt proper for your uſe.

There is another Requiſite fit to be underſtood before you proceed to Obſervation, and that is, how to place your fore-ſtaff to youre eye, to prevent an error, mentioned by Mr. *Wright* in his *Correction of Errors*, to avoid which, take theſe few hints.

Firſt, Place the Center of the Staff at A, to the outſide of the Corner of your eye, as near your eye as conveniently you can, without hindering your ſight, letting the end reſt upon your eye bone, reſpecting, as it were, the eyes Center, and cauſe the viſual Rayes to concur with the middle parallels drawn on each ſide of the Croſs-Staff, and then is your Staff rightly placed for Obſervation: but becauſe this is ſomewhat difficult plainly to be deſcribed, and perhaps that which is already ſaid, may not be ſo obvious to the Reader as I could wiſh it, I will therefore give an eaſie Demonſtration, which may be verified by experience.

Having firſt of all ſatisfied your ſelf in the truth of the diviſions on the Staff, and likewiſe of the exact length, and half length of your Croſſes,

Croſſes, then put on the ſixty Croſs, and place it to 30 degrees, on his proper ſide, and alſo ſlip on the ninty Croſs parallel with the former, and put that to 30 degrees likewiſe on his peculiar graduations, then bring the end of the Staff to the Corner of your eye (as is directed) and remove it ſomewhat higher or lower, until you ſee each end of the two Croſſes at once exactly to concur and agree with the viſual Lines proceeding from your eye; that is the place of your Staff in time of Obſervation, and may eaſily be found by frequent trial.

Having thus prepared for your Obſervation, and acquainted your ſelf with the holding of your Inſtrument, being upon the Deck, turn your face towards the Sun, and place your Staff to your eye, holding the Croſs as upright as you can, look at the upper-end of your Croſs, as at C for the Sun, and at the lower at B for the Horizon; but if the Sea obſcure the Horizon from your ſight, then remove the Croſs a little farther from your eye; but if on the contrary your ſight do not extend ſo low as the Horizon, but the Skie only appears in ſtead thereof, then move the Croſs a little nearer your eye, until by the upper part thereof you ſee the Center of the Sun, and by the lower the Horizon exactly at the ſame time, then look upon the proper ſide of the Staff (for the Croſs you uſe) the Suns preſent Altitude will be cut by the ſame; and this, if it were for one ſingle Obſervation either of the Sun or any Star, were ſufficient.

But the Suns greateſt Altitude being that you are about to procure, you muſt therefore wait, making Obſervation as your judgement ſhall direct you, until the Sun be upon the Meridian, ſtill ſliding the Croſs nearer your eye as the Sun riſes, until you perceive him to be at the higheſt; for ſo ſoon as the Sun is to the Weſtward of the Meridian, and falling, if you make Obſervation again, you will find the Sea to obſcure the Horizon from your ſight, and then in no caſe remove your Croſs, but let it remain fixed, and finiſh your Obſervation for that ſeaſon.

Then caſt your eye upon that ſide of the Staff belonging to the Croſs you uſe, the degrees and minutes cut thereby, and numbred with larger figures (decreaſing alwayes from the Center of the Staff) gives the Suns Meridional Altitude, and the ſmall figures underneath, the Complement of the Altitude or the Zenith diſtance.

In obſerving forward by the Croſs-Staff, 'tis uſual to have a piece of red Glaſs to defend the ſight from the luſtre of the Sun in time of Obſervation.

['Twould,

['Twould, in my opinion, be better to have the Glaſs fitted in a piece of Braſs, and ſo to put upon the end of any of the Croſſes as occaſion requires. Thus much for a forward Obſervation.]

After the ſame manner you muſt obſerve the Altitude of the Stars.

To make a backward Obſervation of the Suns Altitude by the Croſs-Staff.

Theſe Obſervations are frequent at Sea, eſpecially with the *Hollander*; And to perform this, you muſt have a Horizon Vane to fix upon the Center of your Staff, or elſe a ſliding one, according to the *Dutch* faſhion.

Likewiſe there is a Shooe of Braſs to fit on to the end of any of the Croſſes, whoſe uſe is the ſame with the Horizon Vane in the Quadrant. I will briefly ſhew the uſe of theſe Contrivances.

Having a Staff thus fitted, place the Horizon Vane upon the Center or eye-end of the Staff, and put on a Croſs fitteſt for your purpoſe, fix the Braſs Shoe at the Lower end thereof, then turn your Back to the Sun, and looking through the ſight (made by the Braſs Shooe) on the end of your Vane, elevate or depreſs the end of your Staff, until the ſhadow made by the upper end of the Croſs, fall upon the upper part of the ſight in the Horizon Vane, then look through that ſight for the Horizon: But if the Sea obſcure the Horizon from your ſight, then remove your Croſs a little nearer to the Horizon Vane; but if on the contrary, your ſight doth not extend ſo low as the Horizon, but the Skie only appears in ſtead thereof, then remove the Croſs further from the Horizon Vane, till you ſee the ſhadow fall upon his due place, and perceive the Horizon exactly at the ſame time, then have you the Suns preſent Altitude.

If you obſerve for the Latitude, you muſt reiterate your Obſervation as before, and when you perceive the Sun to be paſt the Meridian, deſiſt; and concluding your Obſervation, account your degrees and minutes, either of the Altitude, or its Complement, as is before ſhown.

If any deſire to uſe the Staff in a backward Obſervation, after the *Dutch* faſhion, the beſt way is to have a Horizon Vane to ſlide evenly upon the Staff, and then all the variety from the former manner of Obſervation will be this.

Place

Place any of your Croſſes, that you intend to uſe, upon the Center of the Staff, turning the Nut inward, then ſlide on your Horizon-Vane with the Nut inwards, and fix on the Braſs Shooe to the lower end of your Croſs; then proceed with your Obſervation, removing the Horizon-Vane as before you did the Croſs: and the degrees and minutes cut by the edge of the Horizon-Vane, upon the ſide peculiar to the Croſs you uſe, is the Suns Altitude or Complement thereof, as you reckon it in the greater or leſſer Figures.

There is a ſecond contrivance of the Croſs-Staff, *which in ſome reſpects is more convenient than the former, and is commonly uſed by our Countrymen, by ſome called the* Jacob-Staff.

This ſecond contrivance differs little from the former, the Staff being divided and figured after the ſame order, only inſtead of the ſeveral Croſſes in that already deſcribed, here is uſe made only of one Croſs or Tranſum, and two Vanes ſliding thereon.

This Tranſum is made four ſquare, and fitted to ſlide upon the Staff after the uſual manner; the one ſide of this Tranſum is croſſed with ſix ſhort Lines, the two neareſt to each other are diſtinguiſhed with the Figures 30, the next two with 60, the remoteſt with 90; There is a Horizon fitted to this, much like that of the Quadrant.

The Uſe of this Inſtrument is briefly thus.

The long Tranſum ſupplyes the place of the 30, 60, and 90 Croſſes, by the help of the two Vanes ſliding thereon. As ſuppoſe you had occaſion to make uſe of the thirty Croſs, then place the Vanes on the Tranſum to the diviſions under 30, and 30 on each ſide of the Staff; and then by removing your Tranſum to and fro, you may obſerve your Altitude by the edges of the two Vanes, after the ſame manner as you do with the thirty-Croſs, on the ordinary Croſs-Staff. And the ſame is to be underſtood of the reſt of the Croſſes, ſo that with this diſtinction laſt noted, this contrivance of the Croſs-Staff is as uſeful as any other in all reſpects and varieties whatſoever: Beſides, you are not here

troubled to ſhift your Croſſes, in caſe your Altitude ſhould deceive you, (which ſometimes happens) and may chance to be the occaſion of loſing an Obſervation; but in this Inſtrument the Croſſes are ſuddenly altered, only by removing the Vanes to your reſpective diviſions.

Note, That you may place either the upper or lower edge of the Vanes, to the Lines on the Tranſum, as you find moſt Convenient, provided only that you Obſerve by the ſame edges.

SECT. II.

The Deſcription and Uſe of the Quadrant.

THIS Quadrant is of a very commodious Form and Contrivance, being at preſent the beſt approved, and moſt general Inſtrument that is in Uſe for Obſerving the Suns *Meridian Altitude* at Sea.

The Parts of this Inſtrument, are principally three Vanes, and two Arches, which Arches together contain 90 degrees, and give it therefore the Denomination of a *Quadrant*.

The Figure of the Quadrant, and mauner of Obſervation.

Of the three Vanes. That which in time of Obſervation reſpects the Horizon, in this annexed Figure repreſented by A, is called the Horizon-Vane; that which gives the ſhadow, noted by B, is named the

ſhadow-Vane, and that through which you are to look for both ſhadow and Horizon, diſtinguiſhed with C, is called the ſight-Vane.

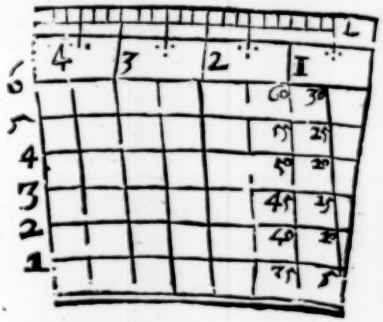
Of the Arches. The leſſer, noted with *d e*, is named the ſixty-Arch, becauſe it uſually contains but 60 degrees; it is of a ſmall Radius, adviſedly ſo contrived, for the more apt placing of the Vane B thereon, that the ſhadow thereof falling upon the Horizon-Vane A, at this ſhort diſtance, might become the ſtronger, and the more perſpicuous to the eye of the Obſerver.

This Arch is commonly divided but to every degree, and numbred from the upper end of the Arch downwards to the Line of Partition (which is a Line drawn on the middle of the upper Leg of the *Quadrant*, between the two Arches) with 5, 10, 15, *&c.* And this is the Complement of the Altitude; ſometimes this Arch is figured with the Altitude, from the Line of Partition upwards towards the higher end of the Arch, with 5, 10, 15, *&c.* to 60; but this is not frequently uſed.

The greater Arch here denoted by the Letters *f*, *g*, is called the thirty-Arch; this Arch is of a large Radius, the better to be divided and ſubdivided into degrees and minutes, the Limb whereof is of a competent breadth, and thereon are uſually deſcribed ſeveral concentrick Circles, interſected with Diagonal Lines, for the more facile and exact dividing the degrees into every tenth, fifth (and ſometimes every ſecond) minute; and hereby the ſubdiviſions are conſpicuous, and may readily be computed by the Obſerver.

But becauſe poſſibly this manner of diviſion may not be underſtood by every one that has occaſion for this Inſtrument, for their ſakes therefore have annexed this following Figure.

The Figure of part of the Arch.



This Figure is part of the Limb of this Arch, as 'tis uſually drawn upon the Limb of the Quadrant, each degree being ſubdivided into five minutes: upon the plain of this Arch are deſcribed ſix Concentrick Circles, and are noted with the figures 1, 2, 3, 4, 5, 6. And in the limits of each degree are drawn two Diagonals interſecting theſe Circles; and thoſe Diagonals divide each degree into two parts, *viz.* into 30 min. and the Concentrick Circles ſubdivide each of theſe Diagonals repreſenting 30 minutes into ſix other parts, being five minutes a piece; therefore the firſt interſection at 5, is five minutes; the ſecond at 10, is ten minutes; the third at 15, is fifteen minutes; the fourth at 20, is twenty minutes; the fifth at 25, is twenty five minutes; the ſixth at 30, is thirty minutes. The firſt again at 35, is 35 minutes; the ſecond at 40, 40 minutes; at 45, is 45 minutes; at 50, is 50 minutes; at 55, is 55 minutes; and at 60, 60 minutes, or 1 degree: And the like is to be underſtood of the reſt, alwayes as they aſcend, encreaſing 5 minutes.

And take this for a general Rule, firſt count how many Concentrick Circles there are, which are uſually ſix (and are to be computed as is here ſhown and noted by the figures at the end of this Scheme) then ſee how many Diagonal Lines are drawn within the extent of each degree, which are commonly two, as in this Figure (ſometimes for the more curious, there are five drawn within this limit) then multiply the number of

Con-

Concentrick Circles, by the number of Diagonals in one degree, and by the Product divide 60 (the minutes in a degree) the Quotient ſhall give you the Number of minutes, that each interſection encreaſes by, and is more than the precedent. As ſuppoſe the Concentrick Circles to be (as uſually) ſix, the Diagonals in each degree (which is rare) five; then multiply ſix by five, the product is 30, by which if you divide 60, the Quotient is 2; which ſhews that the interſections encreaſe by two minutes, the firſt repreſenting 2 minutes, and ſo 4, 6, 8 minutes, &c. to 58 and 60 minutes, or 1 degree; and then 1 deg. 2 min. 1 deg. 4 min. 1 deg. 6. min. &c. and the like is to be underſtood of the reſt.

The Uſe of the Quadrant.

This Inſtrument is ſeldom uſed upon any other occaſion, than to obſerve the Suns Meridian Altitude, which to perform, we will briefly deſcribe.

Firſt, put the Horizon-Vane on the end of the Quadrant at A, and then the ſight-Vane upon the thirty-Arch in the precedent Figure. And laſtly, The upper edge of the Shadow-Vane upon the ſixty-Arch to a certain number of degrees moſt proper for your preſent Obſervation; which readily to perform, take this Caution.

Conſider what will be the Complement of the Meridian Altitude that day, then place the ſhadow-Vane ſo, that the Degrees cut by the upper edge of the Vane, be alwayes leſs by 10 or 15 deg. than you judge the Complement of the Suns Meridian Altitude will be that day in the place of Obſervation.

For inſtance, Suppoſe that the greateſt Altitude of the Sun, for the time, in the place of Obſervation, be eſtimated to be 45 deg. the Compl. is 45 deg. then place the Shadow-Vane at 30 or 35 degrees, which are proper for your preſent Obſervation.

Having thus prepared your Inſtrument, & being ready upon the Deck, turn your back towards the Sun, and holding the Quadrant as upright as you can, place the ſight-Vane to your eye, and looking through the Sight, bring the ſhadow of the upper edge of the Shade-Vane, to fall upon the upper part of the ſlit, or open ſight in the Horizon-Vane, and at the ſame time look through the ſaid ſlit for the Horizon; and if the Sea obſcure the Horizon from your ſight, then ſlide your ſight-Vane a little lower down towards *f*, but if on the contrary your ſight doth not extend

tend ſo low as the Horizon, but if the Skie only preſents it ſelf to your eye, then remove your ſight-Vane a little higher towards *g*, then make Obſervation again, continuing to move your ſight-Vane higher or lower according to theſe directions, until looking through the ſight-Vane, the ſhadow fall upon his due place, and that at the ſame time you exactly ſee the Horizon through the ſight in the Horizon-Vane, then have you the Suns preſent Altitude; but it being the Meridian or greateſt Altitude that you are to Obſerve, you muſt therefore continue to make Obſervations as often you ſhall think fit (but eſpecially you are to tend your Obſervation when you perceive the Sun almoſt upon the Meridian) uutil the Sun be to the Weſtward of the Meridian, and to be leſſening his Altitude; for then if you make Obſervation, the Sky will be ſeen, and not the Horizon; and in this caſe you muſt not alter your Vanes, but letting them ſtand, conclude your Obſervation for that ſeaſon: then caſt your eye upon the thirty-Arch, and ſee how many degrees and minutes are cut by the inſide of the ſight-Vane, and thereto add the degrees at the upper edge of your ſhadow-Vane, the Sum is the Complement of the Altitude, or the Suns diſtance from the Zenith.

Note, The ſmall Arch in ſome Quadrants contains 70 degrees, and the greater 20 degrees, whoſe ſum is 90. Theſe Arches are numbred and divided like the former; and if that be well underſtood, this will not ſeem obſcure, and therefore it is needleſs to ſay any more of this Alteration.

The manner of working your Obſervations of the Meridian Altitude of the Sun, taken by this Inſtrument, ſhall be largely ſhewn in the general Rules for that purpoſe.

Sect. III.

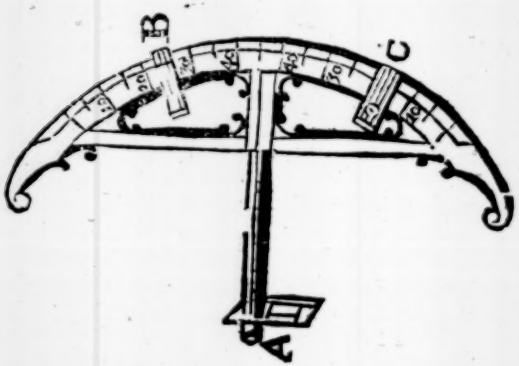
The Deſcription and Uſe of the Croſs-Bow-Quadrant.

This Inſtrument is of good uſe in Navigation, not only for Obſervation, but in regard of the Portability of it, lying in a little room, which is oftentimes a great conveniency in ſome Ships eſpecially; it bears the name

name of a Cross-Bow Quadrant, because of its resemblance to a Cross-Bow.

This Instrument contains a graduated Arch, a Staff, and three Vanes.

The Figure of the Cross-Bow Quadrant,



The graduated Arch, is a Quadrant, or contains 90 degrees, and is numbred from the ends both wayes with 10, 20, *&c.* to 45 degrees in the middle of the Arch.

In the middle of this Arch is made a Shaft and Socket, to contain a Staff fitted thereto, to put in for Observation, and remove at pleasure; this Staff when placed in the Socket, is the Radius of the Arch or Quadrant.

The Vanes are, the *Horizon-Vane*, the *Shadow-Vane*, and the *Sight-Vane*, as in the Quadrant.

The Use of the Cross-Bow Quadrant.

This Instrument is Chiefly to observe the Suns Altitude, which you must thus perform.

First, Put on the Horizon-Vane on the end of the Staff, then place the Shadow-Vane upon the upper part of the Arch, to some certain degree; and

and lastly, put on the Sight-Vane on the lower part of the Arch; thus your Bow is fitted for Observation.

Then standing with your back towards the Sun, take the handle of the Bow in your hand, holding the Instrument as upright as you can, then bring your sight-Vane to your eye, and look through your Sight to your Horizon-Vane, holding your Bow so, as that the upper part of the shade (of your shadow-Vane) may lie upon the upper edge of the slit of your Horizon-Vane.

At the same time you must look through the Horizon-Vane; and if you cannot see it, but do see all Sky and no Water, you must slide your sight-Vane a little higher towards C, but if on the contrary, you see all Water and no Sky, then put your Sight-Vane a little lower towards B; then make Observation again, removing the sight-Vane, until you see the upper part of the Shade to fall upon the upper part of the slit; and likewise see the Horizon at the same time through the Horizon-Vane, then have you the true Altitude of the Sun at that time; but if your Observation be to find the Meridian Altitude of the Sun, then you must wait, and make Observation in the same manner as often as you think fit, until you have obtained his greatest Altitude, and that you perceive the Sun to be to the Westward of the Meridian, then is he fallen; and if you make Observation the Sky will only appear and not the Horizon, therefore let your Vanes stand upon the Arch, and finish your Observation for that time.

Then look upon the lower part of the Arch, and see what degrees and minutes stand against your sight-Vane, and likewise what degrees do stand against the upper edge of your Shadow-Vane, add them together, and the Sum is the Complement of the Altitude, or the distance from the Zenith.

This Instrument may also conveniently be used to make a forward Observation of the Altitude of the Sun or Stars, by removing the Horizon-Vane, and placing the Center of the Staff to your eye, after the manner of the Cross-Saff, the Vanes supplying he want of Crosses, by fixing one Vane to a certain number of Degrees, and removing the other upwards or downwards according to the Altitude to be observed. The sum of the degrees is the Compl. of the Altitude.

The manner of working the Observations by this Instrument, is hereafter inserted in the general Rules for that purpose.

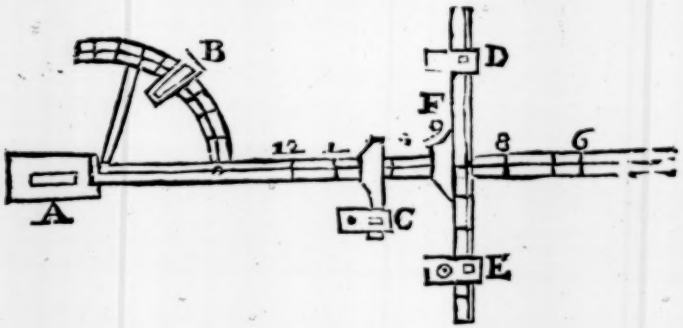
SECT. IV.

The Deſcription and Uſe of the Plow.

The Deſcription of the Plow.

This Inſtrument was antiently in uſe amongſt Mariners, although at this day it is not ſo commonly uſed as formerly; it conſiſts of a Staff having a ſmall Arch, and three Vanes.

The Figure of the Plow.



The Staff is about two foot and a half long, or three foot at the moſt; at the Center-end of which is erected a ſmall Arch, that is divided into 85 degrees; on the ſide of the Staff are ſet off the Graduations proper to the Plow, beginning at 5 or 6 degrees, and encreaſing to 10 degrees towards the Arch, every degree being divided into ſingle minutes.

The Vanes are a *Horizon*, as A, and *Shadow-Vane* as B, (to be uſed as in the Quadrant) and a *Sight-Vane* moving upon the Staff, as at C.

The

The Use of the Plow.

This Instrument is contrived for a backward Observation of the Suns Altitude after the manner of the Quadrant, therefore fit on your Horizon-Vane, and place the Shadow-Vane to a certain number of degrees, so that they may not exceed the Suns greatest Altitude like to be at the time of Observation, but be alwayes somewhat less, yet not so much less as that the difference be above 10 degrees, for in both these cases the divisions on the Staff prove useless; then put the Sight-Vane upon the Staff, and bring the Shade of the upper part of the Vane, to the upper part of the slit in the Horizon-Vane, and look for the Horizon; but if in stead thereof you see all Water, then remove the Sight-Vane towards the Arch; but if on the contrary you see all Sky, and no Water, then move the Vane towards the beginning of the divisions; and this you must reiterate, till the Shadow falling upon this true place, you see the Horizon exactly by the slit in the Horizon-Vane, at the same time you have the Suns present Altitude; and if it be an Observation for the Latitude, then this last work must be repeated as often as you think fit, as in the use of the foregoing Instrument is already declared; The sum of the degrees on the Arch and on the Staff, is the Suns Meridian Altitude.

Sometimes upon the spare sides of the Staff belonging to the Plow, are divided the degrees and minutes proper to the Cross-Staff; and three Vanes or Crosses are accordingly fitted, whose use is in all respects the same with the Cross-Staff, placing the end of the Plow where the Arch stands to your eye, and putting the Vanes (last described) on to the Staff (cross-wayes to the Arch) and turn the said Arch from your eye, that it may not hinder your Observation. What else might be said to the Use of the Plow thus fitted, is already declared in the use of the Cross-Staff.

There is yet a further improvement of the Plow, whereby, it is contrived to supply the place of two other Instruments, beside its own particular use, *viz.* the Cross-Staff and the Quadrant, without inconveniency or incumbrance.

To accomplish this, there is a long Transum, E, F, D, four-square, fitted to slide upon the Staff of the Plow; upon the out-side of this Transum, are drawn seven cross lines, six of which are noted with the figures 30, 60, and 90, and one with the word *Vane*; upon the longer (which is the lower) part of this Transum are drawn several divisions, numbred with 5, 10, &c. and proceeding to 20 degrees upwards

towards the Staff; likewiſe there is a ſight-Vane, as E (like that of the Quadrant) fitted to ſlide upon this Tranſum; the ſpare ſides of the Staff are divided into degrees and minutes, after the manner of the Croſs-Staff. The Uſe briefly follows.

1. *To uſe it as a* Plow.

Place the Horizon and Shadow-Vane as before, then ſliding on the Long Tranſum, with the Nut inward, towards the Arch place the ſight-Vane D, to the Line under the word *Vane*, on the ſaid Tranſum, and then the uſe of it is the ſame with the *Plow* formerly deſcribed.

2. *To Uſe it as a* Quadrant.

The Horizon and Shadow-Vane, ſtanding as before, and likewiſe the long Tranſum with the Nut inwards, place the ſaid Tranſum to the letter Q (on the ſide whereon the Graduations of the Plow ſtand) then bring the ſight-Vane to your eye, and remove the ſame higher or lower upon the Tranſum, until the ſhadow falling upon the upper part of the open Sight in the Horizon-Vane, you ſee the Horizon at the ſame time, then have you the Altitude, which is thus to be computed upon this Inſtrument, Caſt your eye upon the Tranſum, ſee what degrees and minutes are cut by the ſight-Vane, to which add the degrees at the upper edge of the Shadow-Vane, (uſing thoſe diviſions figured with 5, 10, *&c.* at the upper end of the Arch, to 85 at the lower end) the ſum is the Complement of the Altitude, or the Suns diſtance from the Zenith.

3. *To uſe it as a* Jacobs-Staff.

The Tranſum being on the Staff with the Nut inwards, remove the Shadow-Vane and place it on the upper part of the Tranſum on the outſide, as the Sght-Vane ſtands; take off the Horizon Vane, place that end to your eye, turning the Arch downwards (which Arch does aſſiſt you in the holding your Inſtrument, and not at all hinder your Obſervation) and then the uſe hereof is the ſame with the *Jacobs-Staff* already deſcribed. The working your Obſervations ſhall be ſhewn in the general Rules.

SECT.

SECT. V.

The Deſcription and Uſe of an Inſtrument for Obſervation and Operation, called the Removing Quadrant.

The Deſcription of the Removing Quadrant.

This is a uſeful Inſtrument in Navigation, and is convenient for ſtowage in a Cheſt, being it is to take in pieces; it beareth its Name from the manner of its Uſe, one Leg thereof being to be removed in Obſervation.

The parts of it are firſt two pieces with a braſs joynt like a joynt Rule, and will cloſe together; and in the Center is a hole for the putting in the end of an Horizon-Vane, marked with A.

There is alſo a great Arch marked with *d*, *e*, containing a Quadrant, or 90 degrees, divided into minutes by Diagonal Lines, being above an inch in breadth commonly, And alſo there is divided on the ſame Arch, the eight points of the Compaſs, with their halves and quarters.

One end of this Arch is faſtened into one of the pieces with a braſs pin to take in and out at Pleaſure; on each of theſe pieces is a Vane; one a Shadow-Vane noted with C, and the other a ſight-Vane denoted by B; the Shadow-Vane is on that ſide where the Arch is put in and faſtened, and is to move up and down that ſide at pleaſure, for the better and ſharper ſtriking the ſhadow upon the Horizon-Vane; the other ſide moveth upon the Arch, and on the end of this ſide is put the Sight-Vane.

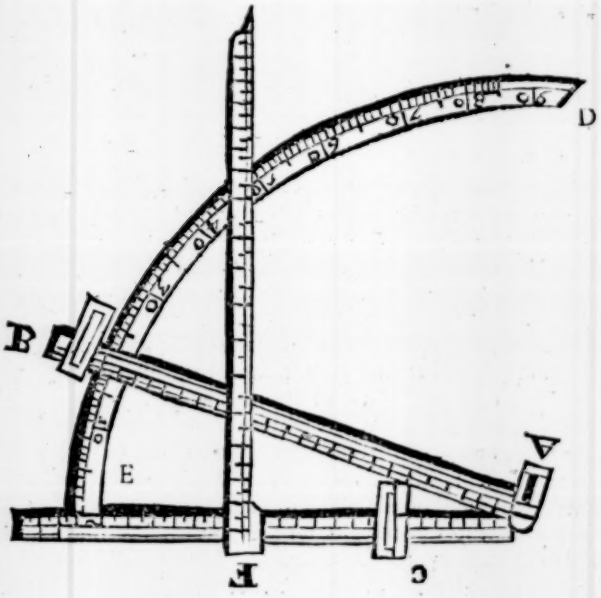
This Inſtrument is principally for a backward, but is alſo capable of a forward Obſervation; The degrees are numbred both wayes, and the Obſervation taken by this Inſtrument is accounted without trouble; for the degrees intercepted between the two containing ſides, is the Altitude of the Sun, and the degrees contained from the ſight-Vane to the lower-end of the Arch, is alwayes the Complement of the Suns Altitude being taken either forward or backward.

This Inſtrument doth likewiſe plainly and more exactly perform the work of the Sinical Quadrant in Navigation, and reſolveth any queſtion in any right-angled Triangle.

For

For the performonce of this work, the two pieces or legs are divided into 60, and ſometimes into an hundred equal parts, which you may call Leagues or Miles in the ſolving any Nautical Queſtion; and there is alſo a long Index that is to have the ſame diviſions on it, as on the legs; and this Index is made to move truly up and down upon the Leg according to the nature of the Queſtion, but alwayes to ſtand at right-Angles therewith; the ſeveral Uſes follow, and firſt for Obſervation.

The Figure of the Removing Quadrant.



To take a Backward Obſervation of the Sun, with the Removing Quadrant.

For the performance thereof, you muſt firſt put the Horizon-Vane into the Center hole, where it is turned round, ſo that you may turn the ſight as

as open and as cloſe as you will your ſelf, ſo alſo that the Horizon-Vane may receive the ſhadow from the ſhadow-Vane; next you muſt put on the two other Vanes, the ſhadow-Vane and the ſight-Vane; the ſhadow-Vane may be put any where upon the Leg, where the Arch is put in and made faſt, then you muſt put in the Arch into that Leg which is the ſtanding part, and pin it in, and alſo put the Arch through the other Leg, to move up and down in time of Obſervation, on which Leg without the Arch, muſt be put on the ſight-Vane; being thus fitted, it is ready for Obſervation.

Therefore turn your back towards the Sun (in the ſame manner as you obſerve with the Quadrant) and place the Inſtrument with the ſight-Vane to your eye, and the Horizon-Vane towards the Horizon, and the ſhadow-Vane uppermoſt, then open the Legs wider and wider, until you ſee the ſhadow of the Sun to fall upon the Horizon-Vane, (as in the Quadrant before mentioned); at the ſame time when you ſee the Horizon through the Horizon-ſight, then you have the Altitude of the Sun cut by the inſide of the movable piece, reckoned from the fixed Leg, and the Complement of the Altitude reckoned from the ſaid inſide of the Leg, toward the lower end of the Arch.

To take a forward Obſervation by the Removing-Quadrant.

This work is but the converſe of the former, for if you at the ſame time take out the Horizon-Vane, and put the Center of the hole as near the Center of your eye as you can and turn your face to the Sun, and letting the upper edge of the ſhadow-Vane cut the Sun, and the inner edge of the ſight-Vane cut the Horizon, the Angle will be the ſame as before, the diſtance of the edge of the ſight Vane, to the inner edge of the removing ſide only excepted, which may be thus allowed; Take the diſtance from the inſide of the Leg to the inner edge of the ſight-Vane, that diſtance meaſured on the Arch, gives the quantity in degrees and minutes, to be ſubſtracted from the Altitude, or added to the Complement of the Altitude found by Obſervation; only note, that in a forward Obſervation you place the ſight-Vane cloſe to the Arch.

The Use of the Removing Quadrant in Operation, shewing the Resolution of the usual Problems in Plain Sailing.

Course and distance being given, to find the difference of Latitude, and the departure from the Meridian?

Course the 6th Rhumb, distance 100 Leagues.

For the solving of this Question by the removing Quadrant, you must proceed thus.

First, Set the inside of the moveable Leg to the Course given in the 6th Rumb, (which you will find upon the Arch of the Quadrant) then upon the said Leg look out 100 Leagues, set the Index thereunto, keeping it with your hand close to the standing part, that the Index may be at right Angles therewith; then where the edge of the Index is cut by the inside of the moveable Leg, you will find 92 Leagues, and $\frac{4}{10}$ the departure from the Meridian.

And upon the other fixed Leg, you will find cut by the Index 38 Leagues, and $\frac{2}{10}$ the difference of Latitude.

Course and difference of Latitude being given, to find the distance and departure?

Course 6th Rumb, difference of Latitude 38 Leagues $\frac{2}{10}$.

To perform this, set the movable Leg to the Course, (reckoned from the fixed Leg) and there keep it fast (by turning the Skrew on the under side thereof) then remove the Index upon the fixed Leg, to the difference of Latitude 38 Leagues $\frac{2}{10}$; and the edge of the Index shall cut upon the movable Leg the distance run 100 Leagues; and upon the Index shall be cut the departure from the Meridian 92 $\frac{4}{10}$ Leagues.

Course and departure from the Meridian being given, to find the distance run, and the difference of Latitude?

Course 6th Rhumb, departure 92 $\frac{4}{10}$ Leagues.

For

For the working this Queſtion, you muſt ſet the moveable Leg to the Courſe given (6th Rhumb) from the fixed Leg, and there keep it faſt, until by moving the Index to and fro on the fixed Leg, the departure from the Meridian be found upon the Index, where it doth juſt touch the inſide of the moveable Leg; then on the fixed Leg the Index will cut 38 Leagues $\frac{2}{10}$, *the difference of Latitude*; and on the movable Leg you ſhall find *cut by the Index*, 100 Leagues, the diſtance run.

The diſtance run, and the difference of Latitude being given, to find the Courſe and departure from the Meridian?

Diſtance run 52 $\frac{3}{10}$ Leagues, difference of Latitude 20 Leagues.

To work this Queſtion by the Removing Quadrant, ſet the Index to the difference of Latitude, upon the fixed Leg 20 Leagues, and there keep it faſt, and then ſeek out the diſtance run upon the movable Leg 52 $\frac{3}{10}$ Leagues, and put that very point to the edge of the Index, and there will be cut upon the Index 48 $\frac{3}{10}$ Leagues, the departure from the Meridian; and upon the Arch you will find cut, by the inſide of the Leg, the ſixth Rhomb, or 67 degrees 30 minutes.

The Diſtance and Departure being given, to find the Courſe and difference of Latitude?

Diſtance 108 Leagues, Departure 90 Leagues.

To reſolve this Queſtion by the Removing Quadrant, find out the diſtance the Ship hath run upon the moveable Leg, and then find out the departure upon the Index, which point is to be ſet to the diſtance found on the movable Leg, as the Index ſtands at right Angles with the fixed Leg; being in this poſition, the edge of the Index ſhall cut the difference of Latitude 60 Leagues upon the fixed Leg; and alſo at the ſame time is cut by the inſide of the moveable Leg (upon the Arch) the Courſe, the fifth Rhomb from the Meridian, or 56 degrees 15 minutes.

The difference of Latitude, and the Departure from the Meridian being given, to find the Course and Distance?

Difference of Latitude 60 Leagues (or 3 degrees) Departure 90 Leagues.

To answer this Question by the removing Quadrant, seek the difference of Latitude 60 Leagues on the fixed Leg, and thereto set the edge of the Index, and then find out the departure 90 Leagues on the Index, unto which point set the moveable Leg, and on the divisions thereof, by the edge of the Index, will be cut the distance run 108 Leagues, and upon the Arch will be found the Course, the fifth Rhumb from the Meridian.

To know how many Leagues you are to Sail upon any Point of the Compass, to alter one degree of Latitude by the Removing Quadrant.

To perform this, you must set the edge of the Index to 20 Leagues on the fixed Leg, and then placing of the inside of the movable Leg unto the first Rhomb from the Meridian, you will find cut the Index upon the movable Leg (which alwayes represents the distance run); the number of Leagues which you are to run upon that point of the Compass to raise one degree of Latitude, *viz.* 20 Leagues, 1 Mile; and on the second Rhomb you will find it to be 21 Leagues 2 Miles; and on the Third Rhomb 24 Leagues; and on fourth Rhomb 28 Leagues 1 Mile; and on the fifth Rhomb 36 Leagues; and on the sixth Rhomb 52 Leagues 1 Mile; and on the seventh Rhomb 102 Leagues 1 Mile.

The Departure from the Meridian is also given upon the edge of the Index at the intersection thereof, with the movable Leg, at every removing to the several Rhombs; as on the first Rhomb you will find it to be 4 Leagues; on the second Rhomb 8 Leagues 1 Mile; on the third Rhomb 13 Leagues 1 Mile; on the fourth Rhomb 20 Leagues; and on the fifth Rhomb the departure is 30 Leagues; and on the sixth Rhomb it will be 48 Leagues 1 Mile; on the seventh Rhomb you will find the departure to be 100 Leagues 1 Mile.

To know how many miles answer to one degree of Longitude in any Latitude, by the Removing Quadrant.

For the performance hereof, you must set the inside of the movable Leg to the Latitude of the place found upon the Limb, reckoned from the fixed Leg, then removing the Index up and down on the fixed Leg (at right Angles with it) until the edge of the Index doth cut 60 Miles on the moveable Leg; at that time you may see how many Miles is cut by the edge of the Index on the fixed Leg, and those are the quantity of Miles answering to one degree of Longitude in that Latitude.

Example.

For the Latitude of 51 degrees 30 minutes, I demand how many Miles answer to one degree of Longitude?

Therefore I first set the inside of the moveable Leg, to the Latitude of 51° 30′ found on the Arch, counted from the fixed Leg; then slide the Index upon the fixed Leg, until the edge thereof doth intersect 60 on the moveable Leg; then on the fixed Leg you will find cut by the edge of the Index 37 $\frac{1}{10}$ Miles shewing that in the Latitude of 51° 30′, there must be 37 $\frac{1}{10}$ Miles; to one degree of Longitude.

SECT. VI.

Rules for finding the Latitude of the Place, by Observations of the Suns Meridian Altitude, or Zenith Distance, by help of the Table of the Suns Declination.

BEcause 'tis common to work the Observations of the Sun, taken by the Quadrant, and other Instruments (now in use) by the Complement of the Meridian Altitude, or the Suns distance from the Zenith, I shall therefore give Rules, Illustrated with Examples, for that purpose.

Rule 1.

If the Sun come to the Meridian in the South, and have South Declination, Substract the Declination from the Complement of the Meridian Altitude, the remainder is the Latitude of the Place of Observation Northerly: but if the Declination exceed the Zenith distance, then substract it from the Declination, the remainder is the Latitude Southerly.

Example 1.

Admit you are at Sea, and the Sun being upon the Meridian in the South, is 37 deg. 30 min. distant from the Zenith, and at the same time hath 12 deg. 00 min. South Declination; I demand the Latitude of the place?

The Operation.

Complement of the Meridian Altitude ——	37°	30′
The Suns Declination, South, substract ——	12	00
The Latitude of the place,	15	30 North.

Example

Example. 2

Admit, being at Sea, the Sun being on the South part of the Meridian is 10 degrees distant from the Zenith, and the Declination 20 degrees 30 minutes South; I demand the Latitude of the place?

The Operation.

The Suns Declination	20°	30′
The distance from the Zenith subſtract	10	00
The Latitude	10	30 South.

Rule. 2.

If the Sun be on the Meridian in the South, and have North Declination, then add the declination to the Zenith distance, the Sum is the Latitude Northerly.

Example.

Admit a Ship at Sea, and the Sun on the South part of the Meridian 30 degrees 30 miuutes from the Zenith, and that the Declination is 15 degrees 30 minutes North, I demand the Latitude?

The Operation.

The Complement of the Altitude or Zenith-distance is	30°	30′
The Declination added	15	30
The Latitude	46°	00′ North.

Rule 3.

If the Sun be on the Meridian in the North, and have North Declination, then subſtract the Co-altitude or Zenith-distance from the Declination, the remaindet is the Latitude Northerly; But if the Co-altitude exceeds the Declination, then subſtract the Declination therefrom, the remainder is the Latitude Southerly.

Example

Example 1.

Suppoſe the Declination were 20° North, and the Co-altitude 12 deg. 30 min. the Sun being upon the Meridian in the North; I demand the Latitude?

The Operation.

The Suns *Declination* North	20°	00′
The *Co-altitude* ſubſtract	12	30
The *Latitude* of the Place	07	30 North.

Example 2.

Suppoſe the Suns *Declination* to be as before, 20 deg. North, and that being upon the Meridian to the Northwards, his *Co-altitude* is 40 deg. 15 minutes, I demand the Latitude?

The Operation.

The *Co-altitude* of the Sun is	40°	15′
The *Declination* North ſubſtract	20	00
The *Latitude*	20	15 South

Rule 4.

If the Sun be upon the Meridian in the North, and hath South *Declination*, then add the *Declination* to the *Co-altitude*, the Sum is the *Latitude* Southerly.

Example.

Admit the Suns *Declination* were 16 degrees 45 minutes South, and the *Co-altitude* 29 degrees 45 minutes, I demand the *Latitude*?

The Operation.

The *Declination* of the Sun South	16°	45′
The *Co-altitude* add	29	45
The *Latitude*	46	30 South.

Rule 5.

If the Sun have no *Declination*, then the Complement of the *Altitude* is the *Latitude* of the Place; and if the Sun be on the *Meridian* in the South, your *Latitude* is Northerly, if in the North, Southerly. This needs no *Example.*

Rule 6.

If the Sun be in the *Zenith* (*i. e.*) 90 degrees above the Horizon, then the *Declination* either Northerly or Southerly is the *Latitude* of the place. This likewise needs no illustration.

Rule 7.

If you be within the Artick or Antartick Circles, and observe the Sun upon the Meridian under the Pole, then add the Suns *Declination* to the Complement of the Altitude, and substract the sum from 180 degrees, the remainder is the *Elevation* of the Pole.

Note,

If your Instrument wherewith you Observe, give only the *Meridian Altitude*, (as the *Plow*, or some other) then substract that *Altitude* from 90 degrees, the Residue is the *Zenith*-distance, or *Co-altitude* of the Sun, and the *Operation* is the same as in the precedent *Examples.*

For the Stars.

What hath here been delivered in these Rules concerning the Suns being upon the *Meridian*, the same is to be understood of any Star, whose *Declination* is known.

Admit

Admit you should observe the bright Star *Arcturus*, whose *Declination* is 21° 19′ North, when he is upon the *Meridian* in the South, and find his Altitude to be 65° 25′, the Complement thereof is 24° 35′, the distance from the *Zenith* (or *Co-altitude*); then adding 21° 19′, to 24° 35′, the sum 45° 54′, the *Latitude* Northerly, according to the *second Rule* afore-going.

But if you observe by any of the Stars near the *North-Pole*, whose *Polar-distance* is set down in the Tables of *Declination*, and if they be on the *Meridian* under the *Pole*, add the Complement of their *Declination*, or *Polar-distance*, to the *Meridian-Altitude* found, the sum is the *Latitude* Northerly.

But *secondly*, If you observe any Star that is upon the *Meridian* in the North, above the *Pole*, then from the *Meridian-Altitude* of that Star substract the Complement of his *Declination*, or *Polar-distance*, the remainder is the *Latitude* Northerly; or if out of the Complement of the Stars *Declination* you can substract his *Meridian-Altitude*, the remainder is the *Latitude* Southerly. The same may be understood of Stars near the South-Pole.

Here I thought it necessary to mention something of the *Crossiers*, which are certain Stars that are of great use in the Southern Navigation, they are so called, because they do somewhat resemble the form of a Cross, according to the annexed Figure.

The Figure of the Constellation, called the Crossiers.

The Star at C, is the Principal Star for Observation, called the *Cocks-Foot*, whose *Declination* is 60 degrees Southerly, according to the opini-

on

on of Mr. *Wright*, in his *Correction of Errors*. But the preſent *Declination* of this Star, according to the judgement of ſome of our ableſt Navigators, is 61 deg. 15 min. Southerly, and ſo the Complement of the *Declination*, or *Polar-diſtance*, is 28 deg. 45 min. By this *Polar-diſtance* and the *Meridian-Altitude* of this Star, when he is either above or below the Pole, you may find the Latitude of the place, by the Rules of the Stars laſt mentioned.

To know when the Star is fit for Obſervation, hold up a thred and Plummet, and when the thred cuts the Star at A, and that at C both at once, then is the *Cocks Foot* upon the *Meridian*, and fit to be obſerv'd.

SECT. VII.

The Deſcription and Uſe of the Nocturnal.

THIS Inſtrument conſiſts of three parts.

Firſt, the broadeſt and greateſt, which we may call the unmoveable part, which hath a handle to hold it by in time of Obſervation.

Secondly, The firſt movable or middle part.

Thirdly, The long Index that is to turn to the poſition of thoſe Stars for which they are made, *viz.* the guards of the Little or great Bear.

The foreſide of the firſt or unmovable part, hath the Limb or outward Circle divided into twelve months, and each month ſubdivided into its reſpective dayes, and are counted towards the left hand, and marked with their names, or the firſt letter thereof, as *J* for *January*, *F* for *February*, *M* for *March*, *&c.* And upon ſome of them there are two other Circles, the outermoſt of which is divided into 24 equal parts or hours; and the other into 29 parts $\frac{1}{2}$, or dayes of the Moons Age, by which the Moons Southing may be known by inſpection, and thereby a computation of the Tydes.

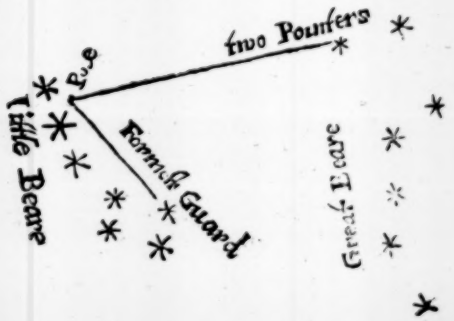
Of theſe Nocturnals there are two ſorts, one for the Guards of the little, the other for the Guards of the great Bear, or *Charles*'s *Wain*, com-

monly called the two *Pointers*. Now to know for which of these Constellations any Nocturnal is made: You may observe, that the Nocturnals that are for the Guards of the great Bear, have the 17*th* of *February* on the top; and if it be for the Guards of the little Bear, then you will find the 21 of *April* there. The backside of this part is divided into the 32 Points of the Compass, which are to shew the bearing of the Guards, thereby to know what *Declination* the North Star hath upon any point of the Compass.

The second and moveable part, hath a Tooth proceeding from it, with the edge continued in a right Line from the Center, which is to be turned to the day of the moneth at pleasure; and on the superficies thereof, is a Circle divided into 24 equal parts, or hours, which when the said Tooth is set to the day of the month, and the Index turned to the position of the Guards, the strait side of the Index will shew the hour of the hour of the Night upon the the said Circle.

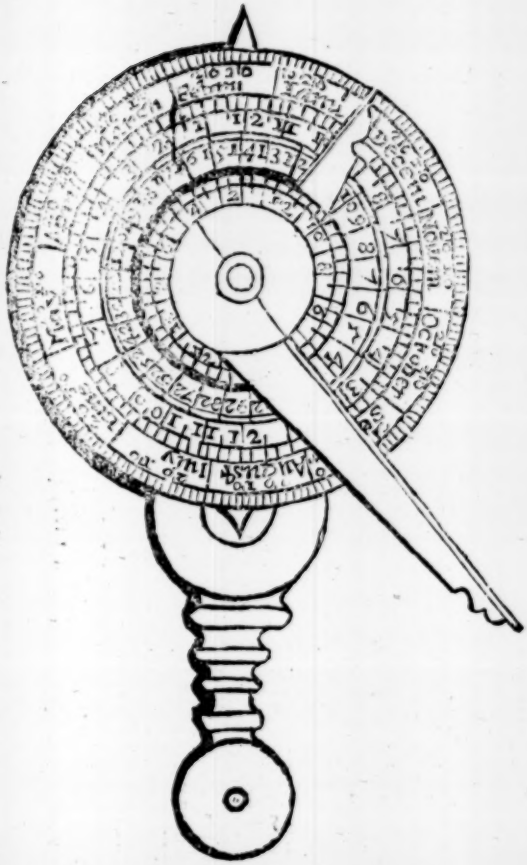
The third and upper movable part is called the Index, having one side thereof proceeding from the Center, which is to be turned to the Guards in time of Observation; and through all these pieces in the Center of the Instrument is a hole, through which you are to see the North Star, and at the same time the Index to be turned to the Guards.

The Figures of the Stars, as they shew themselves in the Heavens, for which the Nocturnals are made.



The

The Figure of the Nocturnal.



Here followeth a Table for the Declination of the North Star, upon every point of the Compass the guards are upon, fitted for both sorts of Nocturnals.

Points of the Compass.	For the guard of the Little Bear.	For the guards of the Gr. Bear, or aftermost Wheels in *Charles Wain*, called the two Pointers.	
	D. M.	D. M.	
North.	2 09	2 20	Above the Pole.
N by E	1 52	2 30	
N N E	1 29	2 35	
N E by N	1 02	2 33	
North East	0 35	2 26	
N E by E	0 06	2 13	
E North E	0 22	1 55	
E by N	0 52	1 33	
East.	1 18	1 07	
E by S	1 41	0 38	
E S E	2 01	0 08	The North Star is under the Pole.
S E by E	2 16	0 22	
South East	2 25	0 52	
S E by S	2 30	1 20	
S S E	2 29	1 44	
S by E	2 22	2 04	
South.	2 11	2 20	
S by W	1 55	2 30	
S S W	1 34	2 29	
S W by S	1 10	2 28	
South West	0 43	2 26	
S W by W	0 14	2 13	
W S W	0 15	1 55	
W by S	0 44	1 33	
West	1 11	1 07	
W by N	1 36	0 38	
W N W	1 58	0 08	
N W by W	2 14	0 22	Above the Pole
North West	2 25	0 52	
N W by N	2 30	1 20	
N N W	2 29	1 44	
N by W	2 22	2 04	

If the former of the Guards be ascending from the North or lower part of the Meridian. — The North-star is above the Pole.

If the former of the Guards be descending from the South, or upper part of the Merid. — The North Star is under the Pole.

If the after Wheeles, or two Pointers be ascend. from the North or lower part of the Meridian. — The North Star is under the Pole.

If the two Pointers be descending from the South upper part of the Meridian. — The North Star above the Pole.

The manner of holding the Nocturnal in time of Obſervation.

Take the handle in your hand, with the fore-ſide towards you, holding of it upright in your hand, (which you may diſcern by the tip that is on the very top of the Nocturnal) then looking through the hole in Center to the North Star, you muſt turn the upper edge of the Index (which cometh from the Center) to the Guards; this being underſtood, you may now proceed to the ſeveral Uſes thereof.

To find the hour of the Night by the North Star, and the Guards either of the Little or Great Bear, and upon what Point of the Compaſs they are.

To perform this, you muſt firſt ſet the Index of the ſecond moveable part to the day of the month (then if it will not ſtay of it ſelf, you muſt ſtay it with your thumb) holding of it as you are before directed; find the North Star through the hole, and turn the Index to the Guards, and then upon the ſecond movable part, the edge of the Index ſhall cut the hour of the Night, at the ſame time you will find on the back-ſide what Point of the Compaſs the Guards are upon, ſo that you may know alſo what *Declination* the North Star hath at that time, either above or under the Pole.

To find the time of the Moons coming to South any day of her Age, and alſo the time of High-Water that Day.

Firſt, Find the Moons Age on the moveable part, and right againſt it, *in the Circle of Hours*, you will find the time of the Moons Southing.

Example.

Suppoſe the Moon were eight dayes old, I demand the time of her coming to South? There-

Therfore look for 8 on the Circle of her Age, and right againſt it you will find in the hour Circle, al moſt half an hour paſt ſix of the Clock in the Evening (becauſe that alwayes between the Change and the Full, ſhe cometh to South in the Evening, but after the Full ſhe cometh to South in the Morning) ſo having found the Moons Southing, if you add thereto the hour of the flowing at any place, it will ſhew you the time of High-Water that day.

Example.

Suppoſe that here at *London* the Moon being 8 dayes Old, I find by the Nocturnal, that the Moon cometh to South at almoſt half an hour paſt ſix of the Clock; to which I add three hours, the time of High-Water at the Full and Change, which make 9 of the Clock and almoſt half an hour paſt, the time of High-Water at *London Bridge* that day of the Moons Age.

And if thoſe Numbers being added together ſhould exceed 12, that 12 muſt be ſubſtracted from it, and that will be the time of Full-Sea. As ſuppoſe the Moon ſhould be 13 dayes old, at which time I find by the Nocturnal that the Moon cometh to South at 10 of the Clock, and almoſt half an hour, unto which if you add 3, it maketh 13 hours and a half, from which if you take 12, there remains 1 of the Clock and almoſt half an hour; the time of High-Water.

Sect. VIII.

The Deſcription and Uſe of the Moon-Dials, that are commonly in the Lids of Pocket Sun-Dials.

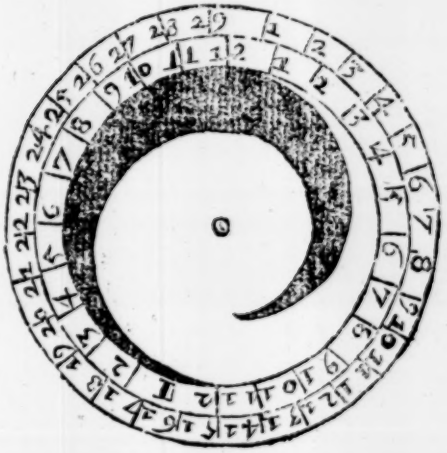
THeſe Dials do conſiſt of 2 parts, one movable and the other unmoveable; on the unmovable part are 2 Circles; on the outtermoſt is placed the Age of the Moon, on the innermoſt the 24 hours of the day and night.

The other is the moveable part, which alſo hath a Circle of hours, and an Index iſſuing from the edg thereof, which upon occaſion is to be turned to any day of the Moons Age required; and ſometimes on the Plate are five Aſpects with which the Moon doth reſpect the Sun, according to the Quantity of her ſeparation in Signs, as you may ſee in this annexed Table.

The

The Figure of the Moon-Dial.

Characters.	Names of the Aspects.	Dist. S.	D.
☌	*Conjunction,*	0	00
✶	*Sextile,*	1	00
□	*Quartile,*	3	00
△	*Trine,*	4	00
☍	*Opposition.*	6	00



The Uses follow

To find the time of High-Water in any place; the hour of Full Sea at the Full and Change of the Moon being known.

For the performance of this, the Age of the Moon must be known, unto which you must set the Index of the moveable Plate, which having done, seek the hour of High-Water at the Full and Change on the same Plate, and right against it, in the hour Circle, on the unmovable Plate, shall be shew'd the time of High-Water that day.

Example.

Suppose at *London-Bridge* I would know what time it is High-Water when the Moon is five dayes old; I therefore set the Index of the moveable

able Plate to 5 in the Circle of the Moons Age; and then becauſe it is High-Water at 3 of the Clock on the Full and Change day at *London-Bridge*; therefore I look againſt the hour of three in the moving Plate, and right againſt it I find the figure 7 in the hour Circle on the unmoveable Plate, which is the time of High-Water.

To find the hour of the Night by the ſhadow of the Moon upon a Sun Dial, by help of the Moon-Dial.

You muſt firſt ſet the Index of the moveable Plate to the Age of the Moon, and then take notice upon what hour of the Dial the Shadow of the Moon doth fall, the ſame hour ſeek on your moving Plate, and right againſt it, in the hour Circle on the unmoveable Plate, ſhall be the true hour of the night.

Example.

Suppoſe the Moon were 17 dayes Old, and I ſee the ſhadow of the Moon to fall upon the hour of 10 on the Sun Dial, therefore I ſet the Index of the moveable Plate to 17, in the Circle of the Moons Age; and right againſt the hour of 10, on the movable Plate, (which was the ſhadow of the Moon upon the Dial) ſhall be cut 11 and ſomewhat more than half an hour, which is the true hour of the Night.

If the movable Plate be divided with the Aſpects upon it, then it is thus to be uſed:

You are to take notice, that the place of the Sun is repreſented by that Point where the Age of the Moon beginneth, juſt at the place of the Conjunction of the Sun and Moon, which is in the Circle of the Moons Age, on the moveable Plate; therefore if you would know what Aſpect the Moon hath to the Sun, you muſt ſet the Index of the removing Plate to the Age of the Moon, and then at the point of Conjunction, you will ſee what Aſpect cutteth it (for the Character of the Aſpect is grav'd upon the Line of correſpondence); as if you turn the Index to 3 dayes and a half of the Moons Age, you will find that the correſpondent Point of the Sextile Aſpect, will cut the Point of Conjunction; and if you turn the Index to the ſeventh day of the Moons Age, you will find that the Correſpondent part of the Quartile Aſpect will cut the point of Conjunction. And the ſame way you may proceed in the reſt.

To know when the Moon cometh to South by the Moon-Dial.

First ſet the Index of the moveable Plate to the Age of the Moon, in the Circle of the Moons Age; which being done, look right againſt 12 in the moveable Plate; and there ſhall be cut, on the hour Circle (of the unmovable Plate) the time of the Moons coming to South.

As ſuppoſe the Moon were 24 dayes old, unto which I ſet the Index, and right againſt 12 in the hour Circle, ſhall be cut 7 a Clock and almoſt a quarter in the morning, becauſe the Moon is paſt the Full.

CHAP. X.

Containing the Uſe of the Plain Scale, Gunters Scale, Sinical Quadrant, Plain Chart, Mercators Chart, of both Globes, of the Inclinatory-Needle; and likewiſe the ſecret Properties of the Load-Stone.

SECT. I.

The Deſcription and Uſe of the Plain Scale.

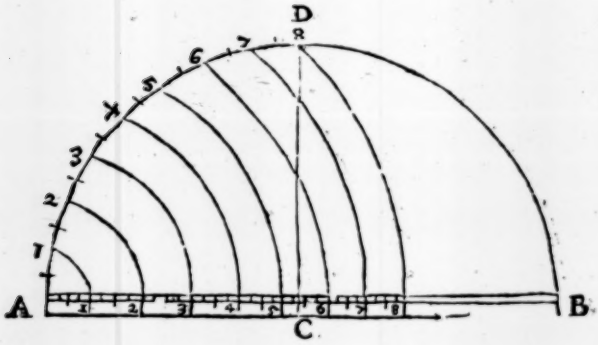
THE Uſe of this Inſtrument is facile and delightful, and ſerves for the Illuſtration of *Problems* in *Navigation* and *Aſtronomy*.

The Lines on a Plain Scale, are uſually a Line of equal Parts, Chords,

Rhombs, and Longitude; but on this here described, are likewise a Line of Natural Sines, Tangents and Secants.

We shall here insert the Projection of these Lines on the Scale.

The Line of Rhombes.

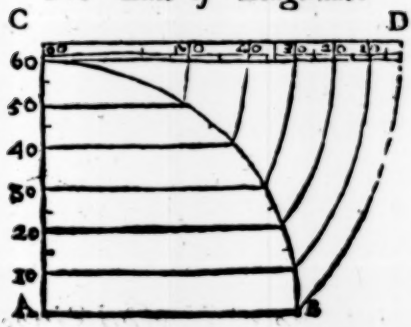


The Projection of the Line of Rhombes.

For the dividing of the Line of Rhombs, first draw the Line A C B, and upon the Point C describe the Semicircle A D B, and divide the Quadrant A D into 8 equal parts, which being done, set one foot of your Compasses in the Point A, and with the other foot extend to each of those divisions, and transfer those extents unto the Line A C B, which will divide the said Line into eight unequal parts, which will be a Line of Rhombs, and to be numbred with 1, 2, 3, 4, &c. unto 8.

XY

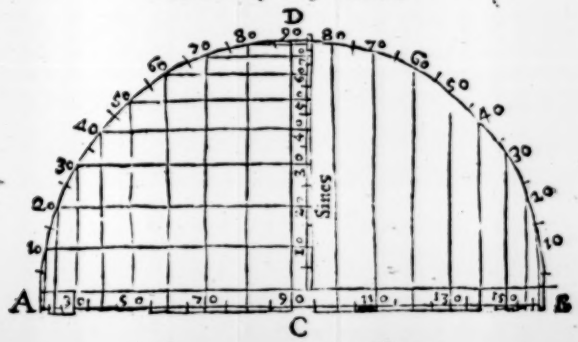
The Line of Longitude.



The Demonſtration of the Line of Longitude.

Firſt draw the Quadrant C A B, and divide the ſide C A into 60 equal parts; then through each of thoſe equal parts, draw Lines Parallel to the ſide A B, until they touch the Quadrant C B; which being done, ſet one foot of your Compaſſes in the Point C, and extend the other foot unto each reſpective Point of interſection in the Quadrant C B; and then transfer them to the Line C D (which is to be the diſtance between C and B, or the Chord of 90 degrees) ſo ſhall thoſe Interſections divide the Line C D into 60 unequal parts, which is called the *Line of Longitude.*

The Line of Verſed Sines.



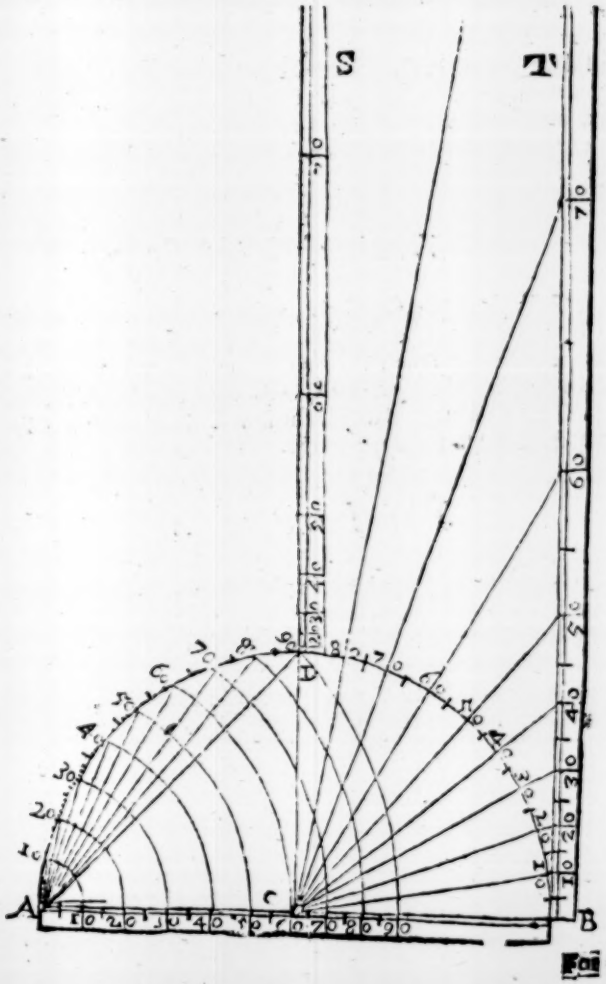
The Line of Right Sines.

The demonſtration of the Line of Sines is thus to be performed; Firſt draw the Line A C B and upon C deſcribe a Semicircle, and one of the Quadrants divide into 90 degrees as the Quadrant A D C, then draw a Line through each tenth degree of the Quadrant parallel to the Line A C B, it will divide the Line D C into 90 unequal parts, which will be a Line of Natural Sines, and to be numbred from C towards D, with 10, 20, 30, *&c.* unto 90.

The Line of Verſed Sines.

For the Projection of the Line of Verſed Sines, it is thus to be effected; Firſt draw the Line A C B, and upon C draw the Semicircle A D B, which divide into 180 Degrees, then drawing right Lines parallel to the Line D C, they will divide the Line A B into 180 unequal parts, which will be a natural Line of Verſed Sines, and to be numbred with 10, 20, 30, 40, *&c*, unto 180.

The Line of Chords.



For

For the Demonſtration and Diviſion of the Line of Chords, you muſt firſt draw the Diameter A C B in the foregoing Scheme, and upon the Center C deſcribe the Semicircle A D B; which Semicircle divide into two equal Quadrants by the Point D, then divide the Quadrant D A into 90 equal parts or degrees; this being done, ſet one foot of your Compaſſes in the point A, let the other be extended to each drgree of the Quadrant A D, which Extents transfer unto the Line A C B, as you may ſee the Arches lead in the foregoing Figure. This Line ſo divided into Ninety unequal diviſions, is called a Line of Chords, and may be ſet on any Scale. After this manner you make it of what Radius you pleaſe; and number it with 10, 20, 30, *&c.*

The Line of Natural Tangents.

Firſt draw the Quadrant, as in the foregoing Scheme, and divide it into 90 degrees, and from the Point B erect a Perpendicular Line, as the innermoſt Line T B, then from the Center C draw Lines through each degree of the Quadrant C D B, until they touch the Line T B, and thoſe interſections will divide the Line T B into a natural Tangent, to be numbred with 10, 20, 30, *&c.*

The Line of Secants.

Having drawn thoſe Lines in the foregoing Scheme, through each reſpective degree of the Quadrant, from the Center C, until they touch the Line T B, extend your Compaſſes from the Center C to the extremity of each reſpective Line, and the foot of the Compaſſes ſtill remaining in the Point C, tranſter the ſaid Lines unto the Line C D S, ſo ſhall they divide the ſaid Line into unequal parts, which is a Line of Natural Secants, and number them with 10, 20, 30, *&c.*

Problems of Plain Sailing by the Plain Scale.

Problem I.

A Ship Sailes N. E. by E. 108 Leagues; I demand the difference of Latitude and Departure?

In the following *Problems* of *Plain Sailing*,
A C represents the *Distance Sailed.*
A B the *Difference of Latitude.*
B C the *Departure.*
B A C the *Course.*
A C B the *Complement of the Course.* *Fig.* 26.

Draw the occult Line A B, take off 60 from the Line of Chords, and sweep the prick'd Arch d e, Set off the Course five points, taken from the Line of Rhombs, from d to e; then draw the Line A e C, and set off 108 Leagues, by the Line of equal parts, from A to C let fall the perpendicular B C, and so finish the Triangle A B C, in which you will find the Diff. Lat. A B 60 Leagues. The Departure B C, 90 Leagues.

Problem. II.

A Ship Sailes N. E. by E. until her difference of Latitude be 60 Leagues; I demand the Distance and Departure?

Fig. 26

Draw A B of the given length, and raise the occult perpendicular B C, set off the Course 5 points, as in the former *Problem.* Draw A C until it meets with B C, and finish the Triangle; the Distance is 108 Leagues, and the Departure 90 Leagues.

Problem III.

A Ship Sailes N. E. by E. until her departure be 90 Leagues; I demand the Distance and Diff. Lat.

Fig. 27.

Draw

Draw the occult Line A B, and raiſe the Perpendicular B C of the given length 90 Leagues; then upon the Point C ſweep the Arch d e, with the Chord of 60°, and place the Complement of the Courſe three Points from d to e, then draw C e A until it meet with A B, and finiſh the Triangle; The Diſtance is 108 Leagues; the Difference of Latitude 60 Leagues.

Problem. IV.

A Ship Sailes between the North and the Eaſt 108 *Leagues, until the Difference of Latitude be* 60 *Leagues; I demand the Courſe and Departure.*

Fig. 28.

Draw A B 60 Leagues and raiſe the occult perpendicular B C, take off the Length of A C the Diſtance 108 Leagues, and placing one point of your Compaſſes at A, deſcribe the occult Arch cutting the Line B C at the point C, by which draw A C and finiſh the Triangle; the Departure B C is 90 Leagues, with a Chord of 60° ſweep the Arch d e, which meaſured upon the Line of Rhombs, will be found five Points, the Courſe ſought.

Problem. V.

A Ship Sailes between the North and Eaſt 108 *Leagues, until her Departure be* 90 *Leagues; I demand the Courſe and Difference of Latitude?*

Fig. 28

Draw the occult Line A B, and raiſe the Perpendicular B C of the given Length 90 Leagues; take A C 108 Leagues, and ſeting one point of the Compaſſes at C, deſcribe the occult Arch cutting the Line A B at A, by which draw A C and finiſh the Triangle, the Courſe is five points, meaſured as in the former *Problem*, the Difference of Lat. 60 Leagues.

Problem. VI.

A Ship Sailes between the North and Eaſt, until the Difference of Lati-

tude

rude be 60 Leagues, and the Departure 90 Leagues? I demand the Course and Diſtance?

Fig. 28.

Draw A B 60 Leagues, raiſe the perpendicular B C 90 Leagues, and by the Points A and C, draw A C, and finiſh the Triangle; The Courſe is found 5 points, as in the 4th *Problem*; the Diſtance 108 Leagues.

Problem. VII.

There are two Ports that bear S. W. by S. and N. E. by N. diſtant 40 Leagues; A Ship ſailes from the Northermoſt of them, firſt South, and then Weſt by South, ſometimes upon one of theſe Courſes, ſometimes upon the other, until ſhe arrive at the Southermoſt Port; I demand how many Leagues ſhe hath ſailed upon one Courſe, and how many upon the other?

Fig. 29

Let A repreſent the Northermoſt Port, and E the Southermoſt, A E their Diſtance, A D the Diſtance ſailed upon the South Courſe, D E the Diſtance upon the W. by S. Courſe.

Draw the Line A E 40 Leagues, being a N. E. by N. and a S. W. by S. Line; Deſcribe the Arch f g, ſetting off three points, and draw the occult Line A D, being a South Line; then ſweep the Arch h I, and ſet off four points, drawing the occult Line D E until it meet with A D, and ſo finiſh the Triangle A D E; The Diſtance ſailed South is 29 Leagues, and W. by S. is 22½ Leagues.

Problem. VIII.

There are two Iſlands that bear Eaſt and Weſt, and are Diſtant 40 Leagues; A Ship ſailes from the Weſtermoſt N. E. by E. and then ſailing 22 Leagues and a half further, arrives at the Eaſtermoſt Port; I demand the Diſtance ſailed upon the firſt Courſe, and what was the ſecond Courſe?

Fig. 29

Let A repreſent the Weſtermoſt Port, E the Eaſtermoſt, D the place where the Ship altered her Courſe, making the beſt of her way; A D the N. E. by E. Courſe; D. E. the other Courſe unknown; Draw A E 40 Leagues, ſet off an Angle of three Points, and draw A D, the N. E. by E. Line, occultly; take the Diſtance 22 Leagues and a half, and placing one point of your Compaſſes in the point E, croſs the Line A D in the point D, draw D E and finiſh the Triangle: The Diſtance upon the firſt Courſe is 29 Leagues, the Angle at E is four points, therefore the ſecond Courſe is S. E.

Problem. IX.

Two Ships ſail from the ſame Iſland, the firſt ſailes N. W. by N. 22. Leagues and a half, the ſecond W. by N. 40 Leagues, and arrive at their ſeveral Ports; I demand the Bearing and Diſtance of thoſe Ports?

Fig. 29

E repreſents the Iſland, D the Northermoſt Port, A the Eaſtermoſt.

Draw A E. 40 Leagues, and ſet off the Angle at E four points, and draw D E 22 Leagues and a half, then by the Points D and A, draw A D, and finiſh the Triangle; the Angle at A is 3 points, which ſhews the bearing of the Ports to be E. N. E. and W. S. W. and the Diſtance A D 29 Leagues.

Problem. X.

A Ship ſailes from a certain Port W. N. W. 22 Leagues and a half, and then more Southerly 29 Leagues, and ſhe is forced back again to the Port from whence ſhe came 40 Leagues; I demand her Courſe from the ſecond place to the third, and how ſhe ſteered back again.

Fig. 29

E repreſents the firſt Port, D the place where the Ship altered her Courſe, A the Place where ſhe was driven back.

Draw the Line D E 22 Leagues and a half, take the Diſtance A D 29 Leagues, placing your Compaſſes in D, deſcribe the occult Arch at A, and take the Diſtance A E 40 Leagues, deſcribe another occult Arch croſſing the former in the Point A; draw A E and A D, and finiſh the Triangle;

Triangle; The Arch m n is 9 points, therefore the Courſe from the ſecond Place to the third is S. W. by S. and ſhe ſteered back again to the firſt Port E. N. E.

Here follow ſome *Problems* of *Mercators Sailing*, wrought two wayes.

Firſt, By the *Plain Scale* only, by taking the middle Latitude, which is not exactly true, but may ſerve as an approximation in a ſingle Courſe, provided the diſtance be but ſmall, otherwiſe 'tis too groſs.

The *ſecond* way is by the *Meridional Parts*, which will be exact, according to the capacity of the Inſtrument.

The Uſe of the Plain Scale in Mercators Sailing by the middle Latitude.

Problem 1.

A Ship being in the Latitude of 40 degrees, Sails a North-Weſterly Courſe, until ſhe come into the Lat. 45° 30′, the difference of Longitude 90 Leagues, I demand the Courſe, Diſtance and Departure?

Fig. 30

For the ſolution hereof by the *Plain Scale*, firſt draw the Line A C B, and upon the Center C deſcribe the Semicircle A D B, and croſs the Line A C B at right Angles with the Line E C D; then by Arithmetick find the middle Latitude, by taking the half Sum of both Latitudes added together, which you will find to be 42° 15′, which middle Latitude ſet off from D to M and L both wayes, and draw the Line M L then ſet the Diſtance D F from B to G, then ſet off the difference of Latitude 110 Leagues from B to H, and from G to A; and upon the point A erect a perpendicular, as A K, and from A ſet off the difference of Longitude in Leagues, which is 90, from the point K draw the Line K G, then from the point H erect an occult perpendicular as the Line H I, then laying a Ruler from the point B, to the point E, where the Line C K doth cut the Line E C, and draw the Line B I; then upon the point B deſcribe the occult Arch C n, which being meaſured in the line of Chords, will be found to be 31 ½ or 2 Points three quarters, which is the Courſe required, N. N. W. three quarters North, and the Line B I is the diſtance required, which

being measured upon the Line of Leagues, will be found to be 128 Leagues, the Departure H I 67 Leagues.

Problem. II.

A Ship being in the Latitude 40° North, sailes N. N. W. three quarters of a point, or 7° three quarters North, until she come into the Latitude of 45° 30′; I demand the Distance run, the Difference of Longitude and the Departure?

Fig. 30

In the solution of this *Problem* by the *Plain Scale*, draw the Line A B at any convenient length, and upon C describe the Semi-circle A D B, and find the middle Latitude as before, and set it off from D to M and L, and draw the Line M L, and upon the point B describe the obscure Arch, C n, and set off the Course given (which is 2 points three quarters, or 31° and a quarter) from C to n, and set the distance C F from C to G, and from B set off the Difference of Latitude 110 Leagues; and the same distance from G to A, and from the points H and A, erect the two perpendiculars H I and A K, then through the point N draw the Line B I, which being measured in the Scale of Leagues, will be found to be 128, then laying a Ruler from G to the Intersection of the Lines at E, draw the Line G K, and note where it intersecteth the Line A K, which is at K; so the Distance A K being measured upon the Scale of Leagues, will be found to be 90 Leagues, the Difference of Longitude sought, and H I the Departure 67 Leagues.

Problem. III.

A Ship being in the Latitude of 40° North, sailes between the North and the West, until she arrive to the Latitude 45° 30′, and that her Distance run be 128 Leagues; I demand the Course, difference of Longitude and Departure?

Fig. 30

For the solution of this *Problem*, first draw the Line A C B at any convenient length, and upon C describe the Semi-circle A D B, and set off the middle Latitude as before; and likewise the Distance C F from C to

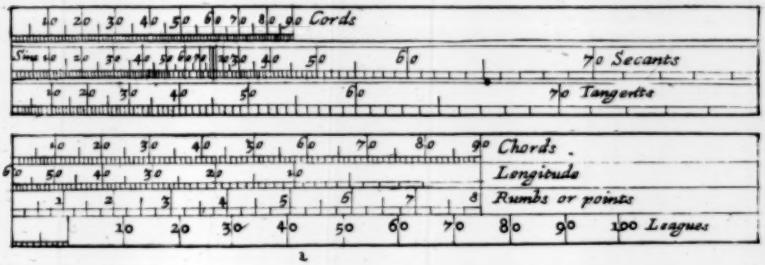
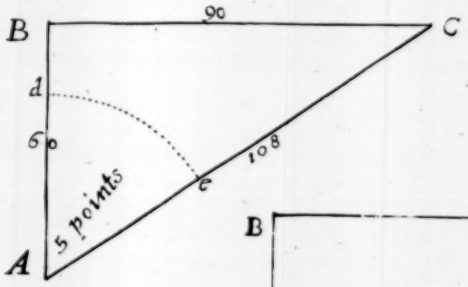


Fig 26



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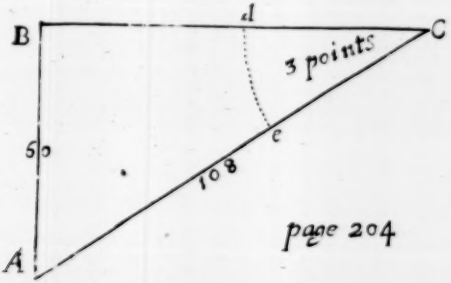

Fig 28

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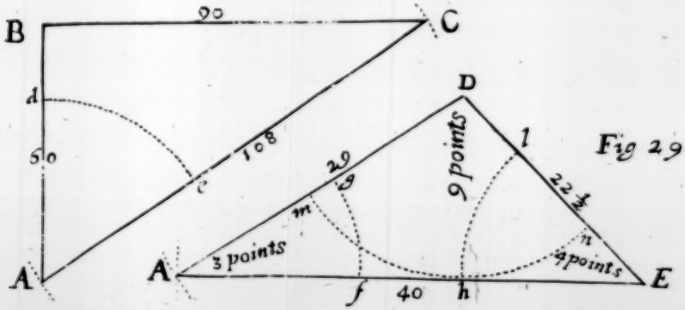


Fig 29

C to G: also the difference of Latitude in Leagues from B to H, and from G to A, then erect the two perpendiculars at H and A, then take the Distance between the Compasses, and set one foot of the Compasses in B, and extend the other foot towards I, until it doth intersect the perpendicular at H in the point I, then laying a Ruler upon the point G, unto the intersection of the Lines at E, draw the Line G K, and note where it doth intersect the perpendicular at A, which will be at K; then the distance K A being measured on the Scale of Leagues, will be found to be 90, the Difference of Longitude sought; then for the finding the Course, with the Radius of your Scale, draw the obscure Arch C n, and where it doth intersect the Line B I, that distance being measured in the Line of Chords, will be found to be 31° and a quarter, or two points three quarters, the Course required, which is N. N. W. three quarters North, and the Departure H I 67 Leagues.

Problem. IV.

A Ship being in the Latitude 40° *North, sailes N. N. W. three quarters* (or 7° $\frac{1}{2}$) N. 128 *Leagues; I demand the Latitude of the second place, the difference of Longitude and Departure?*

Fig. 30

For the solution of this *Problem*, first draw the Line B A of any convenient length, then from one end thereof, as B, describe the occult Arch C n, and set off 31° and a quarter, or two points three quarters from C to n, then by the point n, draw the Line B I, the distance 128 Leagues, and from the end thereof, as at I, let fall the perpendicular I H, then measure the distance H B, which you will find to be 110 Leagues, or 5° 30′, the Latitude of the second place is 45° 30′; then having the two Latitudes, find the middle Latitude, as is before directed; then upon the Line B A and upon the Center C, describe the Semicircle B D A, and drawing the Line D E from the point D, set off the middle Latitude 42° 45′ both wayes, to M and L, and draw the Line M L then take the distance D F in your Compasses, and set it off from B to G, and from H to A, then upon the point A erect an occult perpendicular, as M K, then by the point E, draw the Line G K, till it intersect the perpendicular at K; then draw A K, which being measured in the Line of Leagues, will be found to be 90 Leagues, or 4° 30′, the difference of Longitude, and H I the Departure 67 Leagues.

Prob.

Problem. v.

A Ship being in the Latitude of 40°, ſailes in that Parallel, until her difference of Longitude be ſix degrees; I demand her Diſtance run?

This Queſtion is uſually demonſtrated amongſt the *Problems* of *Mercators* ſailing by a Scheme drawn for that purpoſe, differing from that already deſcribed, but we ſhall here ſhew the way how to reſolve this *Problem* by the Line of Longitude on the Plain Scale.

It is to be underſtood, that, according to the Globe, the Meridians do incline nearer together, until they concur and interſect each other in the Poles, ſo that thereby the degrees of Longitude are not 60 minutes in any Parallel on the North or South ſide of the Æquinoctial; but the nearer to either of the Poles you approach, the more they decreaſe, ſo that in the Latitude of 60 degrees, there are but 30 minutes to one degree of Longitude; and in the Latitude of 84 degrees, there is but 6 minutes, which doth ſhew the errors of the plain Chart; and therefore in Sailing, there ought to be reſpect had to the rectifying thereof according to the Globe, and to that end was this Line of *Longitude* contrived, which is thus to be uſed. If you deſire to know how many minutes there are in a degree of *Longitude* in any *Latitude*,

You muſt extend the Compaſſes from the Center in the *Line* of Chords to the degrees of the *Latitude* of the Place, and the ſame extent will reach from the Center at 60, on the *Line* of *Longitude*, to the number of minutes anſwering to a degree of *Longitude* in that *Latitude*.

Therefore for the ſolution of the fifth *Problem* here propoſed, extend your Compaſſes upon the *Line* of Chords, from the Center to the *Latitude* of the place, which is 40°, and the ſame extent will reach from the Center at 60 in the *Line* of *Longitude*, to 46, which ſhews that 46 minutes makes a degree of *Longitude* in that *Latitude*, which 46 being multiplied by ſix, the degrees of *Longitude*, gives 276 minutes, the Diſtance run, which was required.

Prob.

Problem. VI.

A Ship being in the Latitude of 40 degrees, ſailes in that Parallel 276 minutes; I demand her difference of Longitude?

For the ſolution of this *Problem*, find how many minutes make a degree of *Longitude* in the *Latitude* of 40 degrees (as in the laſt *Problem*) which is 46, therefore if you divide 272 the Diſtance run, by 46 (the miles in a degree of *Longitude* in that *Latitude*) the quotient will be 6 degrees, the difference of *Longitude* required.

Another Way to Work Mercators Sailing by the Plain Scale, by the Meridional Parts.

Problem. I.

A Ship ſailes N. N. W. from the Latitude 40° North, to the Latitude 42° 20′ North; I demand the Diſtance ſailed, the Departure and Difference of Longitude?

Fig. 31

Having the two *Latitudes*, 40° North and 42° 20′ North, find the *Meridional Difference of Latitude* by the Table of *Meridional parts*, which is 186 min. and ſubſtracting one *Latitude* from the other, the Difference is, 2° 20′ or 140 min.

To work this *Problem*, Draw the Line A b B, then place 140 from A to b, and 186 from A to B, raiſe the two occult perpendiculars b c, and B C, ſet off the Courſes two points, and draw the Line A c C, producing it until it cut both the perpendiculars in the Points c and C, and ſo finiſh the two Triangles A b c, and A B C; The Diſtance A c is 151 minutes, the Departure b c 58 minutes, and the Difference of *Longitude* B C 77 minutes.

Prob

Problem. II.

A Ship Sailes from the Latitude 40° N. to the Latitude 42° 20′ N. until her difference of Longitude be 77 minutes Westerly; I demand the Course, Distance and Departure?

Fig. 31

The *Meridional Difference of Latitude* is as in the first *Problem*, 186 minutes, the *Proper difference of Latitude* 140 minutes.

Draw A B 186 minutes, place 140 minutes from A to b, raise the perpendicular B C of his given length, 77 minutes, and also the occult perpendicular b c, by the points A and C draw A C, and finish the two Triangles; the Course, the Angle at A is two points, or N. N. W. the Distance A c 151 minutes, the Departure 58 minutes.

Problem III.

A Ship Sailes Westerly 151 minutes, from the Latitude 40° North, to the Latitude 42° 20′ North; I demand the Course, Departure, and difference of Longitude?

Fig. 31.

The *Meridional Difference of Latitude* is 186 minutes, the *Proper Diff. Lat.* 140 minutes.

Draw A B 186 minutes, and A b 140 minutes as before, and raise the two occult perpendiculars b c and B C, take the Distance 151 min. and placing one point of your Compasses in the point A, cross the occult Line b c, in the point c, and draw A c, producing it until it concur with B C, and finish the Triangles; the Course is two points, or N. N. W. the Departure 58 minutes, the Difference of Longitude 77 minutes.

Problem IV.

A Ship Sailes N. N. W. 151 min. from the Latitude 40° North; I demand the Latitude, Departure and Difference of Longitude?

Fig. 31.

Draw

Draw the occult *Line* A B, and ſet off the the Courſe two points, and the Diſtance A c 151 minutes, let fall the perpendicular b c, and finiſh the Triangle A b c; Then A b will be found 140 minutes or 2° 20′, which makes the other *Latitude* 42° 20′, by which you will find the *Meridional Parts* to be 186 minutes. Place 186 minutes from A to B, and raiſe the occult perpendicular B C until it meet with A c C continued, and ſo finiſh the Triangle A B C; The Departure b c is 58 min. the Difference of *Longitude* B C 77 minutes.

Problems of Great Circle Sailing.

Problem 1.

Two Places both in one Latitude, the Difference of Longitude being given, to find the Courſes and Diſtances from place to place by the arch of a Great Circle.

Example.

Suppoſe the *Lizard* and *Pangam Iſland* on *New-found Land*, both in the *Latitude* 50° North, the *Difference of Longitude* between them 47°; I demand the *Courſes* and *Diſtances* from place to place.

Fig. 32.

Draw the *Line* A E, and place the *Tangent Complement* of 50° the *Latitude*, from A to B; with 60° of the Chords ſweep the Arch D E, and ſet off 47°, the *Difference of Longitude* from D to E; and draw the *Line* A D, and place the Tangent 40°, the *Complement of the Latitude*, from A to C, then draw the *Line* B C upon the Arch D E, ſet off every 5° degrees from E to D, and draw the prick'd *Lines*, A b, A c, A d, *&c.* and where theſe *Lines* Interſect B C, place the *Letters* b, c, d, f, g, *&c.* the Diſtances A b, A c, A d, *&c.* being meaſured on the *Line* of *Tangents*, are *Tangents Complement* of the *Latitude*, as follow-eth.

Compl. Lat.		*The Latitudes.*	
A b	39	Therefore the *Latit.* are,	51
A e	38 ½		51 ½
A d	38		52
A f	37 ½		52 ½
A g	37 ½		52 ½
A n	37 ¼		52 ¼
A o	38		52
A u	38 ¼		51 ¼
A i	39 ½		50 ½

These are the *Latitudes* by which the Arch passes, at every 5° of *Longitude* from B, representing the *Lizard*, to C which represents the *Island*. Having these *Latitudes* and *Longitudes*, you may find the *Course* and *Distance* according to *Mercators Sailing*.

A c is the *Tangent Compl.* of the greatest *Latitude* by which the Arch passes, 52° ½.

So the *Latitudes* and *Longitudes* of the several Points, b, e, d, &c. are as followes, likewise the *Courses* and *Distances* from place to place.

	Lon.	*Lat.*	*Places.*	*Courses.*	*Dist.*
B	00°	50°	From B to b	W. N. W. ½ W.	198′
b	05	51	From b to e	W. by N.	195
e	10	51 ½	From e to d	W. by N. ¼ W.	182
d	15	52	From d to f	W. by N. ½ W.	180
f	20	52 ½	From f to g	Almost W.	196
g	25	52 ½	From g to n	W. by S. ¾ W.	176
n	30	52 ¼	From n to o	W. by S. ½ W.	193
o	35	52	From o to u	W. by S.	186
u	40	51 ½	From u to i	W. S. W. ¼ W.	196
i	45	50 ½	From i to C	W. S. W. ¼ W.	81
C	47	50			

Problem II.

Two Places differing both in Latitude and Longitude, to find the Courſes and Diſtances from place to place.

Example.

Suppoſe the two places to be *Trinity Harbour* in *Virginia*, in the Latitude 36° North, and the *Lizard* in the Latitude 50° North, the Difference of Longitude between them 68 degrees; I demand by what Latitudes and Longitudes the Arch paſſes, and likewiſe the Courſes and Diſtances from place to place?

Fig. 33.

Draw the Line A F, place the *Tangent* of 40° the *Complement* of the *Lizard's* Latitude from A to C; with 60° of the Chords deſcribe the Arch E F, placing 68 degrees from F to E, drawing the Line A E; then place the *Tangent* 54 degrees the *Complement* of *Trinity Harbour's* Latitude from A to B, and draw B C, letting fall the perpendicular A d; then ſet off every 5 degrees from E towards F (becauſe we Sail from B) draw the prick't Lines, A 1, A 2, *&c.* the Diſtance A 1, A 2, A 3, *&c.* meaſured on the Line of *Tangents* gives the *Complements* of the Latitudes by which the Arch paſſes, at every 5 degrees difference of Longitude from B, repreſenting *Trinity Harbour*, towards C which is the *Lizard*.

The Distances, A 1, A 2, A 3, &c, are as followes.

Dist.	Deg.
A 1	50 ¾
A 2	48 ½
A 3	46 ¼
A 4	44 ¼
A 5	42 ¾
A 6	41 ¾
A 7	40 ¾
A 8	40
A 9	39 ½
A 10	39 ¼
A 11	39
A 12	39 ¼
A 13	39 ½

Therefore the Latitudes and Longitudes by which the Arch passes are as follows.

	Long.	Lat.
B	00	36
1	05	39 ¼
2	10	41 ¼
3	15	43 ¼
4	20	45 ¼
5	25	47 ¼
6	30	48 ¾
7	35	49 ¾
8	40	50
9	45	50 ¼
10	50	50 ¼
11	55	51
12	60	50 ½
13	65	50 ½
C	68	50

Having the Latitudes *and* Longitudes *by which the Arch passes, you may find the* Courses *and* Distances *from Place to place, by* Mercators Sailing, *as in the Problem afore-going.*

The Courſes and Diſtances from place to place, wrought by Mercator, *are as follows in the Table.*

Places.	*Courſes.*	*Diſtances.*
From B to 1	N. E. ½ E.	298′
From 1 to 2	N. E. by E.	282
From 2 to 3	N. E. by E. ½ E.	256
From 3 to 4	N. E. by E. ½ E.	241
From 4 to 5	E. N. E.	226
From 5 to 6	E. N. E. ¼ E.	215
From 6 to 7	E. N. E. ½ E.	206
From 7 to 8	E. by N.	200
From 8 to 9	E. by N. ¼ E.	191
From 9 to 10	E. by N. ½ E.	189
From 10 to 11	E. ſomewhat N.	177
From 11 to 12	E. by S. ¼ E.	188
From 12 to 13	E. by S. ½ E.	189
From 13 to C	E. by S. ¼ E.	117

Astronomical Problems Wrought by the Plain Scale.

Problem I.

The Suns Place or Distance from the next Equinoctial Point, and the greatest Declination being given, to find the present Declination.

Example.

The Suns Place is 26 degrees ½ of *Taurus*, that is 56 deg. ½ from the *Equinoctial* point *Aries*; I demand his Declination?

Fig. 34

With the Chord of 60 degrees describe the Semi-circle B D C, and raise the perpendicular A D, and from the point C, set off the greatest Declination 23 deg. ½, from C to E, and draw the Line A E; then for the Suns Longitude, set off the Sine 56 deg. ½ upon the Line A E, from A to F, then from the point F, take the nearest distance F I to the Line A C, which measured on the Line of Sines is 19 deg. ½; or else through the point F, draw G H, paralled to B A C; then A G measured on the Sines, or C H on the Chords, give 19 deg. ½, the Suns present Declination Northerly.

Problem II.

The Suns greatest and present Declination being given; to find his Place or Longitude.

Example.

May the 7th 1672, the Suns Declination is 19 degrees ½ North, the greatest Declination (as before) 23 degrees ½; I demand the Suns true place?

Fig. 34

Draw B C and describe the Semi-circle B D C, raise the perpendicular A D, and draw the Line A E, as in the former *Problem*, place the Suns Declination 19 deg. ½ from B and C to H and K; draw the Line H K, which

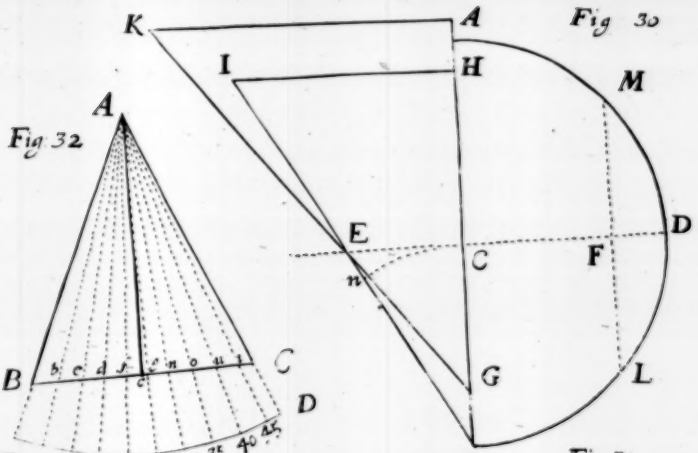
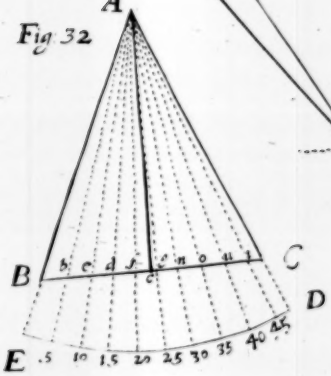


Fig 30



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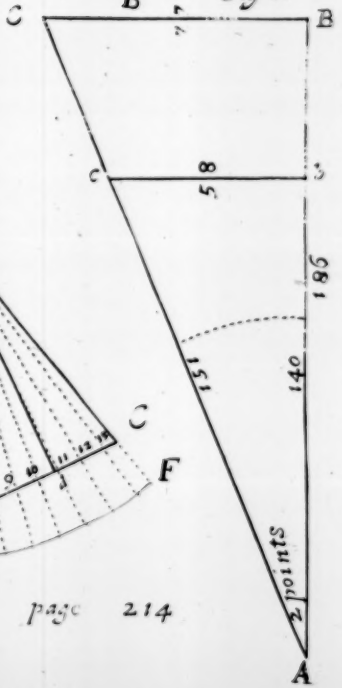


Fig 31

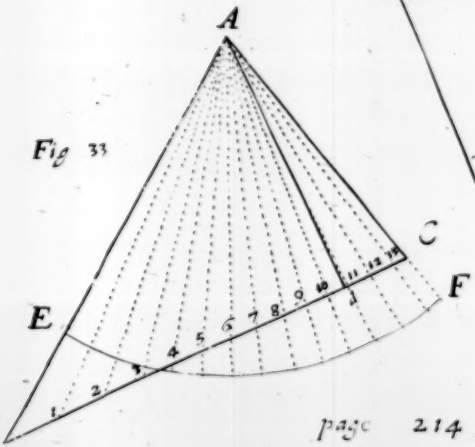


Fig 33

which interſects A E in the point F; the Diſtance A F is a Sine 56 deg. ½, the Suns Diſtance from *Aries*; ſo that the Suns Longitude is 26 degrees and three quarters of *Taurus*.

Problem III.

The Suns Place and greateſt Declination being given; to find his Right Aſcenſion.

Example.

The Suns place is 26 ¾ of *Taurus*, the greateſt Declination as before; I demand his *Right Aſcenſion*?

Fig. 34

Deſcribe the Semi-circle, draw A D and A E as before, place the Sine 56° ½, the Suns Diſtance from *Aries*, from A to F; through the point F draw the Parallel H K, then is F G the Sine of *Right Aſcenſion*, G H being Radius, which you may meaſure after this manner: Place the Diſtance H G from A to o, upon o as a Center, with the Diſtance F G, deſcribe the occult Arch at M, a Ruler laid from A until it touch the Arch, will cut the Semicircle B D C in the point N, the Arch C n is the meaſure of F G, 54° ½, the *Right Aſcenſion*.

Problem. IV.

The Suns Declination given (the greateſt declination being known) to find the Right Aſcenſion.

Example.

May the 7th 1672, the *Suns Declination* is 19° ½ North; I demand *Right Aſcenſion*?

Fig. 34

Deſcribe the Semi-circle B D C, and draw the Line A D and A E as before, place the Declination 19° ½ from B and C to H and K, drawing H K; F G being meaſured as in the third *Problem* gives the *Right Aſcenſion* (as before) 54° ½.

Prob.

Problem. V.

The Latitude of the Place and the Suns Declination being given, to find his Amplitude?

Example.

July 23 1671, in the Latitude 51° ¼ North the *Suns Declination* was 17° ¼ North; I demand the *Suns Amplitude?*

Fig. 35

Draw B A C, and the Semi-circle B Z C, the perpendicular A Z, place the Latitude or heigth of the Pole 51° ¼ from B to P, and draw A P, set off the *Complement* of the *Latitude* 38 ¾ from C to Q, and draw A Q the Equinoctial; place the Chord of the Declination 17° ¼ from Q to D, and the Sine thereof from A to G, and draw the parallel of *Declination* A F; A F measured on the Line of Sines is 29° ½, the *Amplitude* required.

Problem. VI.

The Latitude of the Place and the Suns Declination being given, to find the Ascensional Difference.

Example.

July 23 1671, in the Latitude 51° ¼ North, the *Suns Declination* 17° ¼ North; I demand the *Ascentional Difference?*

Fig. 35

Describe the Semi-circle B Z C, and draw the Line A Z, A P, A Q, and D F as in the 5th *Problem*; F G is the Sine of the *Ascentional Difference* to the Radius D G, which is thus measured, place D G from A to o, upon o, as a Center, with the Distance F G, describe the Arch at E, a Ruler laid from A until it touch the Arch gives the point I; and B I 23 ½ is the measure of the *Ascentional Difference.*

What the *Ascentional difference* is, and the Use of it, may be seen *Prob.* 5, 6, 7, and *Chap.* 7.

Prob.

Problem. VII.

The Latitude of the Place, and the Suns Declination being given, to find when he ſhall be due East or Weſt.

Example.

In the Latitude 51 deg ½ North, the *Suns Declination* is 17 *degrees* ½ North; I demand at what time he ſhall be due *East* or *Weſt*?

Fig. 36

Deſcribe the Semi-circle B Z C, and draw the Line A Z, A P, A Q, and D O as before; E O is the Sine of the time from 6, that the Sun is *East* or *Weſt* to the *Radius* D O; which to meaſure, place D O from A to a, and upon the Center a, with the Diſtance E O deſcribe the Arch at g, a Ruler from A until it touch the Arch, gives the point L, and B L 14 deg. ¼ is the meaſure of E O, which reduced to time (*Vide Probl. 7. Chap.* 7.) makes 59 minutes: which ſhews that the Sun is due *East* at 59 min. paſt ſix in the Morning, and due *Weſt* at one minute paſt five, or 59 min. before ſix at Night.

Problem. VIII.

The Latitude of the Place and the Suns Declination being given, to find the Altitude of the Sun being due East or Weſt.

Example.

In the Latitude 51 deg. ½ North, the *Suns Declination* 17 deg. ½; I demand the *Suns Altitude* being due *East* or *Weſt*?

Fig. 36.

Deſcribe the Semi-circle B Z C, and draw the Line A Z, A P, Q A and D O as before; A L being meaſured on the Line of Sines is 23° *fere*, the *Suns Altitude* being due *East* or *Weſt*.

Problem. IX.

The Latitude of the Place and the Suns Declination given, to find the Suns Altitude at ſix.

Example.

In the Latitude 51 deg. ½ North, the *Suns Declination being* 17° ½ North; I demand his *Altitude* at ſix?

Fig. 36.

Deſcribe the Semi-circle B Z C, draw the Lines A Z, A Q and D O, and through the Point O, draw the Line L o b; B L or C b meaſured on the Chords, or A I on the Sines, gives 13 degrees ½, the *Altitude* of the *Sun* at ſix.

Problem. X.

The Latitude of the Place and the Suns Declination given, to find the Suns Azimuth at ſix.

Example.

In the Latitude of 51 deg. ½ North, the *Suns Declination* 17 deg. ¼ North; I demand the Suns *Azimuth at ſix?*

Fig. 36.

Deſcribe the Semi-circle, B Z C, and draw the Lines A Z, A P, A Q and D O as before; draw, L o b as in the 9th *Problem*; I o is the Sine of the Suns *Azimuth* to the *Radius* I L, which is thus meaſured; place L I from A to e, with the Diſtance I o upon the Center e deſcribe the occult Arch at d: a Ruler laid to touch the Arch, gives the point b, and C b meaſured is 11 deg. ½, the *Azimuth* from the *Eaſt* or *Weſt*; So that the Sun is E. by N. at 6 in the *Morning*, and W. by N. at 6 at *Night*.

Problem. XI.

The Latitude of the place, the Suns Declination and Altitude given, to find the Suns Azimuth.

Example.

Example.

In the *Forenoon*, in the Latit. 51 deg. ½ North, the Suns *Declination* is 20 deg. ¼ N°. and his *Altitude* 43 deg. I demand his *Azimuth*?

Fig. 37.

Deſcribe the Semi-circle B Z C, and draw the Lines A Z, A P, A Q and D F, the parallel of *Declination* as in the fromer *Problems*, place the *Altitude* 43 deg. from B and C to d and e, and draw the parallel d e, which interſects the Parallel D F in the point G; I G is the Sine of the Suns *Azimuth* from the *Eaſt* towards the *South*, I d being the Radius; which to meaſure, place I d from A to C, and thereon with the Diſtance I G deſcribe the Arch at f, a Ruler laid from A to touch the Arch gives the point h, B h 24 deg. ¼ is the meaſure of I G, *Eaſt Southerly*, So that the Suns *Azimuth* is S. E. 65 deg. ¼.

Problem XII.

The Latitude of the Place, the Suns Declination and Altitude being given, to find the hour from Noon.

Example.

In the *Afternoon*, in the Latitude 51 deg. ½ North, the *Suns Declination* is 20 deg. ¼, the *Altitude* 43 deg. I demand the *Hour*?

Fig. 37

Deſcribe the Semi-circle B Z C, and draw the Lines A Z, A P, A Q D F, and d e, as in the 11 *Problem*; F G is the Sine of the hour from ſix, which to meaſure place D F from A to u, and thereon with the Diſtance F G, ſweep the Arch at K; a Ruler laid to touch the Arch gives the point o, and C o is the meaſure of F G, 45 deg. which reduced into time gives 3 *Hours*, the time *Afternoon*.

SECT. II.

The Use of Gunters Scale.

I Shall not say any thing of the description of this Scale, nor of the Projection of the Lines thereon, being the *Logarithms* of Numbers, Sines, Tangents, *&c.* placed upon a Scale. This is sufficiently explained by Mr. *Gunter*, Mr. *Wingate* and others.

To find a whole Number on the Line of Numbers.

Among the figured Divisions look for the first figure of your Number, then for the second figure, count so many tenths from the long divisions, on towards the end of the Rule, as the Unites in the second figure amount to; then for the third figure, count from the last tenth so many Contesms as the figure hath unites; and so likewise for the fourth figure, count from the last Contesm so many milions (or thoulands) as the same fourth figure contains unites; this done, that shall be the point where the number propounded is represented on the Line of Numbers.

The Number given being 12, *to find the Point on the Line of Numbers that doth represent the same.*

Therefore according to the Rule, 1 being the first figure of this Number, I take the division at the figure 1 (in the middle of the Line) for the first figure; then the second figure being 2, I count two tenths from that 1, and that is the Point representing 12, where commonly there is a small brass Center, because it's often in use.

Suppose the point representing 144 *were required to be found upon the Line of Numbers.*

For the first figure in the Number being 1, I take (as before) the middle 1; then for the second figure, which is 4, I count 4 tenths onwards,

Fig 34

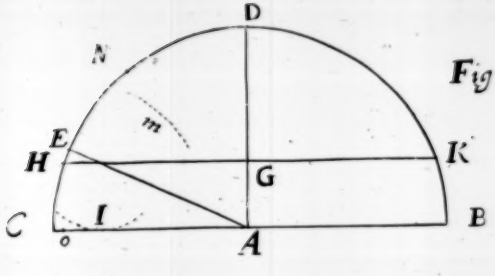


Fig 35

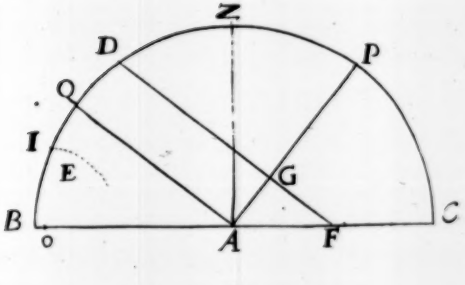


Fig 36

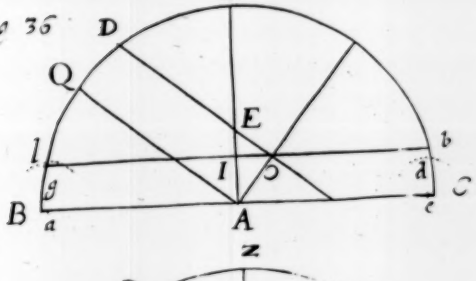
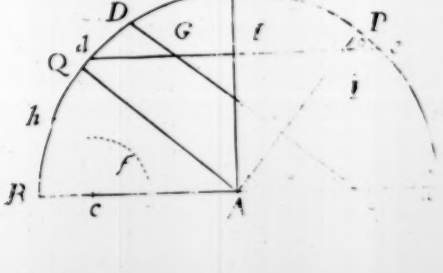


Fig 37



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wards, and from that tenth, I count 4 Centesms, or hundred parts further, and that is the point representing 144.

To find the point representing 1728, first (as before) for a thousand, I take the 1 in the middle of the Line; secondly, for the second figure being 7, I reckon seven tenths onwards, and that is 700; thirdly, for the third figure, being 2, I reckon 2 Centesms from the 7 tenths, which representeth twenty; and then lastly, for 8 you may reasonably estimate 8 millions, or thousand parts from the last Centesm, and that point last found, will be the point representing the number 1718.

To find a Fraction, or broken Number, on the Line of Numbers.

The Fractions that are to be found on the Line of Numbers, ought alwayes to be Decimal Fractions, $\frac{1}{10}$, $\frac{1}{100}$, $\frac{1}{1000}$, (or 1, 01, 001) either inches, feet, yards, pearches, or the like; also in weight or time, or any other denomination, all other Fractions must be reduced into Decimals; and being thus considered, they are expressed as whole Numbers upon the Line.

Note, If you call 1 at the beginning of the Line, one tenth of any integer, then 2 following must be two tenths; 3, three tenths, *&c.* and the 1 in the middle, one Integer; 2, two Integers, *&c.* and 10 at the end must be ten Integers.

But if 1 at the beginning be one Integer, then 1 in the middle must be ten Integers, and ten at the further end 100 Integers; and all the intermediate figures, 20, 30, 40, 50, 60, 70, 80, 90, so many Integers; and every longest division between, as 21, 22, 23, 24, 25, 26, *&c.* single Integers; and the shortest of those divisions, tenths of those Integers; and so in proportion infinitely, as $\frac{1}{10}$, 1, 10. 1, 10, 100. 10, 100, 1000. 100, 1000, 10000, *&c.*

Problem. 1.

Two Numbers being given, to find a third Geometrical proportional unto them; and to a third a fourth, and to a fourth a fifth, &c.

Example.

Example.

Let the two Numbers given be 2 and 4, unto which it is required to find a third proportional, *&c.* Therefore for the performance hereof by the Line of Numbers, extend the Compasses from one of the Numbers given to the other; this done, if you apply the same extent either upwards or downwards from either of the Numbers propounded, the movable point of the Compasses will fall upon the third proportional required; and so the same extent being applyed the same way, from the third, the movable point of the Compasses will fall upon the 4th proportional, and from the 4th to a 5th, *&c.* and so to more, as you please; for if you extend the Compasses from 2 to 4, and turn the Compasses upwards, with one point resting on 4, the movable point will fall on 8, the third proportional, and from 8 to 16, from 16 to 32, from 32 to 64, and so forward.

Problem. II.

One number being given to be multiplied by another number, to find the Product.

To resolve this Question Arithmetically whether by natural or artificial numbers, the proportion is; As 1 is to the Multiplicand, so is the Multiplicator to the Product.

Example.

Let the Multiplicand 8 be multiplyed by 5 the Multiplicator, extend the Compasses on the Line of Numbers, from 1 to the Multiplicand; the same extent being applyed the same way from the Multiplicator, will cause the movable point to fall on the Product: for if you extend the Compasses from 1 to 8, the same extent the same way will reach from 5 to 40: and so if you would now multiply any Number by 8, as the Compasses now stand, it is but placing one foot in any number given, and the movable point will fall on the Product; as if you place one foot in 9, the the other will fall in 72, and so from 8, it will fall in 64, and from 7 to 56, and from 6 to 48, so that the Table of Multiplication may by this be easily made; the extent of the Compasses may be taken from 10, at the further end of the Line, which you may call 1.

Problem. III.

One number being given to be divided by another number, to find the Quotient.

For the reſolution of this Problem, the Proportion is thus; As the Diviſor is to 1, ſo is the Dividend to the Quotient.

Example.

Let 40 be the Dividend, and let the Diviſor be 8; therefore extend the Compaſſes on the Line of Numbers from the Diviſor to 1; this done, the ſame extent the ſame way, ſhall reach from the Dividend to the Quotient, which is 5.

Another Example.

Let 750 be a number given, to be divided by 25; therefore extend the Compaſſes downwards from 25 to 1, then applying that extent the ſame way from 750, the movable point will fall upon 30, which is the Quotient required.

Now to know of how many Figures any Quotient ought to conſiſt.

It will be neceſſary to obſerve how many times the Diviſor may be written under the Dividend, according to the Rules of Diviſion, for of ſo many Figures ſhall the Quotient be compoſed.

For Example, 12231 being given to be divided by 27, which ſaid number may be written according to the Rules of Diviſion, three times under the Dividend; therefore the Quotient ſhall conſiſt of three figures, and ſo of any other.

Problem IV.

To three Numbers given, to find a fourth in a direct proportion, as in the Rule of Three direct.

To reſolve this *Problem*, the proportion is thus; As the firſt Number given is to the ſecond, ſo is the third number to the fourth.

To perform this on the Line of Numbers, you muſt extend the Compaſſes from the firſt number or tearm given, unto the ſecond; which done, that extent being applied the ſame way from the third tearm, will cauſe the movable point to fall on the fourth tearm required.

Example.

Example.

If the circumference of a Circle, whose diameter is 7 inches, be 22 inches; what circumference will a Circle have, whose diameter is 14 inches?

Therefore extend the Compasses in the Line of Numbers from 7, in the first part thereof, unto 14 in the second; this done, the same extent being applied the same way from 22, will make the movable point to fall upon 44 inches the circumference required.

Example 2.

Let the Circumference of a Circle be 22 Inches, and the Diameter thereof 7 inches, how much shall the Diameter of a Circle be, whose circumference is 44 inches?

Extend the Compasses downwards, from 22 in the second part of the Line, to 7 in the first; which done, that extent being applied the same way from 44, will reach to 14 the diameter sought.

Problem. V.

Three numbers given, to find a fourth in an inversed proportion, (or in the backer Rule of Three.)

To resolve this Problem, the proportion is: As the third number is to the second, so is the first to the fourth.

Example.

If 60 men make a Trench in 45 hours, in what time will 40 men make such another?

To perform this by the Line of Numbers, extend the Compasses from the first of the Numbers given to the second, having both the same denomination; this done, if this extent be applyed backward from the third number, the movable point will fall upon the fourth number required; so that if you extend the Compasses from 60 to 40 (those tearms being of the same denomination) *viz.* of men; this done, the extent

extent being applyed backward from 45, will reach to 67, 5, the fourth number you look for. I conclude therefore, that 40 men will perform as much in 67 hours and an half, as 60 men will do in 45 hours.

Problem. VI.

To three numbers given, to find a fourth in a doubled or duplicate proportion.

The uſe of chis *Problem* appears chiefly in proportions of Lines to Superficies, or of Superficies to Lines; Now if the denomination of the firſt and ſecond tearms be of Lines, then extend the Compaſſes from the firſt tearm to the ſecond, (of the ſame denomination) this done, that extent being applyed twice, the ſame way from the third tearm, the movable point will ſtay upon the fourth tearm required.

Example 1.

If the content of a Circle, whoſe Diameter is 14 Inches, be 154 inches, what will the content of a Circle be whoſe diameter is 28 inches?

Here 14 and 28 having the ſame denomination, *viz.* of Lines, I extend the Compaſſes from 14 to 28; then applying that extent the ſame way from 154 twice, the movable point will fall on 615, the fourth proportional ſought, that is firſt from 154 to 308, and from 308 to 616.

But if the two firſt tearms have the denomination of Area's, or Contents, and the Queſitum be a Line, then extend the Compaſſes upon the Line of Numbers, unto half the diſtance between the firſt and ſecond tearm of the ſame denomination; ſo the ſame extent will reach from the third tearm given, to the fourth required.

Example 2.

If the diameter of a Circle, whoſe Area is 154 inches, be 14 inches, what diameter will a Circle have whoſe Area is 616 inches?

Divide the diſtance betwixt 154 and 616 into two equal parts, then ſet one foot in 14, the other ſhall reach to 28, the diameter required.

Problem VII.

Three numbers being given, to find a fourth in a triplicate proportion.

The use of this *Problem*, consisteth in the proportion of Lines, Solids, *& contra.*

If therefore the first and second tearms have the denomination of Lines, (as the diameters of Circles, or the sides of solid bodies) extend the Compasses upon the Line of Numbers, from the first tearm to the second; this done, and that extent applyed three times the same way from the other tearm, will cause the movable point to fall upon the fourth tearm required.

Example 1.

If an Iron Bullet, whose diameter is 4 inches, weigheth 9 pounds, what is the weight of another Iron Bullet whose diameter is eight inches?

Therefore extend the Compasses on the Line of Numbers from 4 to 8; which done, and that extent applied the same way three times from 9, the moveable point will first fall upon 18, then from 18 to 36, and lastly from 36 to 72, the weight required.

But if two given tearms be weight or contents of Solids, and the diameter or side of a Square or Line is sought, then divide the space between the two given tearms of the same denomination into three parts, and that distance shall reach from the third to the fourth proportional.

Example 2.

If an Iron Bullet that weigheth 9 pound be 4 inches diameter, what diameter shall the shot of Iron be, whose weight is 72?

Divide the space between 9 and 72 in 3 parts, and that third part shall reach from 4 to 8, the diameter required.

Example 3.

Also if a Cube whose side is 6 Inches, contain 216 inches, how many inches shall a Cube contain whose side is 12 inches?

To perform this Proposition, extend the Compasses upon the Line of Numbers

Numbers from 6 to 12; that extent measured upon the Line of Numbers three times, shall at last fall on 1728.

Problem VIII.

To find the square Root of any number under 1000000.

The square root of any number, is alwayes the mean proportional betwixt 1, and the number propounded; but yet with this general caution, *viz.* if the figures of the number be even, that is, 2, 4, 6, 8, 10, *&c.* then you must look for the unite, or one, at the beginning of the Line of numbers, and the number given in the second part, and the Root in the first part; or rather reckon 10 at the end to be the unite, and then both Root and Square will fall backwards towards the middle, in the second part of the Line; but if they be odd, then the middle one will be best to be counted the unite, and both Root and Square will be found from thence forward towards 10; so that according to this Rule, the Square of 9 will be found to be 3; the square of 64, will be 8; the square of 144 will be 12; the square 1444 to be 38; the square of 57600 to be 240; the square of 972196, will be found to be 986. And to know how many figures any Root ought to consist of, put a prick under the first figure, the third, the fifth and the seventh, *&c.* beginning from the right hand, and as many pricks as are noted, so many figures there must be in the Root.

Problem. IX.

To find the Cubique Root of a Number under 1000000000.

The Cubique Root is alwayes the first of two mean proportionals, between 1 and the number given, and therefore will be found, by dividing the space between them into three equal parts. And to find how many figures will be in this Root, you must prick under the first figure, the fourth, seventh, tenth, beginning at the right hand; and so many pricks as you find, so many figures must be in the Root, which Root may be easily found, with these cautions.

1. If the last prick fall on the last figure towards the left hand, then the Unite is best placed at 1 in the middle of the Line, and then the

Cube and Root will both fall forward toward 10 at the end of the Line.

2 If the last prick fall on the last figure but one towards the left hand, you may place the unite at 1 in the beginning of the Line, then will the Cube and Root both fall in the second part of the Line between 1 in the middle, and ten at the end of the Line.

If the last prick fall on the last figure but two, then alwayes place the unite at 1 at the end of the Line, and then the Cube and Root will both fall backward, and be found in the second part of the Line of Numbers.

These Notes being observed, the Cube Root of 1728, will be found to be 12; and the Cube Root of 17576, will be 26; and the Cube Root of 438976, will be found 76; and the Cube Root of 8120601, will be 101; the Cube Root of 11390625, will be 225; and lastly, of 513922402, will be found to be 801.

Problem. X.

How to work a proportion in Sines alone; or, three Sines being given, to find a fourth proportional.

Example.

As Sine 22° 45′, to Sine 47° 30′, So is Sine 23° 15′ to a fourth Sine required.

This *Problem* is wrought on the Line of Sines, as the 4th *Problem* is on the Line of Numbers. Take the extent from the Sine 22° 45′ on the Line of Sines, to the Sine of 47° 30′; the same extent shall reach the same way, from the Sine of 23° 15′ to the Sine 48° 50′, the fourth Sine required.

Problem XI.

How to work a proportion in Tangents alone; or, three Tangents being given, to find a fourth proportional.

Example 1.

As Tangent 42° 40′, to Tangent 15° 20′, So is Tangent 39° 08′ to the fourth Tangent required.

This

This *Problem* is wrought on the Line of Tangents, as the former *Problem* on the Line of Sines.

Extend the Compasses on the Line of Tangents, from the Tangent 42° 40′ to the Tangent 15° 20′; the same extent shall reach the same way, from the Tangent 39° 08′ to the Tangent 13° 36′ required.

Example 2.

As Tangent 14° 58′, to Tangent 39° 15′; So is Tangent 47° 18′ to a fourth Tangent required.

On the Line of Tangents, the Tangents above 45° encrease from 45° to 46°, 47° to 50°, 60°, &c. backwards towards the beginning of the Line: therefore in working this proportion, the same extent that reaches from 14° 58′ to 39° 15′, shall reach the contrary way from 47° 18′ to 73° 11′, the fourth Tangent required.

Example 3.

As Tangent 21° 30′, to Tangent 37° 20′; So is Tangent 42° 40′, to a fourth Tangent required.

The extent from the Tangent 21 deg. 30 min. to the Tangent 37 deg. 20 min. if applyed the same way, from Tangent 42 deg. 40 min. will fall beyond 45 deg. at the end of the Line; therefore to remedy this inconveniency, having the distance between Tangent 21 deg. 30 min. and Tang. 37 deg. 20 min. place one point of your Compasses in the Tangent 45 deg. and let the other point fall backwards towards the beginning of the Line, and it will rest on the Tangent 27 deg. 20 min. This point let remain fixed, and close the other point which stands in 45 deg. to the Tangent 42 deg. 40 min. then keeping this distance, place one point in Tangent 45 deg. the other will fall upon the Tangent 60 deg. 45 min. required.

Problem. XII.

How to work a proportion in Sines and Tangents together.

Example

Example 1.

As Sine 22 deg. 30 min. to Sine 37 deg. 10 min. So is Tangent 19 deg. 40 min. to a fourth Tangent required.

The extent on the Line of Sines from 22 deg. 30 min. to 37 deg. 10 min. ſhall reach on the Tangents from 19 deg. 40 min. to 29 deg. 25 min. required.

Example 2.

As Tang. Compl. 60 deg. 15 min. to Sine 56 deg. 45 min. So is Radius, to a Tangent required.

Becauſe there is a Tangent in the firſt place of the proportion, and likewiſe a Tangent in the fourth, therefore this proportion muſt be changed, by putting Radius in the firſt place; and inſtead of the Tang. Compl. in the firſt place, take Tangent 60 deg. 15 min. (if it had been a Tangent, you muſt have taken the Tang. Compl.) and then the proportion will remain thus:

As Radius, to Sine 56 deg. 45 min. So is Tangent 60 deg. 15 min. to the Tangent required.

The extent from Radius, Sine 90 deg. to the Sine 56 deg. 45 min, on the Sines, ſhall reach from Tangent 60 deg. 15 min. to Tangent 55 deg. 40 min. required.

Example 3.

As Radius to Tangent Compl. 60 deg. 15 min. So is Tangent 55 deg. 40 min. to a Sine required.

This proportion muſt be changed, becauſe there is Radius or Sine 90 deg. in the firſt place, and a Sine required. Inſtead of the Tang. Compl. 60 deg. 15 min. take the Tangent 60 deg. 15 min. and put Radius in third place, and ſo the proportion follows.

As Tangent 60′ 15″, to Tangent 55 deg. 40 min. So is Radius to the Sine ſought. Therefore the extent from the Tangent 60 deg. 15 min. to Tang. 55 deg. 40 min. ſhall reach from Radius or Sine 90 deg. to Sine 56 deg. 45 min. required.

Probl.

Problem XIII.

How to work Numbers and Sines together.

Example.

As 56, to 106; So is Sine 29 deg. 30 min. to a Sine required.

Extend the Compaſſes on the Line of Numbers, from 56 to 106, the ſame extent ſhall reach the ſame way on the Line of Sines, from 29 deg. 30 min. to 68 deg. 50 min. required.

Problem. XIV.

How to work by Numbers and Tangents together.

Example.

As 202, to 52; So is Tangent 73° 52′, to a Tangent required.

The Extent on the Line of Numbers, from 202 to 52, ſhould reach the ſame way on the Line of Tangents from 73 deg. 52 min. to the Tangent required; but the Compaſſes ſo extended fall beyond the end of the Line, therefore this defect muſt be remedied, as in the third *Example, Problem* 12, by placing the ſaid extent in Tangent 45 deg. and letting the other point fall backwards in the Line; which being fixed, cloſe the other point to 73 deg. 52 min. and then placing your Compaſſes again in 45 deg. the movable point ſhall fall on 41 deg. 37 min. the Tangent required.

SECT. III.

The Description and Use of the Sinical Quadrant.

THIS Instrument is commonly made of Brass, Box, or Pear-tree, being a Quadrant, or fourth part of a Circle; the Limb thereof being divided into 90, equal parts or degrees, is numbred with 10, 20, 30, 40, *&c.* unto 90; and also is divided into 8 equal parts, which are the Points of the Compass, and doth represent any of them, according as the nature of the Question requireth.

The two sides thereof are commonly divided into 60 (or sometimes into 100) equal parts, and numbred from the Center with 10, 20, 30, *&c.*

Likewise there is an Index that moveth upon the Center of the Quadrant, and reacheth without the Limb, alwayes divided with the same equal parts as the sides, and numbred as before.

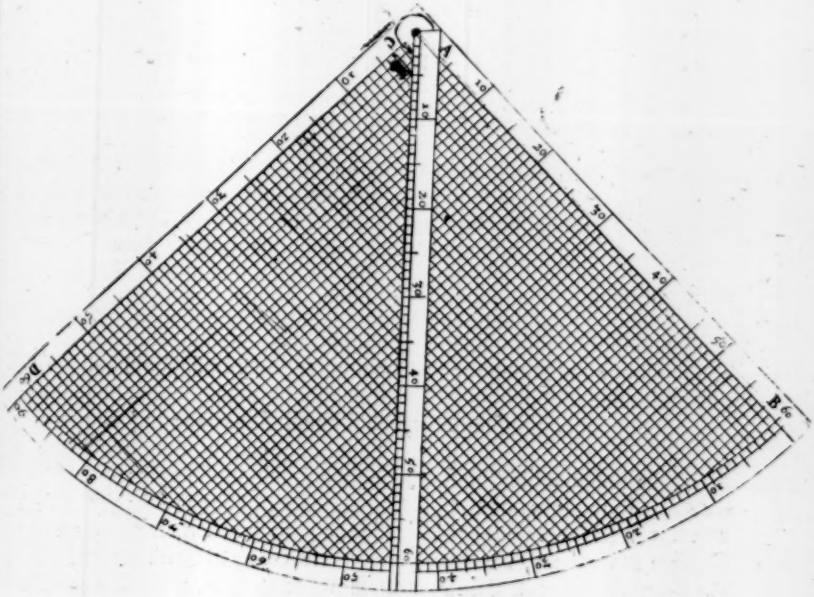
And from those equal parts on the sides, are drawn Parallels throughout the whole superficies of the Quadrant, crossing one another at right Angles.

And the Lines of the fives and tens, are commonly prickt for distinction sake; which said Lines and Parallels do represent the Sines, and Sine Comp. of any Arch, (divided into equal parts) [which I suppose is the reason why it is called a *Sinical Quadrant.*]

But here note, that these Parallels that proceed from the side A B, (in the figure of the *Sinical Quadrant*) are for distinction called *Sinical Parallels*, and those Parallels that proceed from the side C D, are called *Co-Sinical Parallels.*

Now these distinctions being observed, we shall proceed to the Use, in the Solutions of several Problems in Navigation, and in working a Traverse at Sea, *&c.*

The Figure of the Sinical Quadrant.



The Use of the Sinical Quadrant.

Problem 1.

The Course and distance being given, to find the difference of Latitude, and the Departure from the Meridian.

Course the fifth Rhomb, distant 45 Leagues.

Therefore first put the Index to the fifth Rhomb, which being done, find the *Distance* given thereon, which is 45 Leagues; and in the *Sinical Parallels*, you will find the Index to cut 25 Leagues, which is the

Departure; and in the *Co-Sinical Parallels* it will cut 37 ½, which is the difference of Latitude.

Problem. II.

Course and difference of Latitude being given, to find the distance run, and departure from the Meridian.

Course the fifth Rhomb, difference of Latitude 25 Leagues.

Set the Index to the Course, and find the Difference of Latitude in the *Co-sinical Parallels*, and where that doth intersect on the Index, is 45, which is the Distance required; and where it doth meet the *Sinical Parallels*, there is 37 ½ Leagues, the Departure from the *Meridian*.

Problem. III.

The Course and Departure being given, to find the Distance and difference of Latitude.

Course the fifth Rhomb, Departure 37 ½ Leagues.

Set the Index to the *Course* found in the Limb, and in the *Sinical Parallels* find the *Departure* 37 ½, (being numbred in the Margent) and where it doth meet with the Index in the same position, it sheweth the *Distance* run to be 45 Leagues; and where it meeteth with the *Co-sinical Parallels*, there you will find the difference of *Latitude* to be 25 Leagues.

Problem IV.

The Distance and difference of Latitude being given, to find the Course and Departure.

Distance 45, difference of Latitude 25 Leagues.

First, Find the *Distance* run upon the Index, and then move the Index until it doth intersect the difference of *Latitude* in the *Co-sinical Parallels*; and at this position of the Index, look in the Limb, and there you will find the *Course* to be the fifth *Rhomb*, which was required; and where the *Co-sinical Parallel* of 25 doth meet with the *Sinical Parallel* under the

the edge of the Index, that will ſhew you the *Departure* from the *Meridian*, which is 37 ½ Leagues, on the ſide C D.

Problem. V.

The Diſtance run, and Departure from the Meridian being given, to find the Courſe and difference of Latitude.

Diſtance 45 *Leagues*, *Departure* 37 ½ *Leagues.*

Firſt, Find the *Diſtance* run, on the Index, put that to the *Departure*, in the *Sinical Parallels*, and that point ſhall cut in the *Co-ſinical Parallels* the difference of *Latitude*, 25 Leag. and the edge of the Index ſhall ſhew in the Limb the *Courſe*, which is the fifth *Rhomb*, which was required.

Problem. VI.

The difference of Latitude, and Departure from the Meridian being given, to find the Courſe and Diſtance.

Diff. Lat. 25 *Leagues*, *Departure* 37 ½ *Leagues.*

Firſt, Find the difference of *Latitude* in the Margent of *Co-ſinical Parallels*, and alſo the *Departure* in the Margent of the *Sinical Parallels*; and note where thoſe *Parallels* meet each other, in that point put the Index: then on the edge of the Index ſhall be cut 45 deg. the *Diſtance*, and on the Limb the edge of the Index will ſhew the fifth *Rhomb* which was required.

Problem. VII.

To know how many Leagues you muſt ſail upon any point of the Compaſs, to raiſe or depreſs a degree of Latitude by the Sinical Quadrant.

To perform this, you muſt lay the Index upon the point of the Compaſs, and ſee where the *Co-ſinical Parallel* of 20 Leagues (which is one degree in the Equinoctial) doth interſect the edge of the Index, there will be ſhewn the quantity of Leagues you muſt ſail to raiſe or depreſs the Pole upon any point of the Compaſs.

As for Example on the third Rhomb.

If you lay the Index on the third *Rhomb*, the *Co-ſinical Parallel* of 20, will ſhew 24 Leagues, which you muſt ſail on that point, to raiſe or depreſs one degree of *Latitude*; and that point on the Index will ſhew in the *Sinical Parallels*, the departure from the Meridian to be 13 *Leagues* 1 Mile.

Problem. VIII.

Shewing the Uſe of the Sinical Quadrant in working a Traverſe at Sea.

The *Sinical Quadrant* is a plain and ready Inſtrument for this purpoſe, and is commonly imployed for the working of ſhort Traverſes at Sea; I'le give one Example of 24 hours run, in the manner as 'tis uſually plac'd on the Log-Board, and how it may be taken off and wrought by this Inſtrument.

Example.

Admit a Ship at Sea, and bound to the Northward, ſteers away her Courſe North East, but then meeting with a contrary and ſhuffling Wind, ſhe makes ſeveral Courſes, as is here-under expreſſed in this Table, after the form of a Log-Board.

H	K	HK	F	C	W.
2	4	0	0	N. E.	N. W.
4	3	1	0	E. N. E.	N. ½ E.
6	3	0	0		
8	3	0	0		
10	3	1	0	E. ½ N.	N. N. E.
12	4	0	0		
2	4	1	0		
4	3	0	0	E. S. E. ½ E.	N. E.
6	3	1	0		
8	4	0	0		
10	5	0	0	N. by W. ½ W	
12	4	1	0		

In

In this Table there are six Columns; The *first* distinguished with H, shews the time, or hours, at which these Courses and Distances are thus set down upon the Log-Board, that is at 2 o'th Clock, 4 o'th Clock, 6 o'th Clock, *&c.* the Log being commonly hove every two hours.

The *second*, *third*, and *fourth* Columns shew the Knots, half Knots and Fathoms that the Ship runs upon any Course in the space of half a minute, measured by a half minute Glass.

The *fifth* Column contains the Course steerd by the Compass, the true walk that the Ship makes, being left to the discretion of the Calculator, to be allowed according to the mould of the Ship, and the Sail she bears; and also having respect to the Wind and Sea at the same time.

The *sixth* Column shews upon what Point of the Compass the Wind is, and manifesting whether the Course be Large or upon a Wind.

Thus much for the form of the Log-Board, and the manner of seting down the Courses and distances thereon; now somewhat briefly, how to take off (as they call it) this account from the Log-Board, thereby to compute the Ships true Course and Distance by the *Sinical Quadrant*, or other Instrumental or Arithmetical Calculation. 'Tis usual for the Master, his Mates, and all other that are desirous to keep a Reckoning of the Ships way, every day at Noon when the Ship is at Sea to take an account of the several runs upon the Log-Board, for the 24 hours last past, taking notice of the Wind and other Accidents, allowing for every Knot and half Knot, so many miles and half miles run in one hour, and four times so many in a Watch, or four hours; and because 'tis usual to heave the Log but twice in a Watch, or every two hours, and the Course and distance set down accordingly; therefore the Knots and half Knots upon the Log-Board, for each Course must be added together, and the total double gives the Number of Miles upon each respective Course: As for instance, in this example in the Table, under the Letters of distinction (*viz.* H, K, H K, *&c.*) in the first *Parallel*, you will find 4 Knots N. E. which being doubled, gives 8 Miles, the Distance upon that Course: But now for the more orderly working the 24 hours run, its convenient to frame a Table, after the form of this here annexed.

The Operation of these Traverses by the Sinical Quadrant.

1. The first Course is North East 8 miles, the wind Large, therefore lay the Index upon the fourth Rhomb, or 45 degrees from the Meridian, you shall find the Distance run 8 miles upon the Index, to intersect at 5 ½, in the *Co-sinical Parallels*, which is the Northing, and is to be placed in the North Column, and to cut 5 ½ in the *Sinical Parallels*, which is the Easting, to be placed in the East Column, and the reason why the difference of *Latitude* and *Departure* now found by the *Sinical Quadrant*, is set under the North and East Columns, is because the Course is between the North and the East.

A Table of the Northing, Southing, Easting and Westing of these Courses found by the Sinical Quadrant.

Course.	Dist.	N.	S.	E.	W.
	miles.	miles.	miles.	miles.	miles.
N. E.	08	05 ½		05 ½	
E. by N.	19	05 ½		18	
E. ½ S.	24		4 ¾	24	*ferè.*
S.E.by E.½ E.	21		10	18	
N.N.W.½W.	19	17			09
Sum		26	14 ¾	66	
		14 ¾		09	09
Diff. of Lat.	No.	12 ½		57	E.

2. The second Course is North and by East 19 miles upon a Wind, the Course steered is East North East, the Ship lying within 5 ½ points of the Wind, and allowing one point for Lee-ward-way, the true Course is as before East and by North; Therefore place the Index to the seventh point, or 78° ¾ from the Meridian, and by 19 miles, the *Distance*, there will

will be cut 5 ½ miles, in the *Co-sinical Parallels*, which is the Northing, and 18 miles in the *Sinical*, which is the Easting.

3. The third Course is (allowing, as before, one point for Leeward-way) East a ½ point Southerly, and the distance 24 miles; therefore lay the Index to 7 ½ points, or 84 deg. ½, and by 24 found on the Index, shall be cut 4 ½ in the *Co-sinical Parallels*, which is the Southing, and 24 *ferè* in the *Sinical*, which is the Easting of this Course and distance. And what hath been said of these three Courses, the same is to be understood of all the rest in the fore-going Table, giving the same allowance as before, the Ship being still by a Wind.

Having thus therefore, according to these last Instances, found the Northing and Southing, Easting and Westing of these several Courses, and Distances, and placed them in their proper Columns; sum up the miles in those Columns, and orderly subscribe their total, as in this Example.

The sum of the North Column, is 26 miles; of the South Column, 14 ¼; of the East, 66; and of the West 9 miles.

Then compare the North and South Columns together, and also the East and West; and deduct the lesser from the greater, as in the fore-going Table; the Southing is to be substracted from the Northing, and the Westing from the Easting; the Remainder Northerly 12 ¼ miles is the difference of Latitude; the Residue under the East Column 57 miles, is the departure to the Eastward of the Meridian.

And if the direct Course, and nearest Distance, from the place where the Ship began this Traverse, to that where she now is supposed to be, were required, 'tis readily computed by the *Sinical Quadr.* And to perform this, find where 12 ¼ in the *Co-sinical Parallels* intersect the *Sinical Parallel* of 57, and bring the Index to that Point, and by the Index in the Limb shall be shewn the Angle of the Course 78 deg. *ferè*, or 7 points from the Meridian, *viz.* E. by N. and the Distance run, found on the Index, will be 58 miles.

And thus after the form of this first Example, you may find the difference of Latitude, and Departure from the Meridian of any 24 hours Traverse, and likewise reduce it to one Course and Distance.

And what is here in particular applyed to the *Sinical Quadrant*, the same is to be understood of the other Instruments, it being only a repetion of the first Case, by the *Course* and *Distance* given, to find the *Difference* of *Latitude*, and the *Departure*, which found, is orderly to be placed in a Table, as in the fore-going Example.

Having

Having ſpoken ſomewhat of the Log-Board, and of the Uſe thereof, I think it not amiſs here to ſay ſomething of the Log-Line and Half-minute Glaſs.

An Advertiſement concerning the Log-Line, and Half-minute Glaſs.

Seeing that the manner of keeping a Reckoning of the Ships way (by our *Engliſh* Navigators) is commonly by the Log-Line and half-minute Glaſs, and there ought to be great care had to the Truth of them; but it hath been an antient Cuſtom to meaſure ſeven fathom between knot and knot upon the Log-line; which way of meaſuring hath been grounded upon a meer conjecture, that 5 of our feet make a pace, and a thouſand ſuch paces make a mile, and that 60 ſuch miles make a degree; ſo that a degree ſhould contain 300000 of our feet, and one mile (or minute) 5000 feet; and becauſe an half minute of time is the 120th part of an hour, the Log-line ſhould anſwer to that proportion, and be the 120th part of a mile, which by this account is 41 $\frac{2}{3}$ feet, between each knot on the Log-line.

But this erronious computation hath been ſufficiently refuted by Mr. *Oughtred*, Mr. *Norwood*, and others.

Mr. *Oughtred* in his *Circles of Proportion*, pag. 153, doth there propoſe 66 $\frac{1}{4}$ Statute miles to anſwer to one degree upon the Earth, each containing 5280 feet; ſo that according to this computation there is 349800 Engliſh feet in one degree.

And Mr. *Norwood* in his *Seamans Practice* pag. 43. doth declare, *That* (by a worthy and commendable Experiment of his) *he found a degree of the Circumference of the Earth and Sea, to contain 367200 of our Engliſh feet.* But he further conſenteth, *That becauſe the Ships way is more, than doth really appear by the Log-line, and becauſe it is more ſafe to have the Reckoning to be ſomewhat before the Ship, together with the evenneſs of Number, to allow but 360000 feet to be one degree, and conſequently 6000 Engliſh feet to be one minute or 60th part of a Degree (vulgarly called a mile) which Number being divided by 120, giveth 50 foot between knot and knot on the Log-line; ſo that upon this ground, if a Ship runneth out*

one

one of theſe knots in half a minute, ſhe runneth one mile (or the ſixtieth part of a degree) in an hour, or one League and one mile in a Watch (or 4 hours.)

But notwithſtanding Mr. *Oughtreds* Aſſertion, and eſpecially this Experiment of Mr. *Norwoods*, together with the conſent and approbation of Mr. *Collins* and other accompliſhed *Mathematicians* in their Books of *Navigation*, hath ſufficiently detected this Error; yet this Truth hath not had that entertainment, as the excellency thereof hath deſerved, becauſe Cuſtom hath ſo long prevailed againſt Reaſon.

Mr. *Norwood* in his fore-mentioned Book, hath aſſigned ſome reaſons why he ſuppoſeth this error hath been ſo long received and tollerated; I ſhall forbear to mention them, referring you to the Book it ſelf. But I ſhall aſſign one Reaſon more which I have obſerved from experience, which I hope will in ſome meaſure help to prove the Truth of Mr. *Norwoods* Experiment, and that the Log-line (as commonly divided) may be proved to be too ſhort for true meaſure; for I have obſerved, that if a half-minute Glaſs be made of its due length, and according to true time, that then their reckonings intollerably out-run the Ship; and they continually complain, that thoſe Glaſſes are too long; But if they have a Glaſs that is 5 ſeconds ſhorter than true time, they do reaſonably well agree with the Log-line in their Reckonings, becauſe one Error doth counterpoiſe another, *viz.* ſhort meaſure and ſhort time, yet notwithſtanding this concurrence and affinity there is between this Log-line and ſhort half-minute Glaſs, it is apparent that they are both errours, and therefore to be rejected: for I ſuppoſe it would quickly appear, that if the Log-line were of its due length and meaſure (*i. e.*) 50 foot between each knot, and the half-minute Glaſs of its due length, according to true time, there would doubtleſs be a greater harmony and concurrence of truth, and Navigation be of more certainty than it is.

So that now it doth plainly appear, by this above mentioned Obſervation, that the Log-line, as commonly divided, is too ſhort, according to Mr. *Norwoods* Experiment, becauſe the neceſſity of keeping a concurrence in the Reckoning, is by a Glaſs that is too ſhort by 5 ſeconds for the true time of half a minute, or 30 ſeconds.

But here I ſhall give you a Rule to prove whether a half-minute-Glaſs be of true length or not, the way is generally approved to be very true, and what I have many times made Experience of, and can atteſt it by my own knowledge. The Experiment is mentioned by Mr. *Phillips*, in his *Advancement of Navigation*, and is thus to be performed.

An eaſie and exact way to meaſure a Half-minute Glaſs, or any ſmal portion of time.

Take a Bullet of any weight whatſoever, and make faſt a piece of thread or ſilk to it, being 38 ½ Inches in length, from the Center of the Bullet, unto the end of the thread, where a nooſe muſt be made to hang it on a ſmall Pin, which is to be faſtened to any place where the Bullet may ſwing freely.

This *Pendulum* being thus prepared, hang his nooſe on the Pin, the thread being exactly 38 ½ Inches between the Center of Gravity, and the Center of Motion, each of the ſwings of this Bullet (being either ſwift or ſlow) ſhall be a true ſecond of time; So that 60 of theſe ſwings will be the true length of a minute, and 30 the true length of half a min. So by this ingenious Experiment, you may know which of all your half minutes is a true Glaſs; and if you have no Glaſs, you may meaſure any ſmall portion of time by this Experiment, for half a ſecond of time is diſcovered every time the *Pendulum* doth paſs the *Perpendicular*, that is ſuppoſed to fall from the Pin whereon the *Pendulum* doth hang.

But if it ſhould be objected, that at Sea, when the Ship is thrown to and again by the violence thereof, that then the *Vibrations* of the *Pendulum* may by that means be obſtructed, and ſo the ſwings to be uncertain.

A Remedy there is proved againſt this, by making the thread 7 inches ſhorter, and there to make a ſmall knot, which knot you are to hold between your finger and thumb, and then with a motion of your hand to cauſe the Bullet alwayes to aſcend to an Angle of 60 degrees (from the *Perpendicular*) and ſo ſhall each ſwing be equivolent to thoſe before; So that if a Ship be toſſed with the violence of the Sea, yet a man may make ſhift to try this Experiment, and to meaſure a true half-minute of time without the help of a Glaſs.

SECT. IV.

The Description and Use of the Plat in Plano.

THese Plats are commonly drawn upon Vellom, and pasted upon Boards; in the middle of the Plat is a Center, upon which there is an occult Circle described, which is commonly divided into 16 or 32 parts or points; so by every one of these points (from the Cencer) are drawn several Lines quite through the Plat, representing the Rhombs or Points of the Compass, necessary for the Use thereof.

Then is the fashion and form of the Land portraied upon it, and curiously set off with lively Colours; and also a Scale of Leagues to measure the Distances of Places.

There is also a Meridian Line equally divided upon the Plat, which discovereth the Latitude of any Place; The several Uses follow.

The Use of the Plat.

1. *To find the Latitude of any Place upon the Plat.*

Take your Compasses, and set one foot in the place required, and extend the other foot to the neareſt Distance of an East and West Line, and note where that Line doth cut the Meridian Line (that is divided into degrees) then set one foot where it intersects the Meridian Line, and the other Foot will reach upon the Meridian Line, to the Latitude of the place required.

2. *To find the Distance of one Place from another.*

If the Distance required be less than the length of the Scale, then take your Compasses, and set one foot in one of the places, and the other foot in the other place, then with that extent between your Compasses

apply to your Scale of Leagues, and then you will find the measure of the Distance of the two places.

But if the Distance between the two places be greater than the length of the Scale, then first extend your Compasses upon the Scale to the whole Length thereof, and with that extent, set one foot in one of the Places required, then direct the other foot towards the other place by the help of a Scale or Ruler in a right Line; and if the distance be very great, you must turn the distance between the Compasses over and over, until you come to the other place required; and if it falls out that the last extent doth fall over the second place, you must then, from the last place where the Compass stayed, draw in the other point, until it touch in the place required, and measure that upon the Scale of Leagues. As suppose your Scale were an 100 Leagues, and if you turn the Compasses two or three times over, then is the distance so many 100 Leagues, and that smal distance more; which being measured upon the Scale, it giveth the odd Leagues, and so consequently the Distance required.

3. *To find upon what Point of the Compass one Place beareth from another.*

If from the two places propounded, there be a *Rhomb-Line* that lieth directly from place to place, then is there no more trouble in it, but to look upon the small Compass upon the Plat, and see upon what *Rhomb* it is that they bear one from another.

But in case a *Rhomb-Line* doth not lie so direct from one place to another, then extend your Compasses from the first place in the neareſt distance to the next *Rhomb-Line*, that you imagine in your judgement lyeth neareſt a *Parallel* from place to place, and upon that *Rhomb-Line* run your Compasses along, till the other point (being at right Angls with it) doth reach the other place, and that *Rhomb-Line* is the true point of bearing the one from the other.

4. *To keep a Reckoning upon the Plat of a whole Voyage.*

Firſt, It is to be understood, that you are to keep a Reckoning of every dayes work, either by the Tables, or your *Sinical Quadrant* (as you are before taught) or any other way necessary for such a purpose; and also to cast up all your Traverses for one or more dayes: and then after you have so done, and brought it to the neareſt truth you can, either

ther by Obſervation or otherwiſe, then you are to ſet off your work up on your Plat, ſo that the Place where your Ship is, may appear to your eye for the ſatisfaction of your mind, and for the information of your judgement.

As ſuppoſe that you Sail from the *Lizard* South-Eaſtwards; then from that very time you begin to keep your Reckoning of your ſeveral *Courſes* and *Diſtances*, until you have ſome convenient time to caſt up all your work, to find the difference of Latitude, and your Departure from the Meridian of the *Lizard*. The difference of Latitude we will ſuppoſe to be 3°, and the Departure to be 50 Leagues, which 3 degrees you muſt ſubſtract from the Latitude of the *Lizard*, which we ſuppoſe to be 50° 00′ North; ſo that the *Latitude* that the Ship is now in, is 47° 10′, and 50 Leagues to the Eaſtwards.

Therefore to ſet the place of your Ship upon your Plat, you muſt uſe two pair of Plat Compaſſes, with one pair take the extent between the Latitude of 50° 00′, and 47° 10′; and ſet one point of your Compaſſes in the *Lizard*, and extend the other point towards the ſecond place, but ſo that your Compaſſes may ſtand *Parallel* to a North and South Line, which may be eaſily found with the other pair of Compaſſes, by trying whether the Leggs be equidiſtant from the next North and South Line; this done, keep one foot of your Compaſſes in that point, and with the other pair, take the departure 50 Leagues from the Scale of Leagues, then interchange your Compaſſes, placing theſe laſt pair, in the point where the other pair ſtood, ſet this Departure 50 Leagues to the Eaſtward; and ſo that your Compaſſes may ſtand Parallel to an Eaſt and Weſt Line, which you may try, as is ſaid before; the ſecond point thus found upon the Plat, is the place of the Ship, (according to your Reckoning) which was required.

Thus much for the Plat *according to* Plano.

SECT.

SECT. V.

The Use of the True (commonly called Mercators) Chart.

I Shall not here mention the projection of this Chart, it being largely handled by the first Inventor Mr. *Edward Wright*, in his *Correction of Errors*, only here shew very briefly, the ordinary and most necessary uses of this Chart.

1. *To find the Latitude of any Place in these Charts.*

This Operation upon these Charts, is in all respects like that which has already been delivered for the same purpose, in the Use of the Plat, or plain Sea Chart; for if you set one point of your Compasses in the place whose *Latitude* is required, and open them in the shortest Distance to the next East and West Line, observing where it intersects the graduated Meridian, and then place one point in that intersection, turning your Compasses upwards or downwards, according as the place lies, from the East and West Line, and the movable point shall shew upon the said Meridian the *Latitude* of the place required. Suppose the *Latitude* of *Ushant* were required by this Chart?

If you take the nearest extent to an East and west Line, and place that distance from the intersection on the graduated Meridian, as is before directed, you will find the *Latitude* of *Ushant* to be 48° 3′ Northerly.

2. *To find the Longitude of a Place, and consequently the difference of Longitude in degrees, between any two places scituate upon the Chart.*

To find the *Longitude* of any place upon the Chart, set one point of your Compasses in the said place, and take the nearest distance to the next North or South Line, and observe where this Line intersects the Equinoctial, and keeping the same extent in your Compasses, place one point

point in the Interſection, and turning the Compaſſes the ſame way, that the place whoſe Longitude is ſought lies from the North and South Line, the movable point reſting in the Equinoctial, will ſhew the Longitude required.

Suppoſe the Longitude of the *Barbadoes* were required.

If you place the point of your Compaſſes in the Iſland of *Barbadoes* in the Chart, and take the ſhorteſt extent to the next North and South Line, placing the ſame at the Interſection in the Equinoctial as is directed, you will find the Longitude of the *Barbadoes* to be in theſe Charts 317° 30′ from *Teneriff*; but the Longitude of places being various, according to the places from whence it is begun, ſome reckoning it from *Flores* and *Corvus*, ſome from *Teneriff*, &c. The chief buſineſs will be to find the difference of Longitude between any two places, which is thus to be performed.

When you have found the Longitude of the two places, ſubſtract the leſſer from the greater; and the *Remainder*, if leſs than 180°, is the *Difference* of *Longitude* between the two places; but if the *Remainder* be greater than 180°, ſubſtract it from 360, the laſt *Remainder*, is the *Difference of Longitude* required.

Suppoſe the two places were the *Lizard* in the *Longitude* 10° 40′, and *Thoma* Iſland in the *Longitude* 27° 30′, ſubſtracting 10° 40′ from 27° 30′, the *Remainder* 16° 50′ is the *Diff. Long.*

Again, Suppoſe the two places were the *Lizard*, as before, and *Barbadoes* in the Longitude 317° 30′; ſubſtracting 10° 40′ from 317° 30′, there *Remaines* 306° 50′, which ſubſtracted from 360°, the *Remainder* 53° 10′ is the *Difference of Longitude* required.

3. *To know how one Place bears from another.*

For the performance of this *Problem*, lay the edge of a Ruler from one place to another, and with a pair of Compaſſes try to which of the *Rhomb* Lines the edge of the Ruler is the neareſt Parallel, which being found, that ſheweth the point of the Compaſſes the two places bear one from another.

Suppoſe the bearing of the *Barbadoes* from the *Lizard* were required: Therefore lay the edge of the Ruler upon both places, and you will find that South Weſt ½ a point Weſterly is the neareſt Parallel thereto, which is the bearing of the *Barbadoes* from the *Lizard*, and the oppoſite point North Eaſt ½ Eaſt the bearing of the *Lizard* from the *Barbadoes*.

4. *To*

4. *To find the Distance of two places upon* MERCATORS CHART.

If both places be in one and the same Latitude, take with your Compasses the length of a degree of the Meridian at that Latitude (taking half the degree above, and half beneath the Latitude) for so oft as you shall find that length between the two places, so many times 20 Leagues are there betwixt them; but if the distance be great, for expedition, you may take five times the length of that degree, and counting it for 100 Leagues, proceed as before.

Suppose the *Distance* were required between the point of *Ushant* in *France*, and *Trinity Bay* in *New-found-Land*.

The *Distance* taken as before about the Latitude of 37°, you will find it to be 550 Leagues.

But if two places have not the same *Latitude* the *Equinoctial* not coming between them, substract the lesser *Latitude* out of the greater; but if the *Equinoctial* cometh between them, add both *Latitudes* together, so have you the *difference* of *Latitude* between both places.

Now if both places have the same Longitude, so many degrees as there is in the *difference* of *Latitude* so many times 20 Leagues is the *Distance*.

But if the places differ both in *Latitude* and *Longitude*, then look how many degrees the difference of *Latitude* contains, so many degrees of the *Equinoctial* take between your Compasses; then lay a long Ruler to both places, whose distance you seek, and observe where the Ruler crosses the *Equinoctial*, or some other East or West Line, or *Parallel of Latitude*, and leading one foot in the *Equinoctial* or other *Parallel*, move forwards the other also *Parallel*-wise, keeping alwayes that distance, till it cross the *Rhomb* of those two places in such sort, that one foot resting by the edge of the Ruler, the other carried about, may but only touch the *Equinoctial*, or other *Parallel* cut by the edge of the Ruler; then take with your Compasses the *Segment*, or part of that *Rhomb* between the crossing and the *Equinoctial* or *Parallel*, set both feet in the *Equinoctial*; and see how many degrees are contained betwixt them, so many times 20 Leagues is the *distance of those two places*.

Or if that *Segment* of the said *Rhomb* be greater than can well be taken with the Compasses, take the length of 5 degrees of the *Equinoctial* between your Compasses, and look how oft you can find that length in the *Segment* of the *Rhomb* aforesaid, for so many hundred Leagues is the *Distance of those two places*.

It

If the Diſtance from the *Lizard* to the *Barbadoes* were required, the difference of *Latitude* between thoſe places, is 36° 48′; Therefore take 36° 48′ from the *Equinoctial*, and laying a Ruler over both places, of a ſufficient length, it will croſs ſome *Parallel* of *Latitude* about 9 degrees; then keeping this *Diſtance* of degrees in your Compaſſes, apply one point to the edge of the Ruler, ſo that the other point may but juſt touch the *Parallel* croſſed by the Ruler; the *Segment* of the *Rhomb*, between the point where the Compaſſes ſtayes, and the interſection by the Ruler, and *Parallel* of *Latitude*, meaſured by the degrees of the *Equinoctial*, gives the diſtance 1141 Leagues, which was required.

There is nothing elſe that will be of any difficulty in the common uſe of this Chart, if theſe brief hints be underſtood.

SECT. VI.

The Deſcription and Uſe of the Globes.

OF *Globes*, there are two ſorts; one is *Terreſtrial*, and the other *Cœleſtial*.

The *Terreſtrial* hath on the *Superficies* of the Body portrayed and deſcribed the whole form and faſhion of the Earth and Sea, with all the Circles of the Sphear, as Colures, Equinoctial, Tropicks, *&c.*

The *Cœleſtial Globe* hath on its ſurface, the Conſtellations of all the known Stars in the Heavens, placed in their true Latitudes and Longitudes, Right Aſcenſions and Declinations, drawn into ſeveral Images and Figures, according to the fictions of the Antients; with the Circles of the Sphear, as in the *Terreſtrial Globe*.

Geographical Definitions, neceſſary to be underſtood.

Def. I.

The *Globe* of the Earth is a *Spherical Body* proportionally compoſed of Earth and Water, and is divided into Continents and Iſlands.

II.

A Continent is a great quantity of Land not divided nor ſeparated by the Sea, wherein are many Kingdoms and Principalities, as *Europe*, *Aſia*, and *Africa* are one Continent, and *America* is another.

III.

An Iſland is ſuch a part of the Earth that is invironed round with Water; as the Iſland of *England* and *Scotland*, aud alſo *Ireland*, and the Iſle of *Wight*, the *Barbadoes*, &c.

IV.

A *Peninſula* is ſuch a part of Land as is almoſt encompaſſed about with Water, and is only joyned with the Land by an Iſthmus; ſuch is that great part of Land in *America*, called *Peruviana*; and *Morea* in the *Levant*.

V.

An *Iſthmus* is a narrow neck of Land which joyneth the *Peninſula* to the Continent.

VI.

A *Promontory* is ſome high Mountain, or great Cape of Land that ſhooteth it ſelf into the Sea, as *Cape Bon Eſperance*, or *Capo de Verde* in *Africa*.

VII.

The *Ocean* is a general Collection of the Waters, which environeth the World on every ſide.

VIII.

The *Sea* is a part of the *Ocean* to which we cannot come but through ſome ſtreight, as the *Mediterranean* and the *Baltick* Sea.

IX.

A *Streight* is a part of the *Ocean* reſtrained within narrow bounds, and opening a way to the *Sea*; as the Straits of *Gebralter*, that leadeth into the *Mediterranean*, and the Sound that leadeth into the *Baltick* Sea.

X.

A *Creek* is a ſmall narrow part of the *Sea* or *Rivers*, that go up but a little way in the Land.

XI.

A *Bay* is a great Inlet of the Land, as the Bay of *Biſcaia*, and the Bay of *Mexico*.

XII.

A *Gulph* is a greater Inlet of the Land deeper than a Bay, ſuch is the

Gulph

Gulph of *Venice*, and the *Gulph* of *Florida*; which alſo have a ſwift Current.

XIII.

A *Climate* is a certain ſpace of *Earth* and *Sea* that is included within the ſpace of two *Parallels*, and of them there hath been antiently accounted ſeven.

1. *Dia Meroes.*
2. *Dia Syenes.*
3. *Dia Alexandrias.*
4. *Dia Rhodes.*
5. *Dia Rhomes.*
6. *Dia Boriſthenes.*
7. *Dia Ripheos.*

XIV.

A *Zone* is a certain ſpace of Earth contained between certain Circles of the Sphere, and are thus divided.

The *Earth* is divided into five *Zones*, *viz.* One Torrid or Burning *Zone*, two Temperate, and two Frozen *Zones.*

The Torrid *Zone* is that which is on each ſide the *Equinoctial*, bounded by the *Tropicks* of *Cancer* and *Capricorn.*

The two Temperate *Zones* are contained between each *Tropick* and the *Polar Circles.*

The two Friged or Frozen *Zones* are contained within each *Polar Circle*, and their reſpective *Poles.*

The Diviſion of the Earthly Globe.

The *Globe* of the Earth is divided into four parts, *Viz.*

Europe, *Aſia*, *Africa*, & *America.*

Europe is bounded from *Aſia* by the *Mediterranean Sea*, on the Eaſt with the River *Tanais*, and on the Weſt with the Weſtern Ocean; and containeth theſe Provinces.

Germany, *Spaine* *Swedeland*, *Hungaria*,
Italy, *Denmark*, *Muſcovia*, *Slavonia*,
France, *Norway*, *Polonia*, *Grecia*.

The Principal Iſlands are theſe.

Great Brittain, *Candia*, *Sardinia*,
Ireland, *Cicilia*, *Corſica*, *Cyprus*.

Aſia, is bounded on the North with the Northern Ocean, and on the South with the Red-Sea, on the Eaſt with the Eaſt-Indian Ocean, and on the Weſt with the Flood *Tanais*.

The Principal Regions are,

Anatolio, *Armenia*, *Aſſyria*, *Perſia*, *China*,
Syria, *Arabia*, *Meſopotania*, *Parthia*, *India*,
Paleſtina, *Media*, *Chaldea*, *Tartaria*, and the Iſlands thereof.

Africa, is bounded on the Eaſt with the Red Sea, on the Weſt with the *Atlantick* Ocean, and on the South with the Southern Ocean, and on the North with the *Mediterranean* Sea.

The Provinces are,

Egypt, *Barbaria*, *Æthiopia*,
Abiſſines, *Alonomotopa*, *Nuba*.

The Iſlands are.

Madagaſcar, or St. *Laurence*, St. *Thomas*. *Cape de Verde Iſlands*.
The *Canary Iſlands*, The *Madera Iſlands*.

America, is bounded on the Eaſt with the *Atlantick* Ocean, on the Weſt with the Weſt-Indian Ocean, on the North with the Northern Ocean, on the South with the *Magelanick Sea*.

It conſiſts of two parts, *viz*. *Mexicana*, *Peruana*.

The

The Provinces of *Mexicana* are,

Nova Hiſpania, *Terra Florida*, *Nova Francia*.
California, *Nova Albion, vel Anglia*, *Eſtotilant*.

The Provinces of *Peruana* are,

Braziłła, *Tiſnada*, *Caribana*, *Catagena*, *Peru*,
Charah, *Chila*, *Chicha*, *Patagonos*.

The Chief Iſlands of *Mexicana* are,

Iſland, *Friezland*, *Greenland*.

The Chief Ilands of *Peruana* are,

Hiſpaniola, *Cuba*, *Jamaica*, *Porto Rico*, *Barbadoes*, and all the reſt of the *Cariba* Iſlands; *Inſula Margaretta*, *Moluque Inſulæ*, *Remores*, *Java Major*, *Java Minor*, *Salamonis Inſula*. And all other Iſlands in *India Orientalis*.

The Names of the Seas.

Ocean Sea, *Narrow Sea*, *Mediterranean Sea*, *Mare Majore*, *Mare Pacificum*, *Mare Caſpium*, *Eaſt-Indian Sea*, *Perſian Sea*, *Red Sea*, *Mar Del Zur*.

The Names and Number of the Stars of each Conſtellation on the Cœleſtial Globe.

Northern Conſtellations are 21, *viz.*

1 *Urſa Major*,	7	6 *Corona Borealis*,	8
2 *Urſa Minor*,	27	7 *Engonaſes, aut Hercules*,	29
3 *Draco*,	31	8 *Lyra*,	10
4 *Cephus*,	11	9 *Olor, aut Cygnus*,	17
5 *Bootes*, or *Arctophilax*,	22	10 *Caſſiopea*,	13

11 *Per-*

11 *Perseus*,	26	17 *Delphinus*,	10
12 *Heniachus*, or *Anriga*,	14	18 *Equiculus*,	4
13 *Serpentarius*,	24	19 *Pegasus*,	20
14 *Serpens*,	18	20 *Andromeda*,	23
15 *Sagittarius*,	5	21 *Triangulus*.	4
16 *Aquilla*,	9	Sum.	323

Zodiack Constellations, 12. *Viz.*

1 *Aries*,	13	7 *Libra*,	8
2 *Taurus*,	23	8 *Scorpio*,	21
3 *Gemini*,	18	9 *Sagittarius*,	31
4 *Cancer*,	9	10 *Capricornus*,	28
5 *Leo*,	27	11 *Aquarius*,	42
6 *Virgo*,	26	12 *Pisces*,	34
		Sum.	280

Southern Constellations, 27.

1 *Cetus*,	22	15 *Pisces Austrinus*,	11
2 *Orion*,	31	16 *Grus*,	13
3 *Flumen Eridanus*,	34	17 *Phœnix*,	15
4 *Lupus*	12	18 *Indus*,	12
5 *Canis Major*,	18	19 *Pavo*,	20
6 *Canis Minor*, *vel Canicula*,	2	20 *Apus*, *avis Indica*,	11
7 *Argo Navis*,	41	21 *Apisc. Musca*.	4
8 *Hydra*,	25	22 *Chamelion*,	10
9 *Crater*,	7	23 *Triangulum Auster*,	5
10 *Corvus*,	7	24 *Pisces volans*	7
11 *Centaurus*,	37	25 *Dorado*,	7
12 *Fera aut Lupus*,	19	26 *Toucan*, *Anser Americanus*,	8
13 *Ara vel altar*,	7	27 *Hydrus*, *Serpens Aust.*	21
14 *Corona Aust. vel Merid.*	10	Sum.	429

The Material Globes are compoſed of theſe parts.

First, *The Body or Globe it ſelf.*
Secondly, *The Braſen Meridian,*
Thirdly, *The Quadrant of Altitude.*
Fourthly, *The Hour-Circle and Index.*
Fifthly, *The Wooden Frame in which it is put.*

The *Globe it ſelf*, with the Concerns and Apurtenances thereunto belonging, is for the lively repreſentation of the natural ſituation and poſition of the Earth and Heavens, and ſerveth for the demonſtrating of any *Problem* incident to the Sphear, and on the Earth, either in *Aſtronomy*, *Geography*, or *Navigation*.

1. The *Brazen Meridian* is divided into 4 parts or Quadrants each being divided into 90 degrees; within this *Meridian*, the whole Body of the *Globe* turneth upon the *Axis* that cometh forth from the Body, being two ſtrong braſs Wiers.

2. The *Hour Circle* is a flat Ring of Braſs, faſtened upon the North part of the Meridian, and is divided into the 24 hours of a natural day; and each of theſe hours is ſubdivided into halves and quarters.

3. The *Quadrant of Altitude*, is a long and thin ſlip of Braſs, divided into 90 degrees, and is to move up and down upon the ſurface of the Globe to any poſition required; and when placed in the *Zenith*, the edge thereof repreſenteth an *Azimuth*, and the diviſions ſhew the *Almicanters* or *Circles* of *Altitude*.

4. The *Horizon* is a flat and round frame of *Wood*, in which the *Braſen Meridian*, and conſequently the whole *Globe* doth move, being divided into a *Kalender*, ſhewing the day of the Month, the place of the Sun, the Rhombs, *&c.*

Problem 1.

How to ſet the Globe to the Latitude of a place.

Suppoſe you were to ſet the *Globe* to the Latitude of 52 degrees North; the *Globe* being in the Frame, move the *Meridian* either higher or lower, until 52 doth cut the very edge of the *Horizon* on the North ſide thereof, (the divided ſide of the *Brazen Meridian* being towards you) then the

the *Meridian* of the *Globe* being turned North and South, by the help of a *Magnetical Needle*, it doth then represent the natural scituation of the Heaven and Earth.

Problem. II.

To find the Latitude of any place upon the Globe.

First, Find the Place required upon the *Globe*, then turn the *Globe* about, until the place whose Latitude is required, be just under the *Brazen Meridian*; then note what degree stands against it on the *Meridian*, that is the Latitude of the place which was required.

Example.

Let it be required to find the Latitude of *Rome*: turn the body of the *Globe* about, till *Rome* be just under the *Brass Meridian*, and you will see 42 to be right against it, which is the Latitude of *Rome*.

Problem. III.

To find the Longitude of any place upon the Globe.

Turn the Body of the *Globe* about, till the place, whose Longitude you require, comes under the *Meridian*: then observe what degree of the *Equinoctial* is cut by the *Brass Meridian*, and the number of those degrees is the Longitude of the place you seek for.

Example.

Let it be required to find the Longitude of *Rome*, as before, therefore bring *Rome* under the *Meridian*, which being done, the *Meridian* will cut the *Equinoctial* in 36° 30′, the Longitude required.

Problem IV.

To find the Distance of any two places on the Globe.

To perform this lay the *Quadrant* of *Altitude* upon both the places required

quired, and note how many degrees there is contained between them: which being found, multiply by 60, and the Product will give you the distance between the said places in minutes.

Example.

Let it be required to find the distance between *London* and *Rome*; Therefore lay the *Quadrant of Altitude* from one place to another, and you will find 15 degrees to be intercepted between the aforesaid places, which being multiplied by 60, giveth 900 miles or minutes distance between *London* and *Rome*.

Problem. V.

To find the Position of Places one to another.

First, Set the Globe to the Latitude of one of the places, and bring the same place under the *Brass Meridian*, and extend the *Quadrant* of *Altitude*, being fixed over the first place, to the other place, and the end of the *Quadrant* shall point out on the *Horizon* the Position that one place hath to another.

Example.

Let it be required to know the bearing of *Rome* from *London*; Therefore bring *London* under the *Brass Meridian*, and there fit the *Quadrant* of *Altitude*, and lay the edge thereof upon *Rome*, and the end of the *Quadrant* of *Altitude* will point you to 56°, which is the position of *Rome* from *London*.

Problem. VI.

The day of the moneth being given, to find what sign and degree the Sun is in.

First, Find the day of the Month in the Kalender on the *Horizon*, and right against it you shall find the sign and degree in which the *Sun* is.

Example.

Let it be required to find the *Suns* place on the fifth of *May*; You

must find the fifth of *May* in the Kalender, and right against it you will find 25 degrees in *Taurus*, which is the Suns place that day.

Problem. VII.

How to place the Index of the Hour-Circle, for every day in the Year.

The *Globe* being set to your Latitude, and the place of the Sun found, (as in the last Proposition) you must find that degree on the *Ecliptick-Line* of the *Globe*, and bring that degree to the *Brass Meridian*; then staying the *Globe* there, turn about the Index of the *Hour-Circle*, till it points just upon the upper Line of 12 in the Hour-Circle, which being done, the *Hour-Circle* is rectified for any time that day.

Problem. VIII.

To find the time of the Suns rising and setting.

The *Hour-Circle* being rectified, and the *Globe* set to the Latitude, then turn the *Globe* about till the degree in which the Sun is cut the East side of the *Horizon*; and then casting your eye upon the *Hour-Circle*, the Index will shew you the time of the Suns rising; and the *Globe* being turned about, till the degree of the Sun cut the West side of the *Horizon*, the Index will shew you the time of the Suns setting.

Example.

Let it be required to find the Suns rising and setting the fifth day of *May* in the Latitude of *London*, the Sun being then in 25 degrees of *Taurus*. First, find the 25th degree of *Taurus* in the *Ecliptick-Line*, which being turned to the East part of the *Horizon*, you will find the Index point to a quarter after 4 of the Clock; the same point being turned to the West part of the *Horizon*, you will find the hour Index point to 3 quarters past 7, the time of Sun setting.

Having the time of the Suns rising and setting, you may find the length of the Day and Night: for the time of the Suns rising being doubled, gives the length of the Day.

Example,

Example.

The fifth of *May*, the Sun riseth at 4 of the Clock and a quarter past; which being doubled, is 8 hours and a half, the length of the Night; and the Sun setting, which is at 7 a Clock and three quarters, which being doubled, is 15 ½ hours, the length of the Day.

Problem. IX.

To find the Suns Amplitude.

The *Amplitude* of the *Sun*, is an Arch intercepted between the East and West points, and that part of the *Horizon* where the *Sun* riseth or setteth.

The finding of the *Amplitude*, differeth little from the last Proposition, for having brought the degree of the Suns place to the *Horizon*, you must count how many degrees of the *Horizon* are intercepted between the East or West point, and that part of the *Horizon* where the *Sun* either riseth or setteth.

Example.

On the fifth of *May*, I desire to know the *Suns Amplitude*, in the Lat. of *London*; Therefore bring the place of the Sun that day to the *Horizon*, and you will find 31 deg. 15 min. intercepted between the point of the *Horizon*, and the East point, which is the *Suns* true *Amplitude* Northerly.

Problem. X.

How to find the Suns Declination any day of the Year.

The *Declination* of the *Sun* is an *Arch* of the *Meridian* intercepted between the *Suns* place and the *Equinoctial*; to find which, you must bring the degree in which the *Sun* is, to the *Brazen Meridian*, and there stay it, and count how many degrees of the *Brazen Meridian* are contained between the *Equinoctial* and the *Suns* place, and that is the *Declination*.

Example.

I would know what *Declination* the *Sun* hath the fifth of *May*, the

Sun being 25 degrees in *Taurus*, which being brought to the Meridian, you will find 19 degrees incercepted between that point and the Equinoctial on the Brazen Meridian, which is the *Declination* required.

Problem. XI.

To find the Meridian *Altitude of the Sun any day of the Year.*

The *Meridian Altitude* of the *Sun* is an Arch of the Meridian, intercepted between the *Horizon* and the degree in which the *Sun* is. To perform which, turn the *Globe* about till the degree of the Sun be just under the Brass Meridian, then staying the *Globe* there, count how many degrees are contained between the place of the Sun, and the Meridians Intersection with the *Horizon*, and that is the Meridian Altitude.

Example.

On the fifth of *May*, it is required to find the *Meridian Altitude* of the *Sun* that day in the Latitude of *London*; the *Suns* place in the *Ecliptick* is 25 degrees in *Taurus*; Therefore bring that degree under the Brass Meridian, and you will find 57 deg. ½, to be intercepted upon the Brass Meridian, between the place of the *Sun* and the *Horizon*, that is the *Meridian Altitude* of the *Sun* that day.

Problem. XII.

How to know what Altitude the Sun shall have any hour of the day, and on any day of the Year.

Having rectified the Index of the *Hour-Circle* for the day proposed, and found the place of the *Sun*, by the second proposition, turn the *Globe* about, till the Index of the *Hour-Circle* be just upon the time when you would know the *Altitude*; then staying the body of the *Globe* here, bring the *Quadrant* of *Altitude* being screwed on to the *Zenith*, and lay it over the *Suns* place, then the number of the degrees contained betwixt the *Horizon* and the *Suns* place, counted on the *Quadrant* of *Altitude*, is the *Altitude* of the *Sun* at that hour.

Example.

Example.

Let the time given be the tenth day of *April* in the Latitude of *London*, at which time (by the second Proposition) I find that the *Sun* is in the beginning of *Taurus*, and I would know what *Altitude* the *Sun* will have at 9 a Clock in the morning: the Index of the *Hour-Circle* being rectified for that day, turn the body of the *Globe* about till the Index on the *Hour-Circle* lies just upon 9 a Clock, then staying the *Globe* there, lay the *Quadrant* of *Altitude* on the *Suns* place, (which is the beginning of *Taurus*) and the number of degrees between the *Horizon* and the *Suns* place, (counted upon the *Quadrant* of *Altitude*) is the true height of the *Sun*, which here I find to be 36 degrees, and that is the *Altitude* at nine a Clock in the Morning, or three in the Afternoon; for the Sun hath the same *Altitude* at 11, 10, 9, 8, 7, 6, 5, 4, in the Morning, as it hath at 1, 2, 3, 4, 5, 6, 7, 8, in the Evening.

Problem XIII.

How to find the Hour of the day by the Globe.

This Proposition cannot be wrought conveniently by the *Globe* only but the *Altitude* of the Sun must be first taken by some Instrument or other, and then this is but the Converse of the former Proposition, which it performs thus: the Globe being set to the Latitude, and the Index of the *Hour-Circle* rectified, turn the Globe about till the degree of the Sun meet with the *Altitude* taken by the Instrument, and then will the Index on the *Hour-Circle* shew you the hour of the day.

Problem. XIV.

To find both the Right and Oblique Ascention of the Sun.

The Globe being set to your Latitude, bring the degree of the Sun to the Brazen Meridian, there staying it, then what degree of the Equinoctial is cut by the said Brazen Meridian, counting the same from the first point of *Aries*, and that is the *Right Ascension* of the Sun that day; So the Sun being in the beginning of *Taurus*, his *Right Ascention* will be found to be about 27° ¾ and bringing the Suns place to the *Horizon*, the *Horizon* will cut the Equinoctial in 13° ½, which is the *Oblique Ascension*.

These

These *Problems* are common to both the Globes. I shall give you those *Problems* that are only proper to the *Cœlestial* Globe.

Problem XV.

To find the Meridian *Altitude of a Star, or the Altitude of a Star at any other time.*

To find the *Meridian Altitude*, let the Globe be set to your Latitude, and then turn the body of the Globe about, till the Star be under the Brazen Meridian, and then the number of degrees of the Meridian intercepted between the Star and the North or South part of the Horizon, according as the Star is situated, is the *Meridian Altitude* thereof.

Now to find the *Altitude* at any other hour, turn about the Globe, till the Index of the Hour-Circle be at the hour you would know the *Altitude* of the Star; and then apply the *Quadrant* of Altitude to the Star, and the degrees of the *Quadrant* cut by the Star, is his *Altitude* at that time.

Problem. XVI.

To know at any time of the Day or Night, what Stars be above the Horizon.

This is no other then to place the Globe in a true position at any time; Now if you would know what Stars are above the Horizon at any time of the day, you must take the Suns *Altitude*, and turning the Globe about till you bring the degree of the Sun just to the Altitude which you found by Observation, on the *Quadrant* of *Altitude*, and then staying the Globe there, you will see all the Stars that are above the *Horizon* at that time.

This same is to be performed in the Night, by any known Star, the *Altitude* of it being taken, in the same manner.

Problem XVII.

How to know the Rising, Culminating, and setting of any fixed Star, and also what part of the Horizon he riseth and setteth in.

Having

Having rectified the Index of the *Hour-Circle*, and placed the Globe according to the Latitude, then find out the Star, whose rising, calumniating, or setting you desire, and bring him to the East side of the *Horizon*, then will the Index of the *Hour-Circle* shew you the time of his rising; then bring the same Star under the Brazen Meridian, and there staying the Globe, the Index will shew you at what hour the said Star calumniates, and comes to the Meridian. Lastly, Bring the same Star about till it cutteth the Western part of the *Horizon*, and then the Index of the *Hour-Circle* will shew you at what hour the said Star setteth, and by the *Horizon* you may know the Amplitude that is on that part of the *Horizon* it riseth or setteth.

Problem XVIII.

To find the hour of the Night by the Globe.

You must take the Altitude of some known Star by a *Quadrant*, or other Instrument, and then having rectified the Index of your *Hour-Circle*, turn the Globe about till you make the Star agree with the *Quadrant* Altitude, according to the Stars Altitude, and then the Index of the *Hour-Circle*, will point out to you the *Hour of the Night*.

Here you must note, That if the Star you Observe be on the West side of the Meridian, you must then turn the *Quadrant* of Altitude to the West side of the Meridian; and if the Star be on the East side of the Meridian, you must turn the *Quadrant* of Altitude on the East side thereof.

SECT.

SECT. VII.

The Description and Use of an Instrument, called an Inclinatory Needle, that doth (by a secret property of the Loadstone, together with the Magnatism of the Earth) shew you the Latitude of any Place, without Observation either of Sun or Stars.

THIS Instrument was first invented by that excellent Philosopher Dr. *Gilbert*, Physitian in ordinary to Queen *Elizabeth*, and hath the approbation of several other able and learned men hereunder mentioned. Mr. *Blundevel* hath written of it, as may appear in the latter end of *Maginus his Theoricks*; and that expert Philosopher Dr. *Ridler*, an English man, Physitian to the Emperor of *Russia*, who hath largely treated of this Instrument, in his Book of *Magnetical Bodies and Motions*. As also that famous Mathematitian Mr. *Edward Wright*, in his Book of *Correction of Errors in Navigation*, hath given a Geometrical Demonstration of the Natural reason thereof, and hath from thence Calculated a Table of the Inclination of the Magnetical Needle in all Latitudes.

This Instrument hath also been lately commended to the Consideration of this present Age, by the *Vertuosi*, or *Royal Society*, in the Philosophical Transaction, *Vol.* 2. *Numb.* 24.

So that it may appear by all these Testimonies, that this Instrument hath somewhat of Excellency in it, and therefore may be thought worthy of our Consideration and Practice.

The

The Deſcription of the Inclinatory Needle.

This Inſtrument containeth theſe parts,

1. A ſtrong Braſs Ring wherein the Needle doth hang upon two ſmall Pevits or Axeltrees, between two Bridges, and this Braſs Ring hath on each ſide a Grove for a Glaſs to be put on each ſide; and formerly there uſed to be a Ring on the top to hold it on your finger, but this way being not altogether ſo convenient for uſe at Sea, therefore we have contrived it after a more convenient manner for Obſervation at Sea, and to hang like another Compaſs, in a Box, that it may be plyable to every motion of the Ship according to this following Figure.

The Magnetical Needle that hangs on his Pevits, between the two Bridges in this Instrument, before it hath received any virtue from the Loadstone, doth hang in *Equilibrio*, and will turn to any Position whatsoever; but after it hath received the Magnetick Vigor from the Stone, it then becomes subordinate to the powerful commands of the great Magnet the Earth, which being placed to its Magnetical position, *i. e.* parallel to the Magnetical Meridian, then will the Needle respect its true point of Elevation or Depression, according to the Latitude of the place where it is used, which may further appear by this ensuing Table.

A Table of the Magnetical Inclination of the Inclinatory Needle.

Lat. of place.	Inclination.		Magnetical	Lat. of place.	Inclination.		Magnetical	Lat. of place.	Inclination.		Magnetical	Lat. of place.	Inclination.		Magnetical	Lat. of place.	Inclination.		Magnetical
D.	D		M.	D.	D.		M.	D.	D.		M.	D.	D.		M.	D.	D.		M.
1	2		11	16	30		45	31	52		27	46	68		24	61	79		29	76	86		28
2	4		20	17	32		24	32	53		41	47	69		17	62	80		4	77	86		48
3	6		21	18	34		00	33	54		53	48	70		9	63	80		38	78	87		8
4	8		31	19	35		36	34	56		4	49	70		59	64	81		11	79	87		26
5	10		34	20	37		9	35	57		13	50	71		48	65	81		43	80	87		44
6	12		34	21	38		41	36	58		21	51	72		36	66	82		13	81	88		1
7	14		32	22	40		11	37	59		28	52	73		23	67	82		43	82	88		17
8	16		28	23	41		39	38	60		33	53	74		8	68	83		12	83	88		33
9	18		22	24	43		6	39	61		37	54	74		52	69	83		40	84	88		47
10	20		14	25	44		30	40	62		39	55	75		35	70	84		7	85	89		1
11	22		4	26	45		54	41	63		40	56	76		17	71	84		32	86	89		14
12	24		52	27	47		15	42	64		39	57	76		57	72	84		57	87	89		27
13	25		38	28	48		36	43	65		38	58	77		34	73	85		21	88	89		39
14	27		12	29	49		54	44	66		35	59	78		15	74	85		44	89	89		50
15	29		4	30	51		11	45	67		30	60	78		53	75	86		7	90	90		00

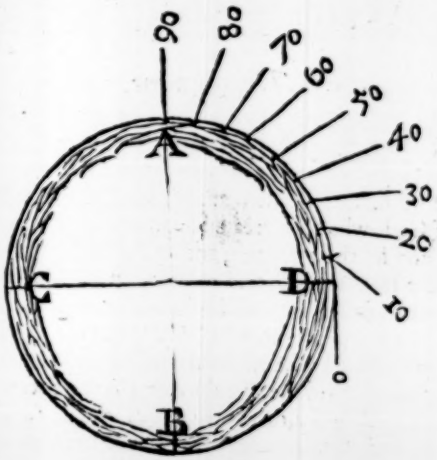
There-

Therefore being in any part of the World, and you ſet this Inſtrument directly North and South by another Compaſs, being placed at a competent diſtance out of the Orbs of Attraction, then will the North or South end of the Needle dip to a certain Angle, which Angle being ſought in this precedent Table, under the Title of *Magnetical Inclination*, right againſt it in the Column next to it under the Title of *Latitude of Places*, ſhall be ſhewn the Latitude of the preſent place.

Example.

Suppoſe you have rectified your Inſtrument North and South, as before, and find the North end of the Needle to be depreſſed below the Horizon to an Angle of 72° 36′; then if you look this Angle in the Table, you will find it in the fifth and ſixth Column, under the Title of *Magnetical Inclination*; and in the fourth Column, under the Title of *Latitude of Places*, you will find 51 degrees, which will be the Latitude of the place. The ſame is to be underſtood in South Latitude, only that then the South end of the Needle will be depreſſed, and the Uſe will be the ſame.

The Natural Reaſon of this may be very lively illuſtrated by the application of a ſmal ſowing Needle round a *Terrella*, or round a *Load-ſtone*, in the manner of this following Figure.



Let the Figure A B C D, represent a *Terrella*, or round Load-stone, A the North-Pole, B the South-Pole, A B the Meridian, C D the Equinoctial; Now if you suppose that the Quadrant A D were divided into 90 equal parts, shewing the several Latitudes of places upon the Earth; Then if you apply a Needle to the point D, it will conform it self to a parallel position to the Line A B, but if moved further to 10 degrees, then shall it have a sensible Angle, and so to 20, 30, *&c.* until it cometh to 90 degrees, and doth erect it self perpendicular upon the very Pole: from which experiment may be gathered the natural reason of the position of the *Magnetical Needle* to the great Magnet the Earth, as this small sowing Needle hath to this *Terrella*, or little Earth; or if a small Magnetical Needle be applyed after the same manner to this Stone, it will perform the same Conclusions as the sewing Needle doth.

SECT. VIII.

A short Appendix, shewing some of the secret Properties of the Load-Stone.

The Proeme.

THE Nature, Powerfulness, and strange Properties of the Load-stone are such, that the more they are known, the more they are justly to be admired, in their lively expressing the infinite Power and Goodness of God, who hath created so pretious a Jewel for the profitable use of Man, and for the enlarging and setting forth of his own Glory, especially in that assistance it affords to man, in the discovery of the whole Universe, which is the work of his hands, and his mighty wonders in the deep Waters; the properties not only serving for Maritime Affairs, but also in Travelling by Land in vast and solitary Desarts; for movable Sun-Dials in all places of the World; for the more ready and exact Chorography of any Country, or the true plotting of any ground, and for the following of any Mineral Vein that is void of Iron under the Earth; and also for Coal-Mines, with several other necessary Uses, retaining in

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it self as it were the Mirror of Philosophy, manifested by its Sympathetical Coition, and Antipathetical Repulsion; with many other Occult Operations, very admirable to behold, two especially that are treasured up in its dusky Entrails, one of Attraction, the other of Direction; it hath Substance, Virtue, and Operation, serving to many good purposes: therefore this Stone of all others may be accounted the most precious, wherein the Majesty of Nature doth most appear; which admirable Treasure God hath vouchsafed to reveal unto the weak knowledge of man now towards the end of the World, being so plain to the meanest capacity; and that out of a base contemptible and dead Creature, as it seemeth to be, and yet filled with such Excellent and Wonderful Virtue, that all the Gems in the World have not the like.

Claudianus, a famous Poet, twelve hundred years since, saith as much in the commendation of the Magnet, when as yet the Sireditial or Iron-drawing property thereof was only known;

——— *Lapis est Cognomine Magnes*
Decolor obscurus vilis, &c.

And again,

Sed nova si nigri videat, miracula saxi,
Tunc superat pulchros cultos, & quicquid Eois
Indus littoribus rubra scutatur in alsa.

But what would he have said, had he seen the true Closet of all Magneticall Miracles unlocked, as now it is at this day!

Of the Name of the Stone, and of the Colour, and from whence they come, and how they were first found.

This Stone is called *Magnes*, used under that promiscuous appellation, both by the *Greeks* and *Latines*; and as *Lucretius* writeth, the name is derived from the Country *Magnesia*.

The Greeks *do call it* Magnes *from the place:*
For that the Magnets *Land it doth imbrace.*

Plate

Plato ſaith, ſome call it *Lapis Heraclius*, from the Name of *Heraclea*, a City of *Lydia*, where it was firſt diſcovered, and upon the ſame account is called *Lapis Lydia*.

Theophraſtus, in his Book of Stones, for the ſame reaſon, calleth it *Herculeum*: Others think it denominated from *Hercules*.

Nicander thinks the Stone ſo called, and ſo doth *Pliny* from him, from one *Magnes* a Shepherd; for it is reported, that he found it by his Hob-naild Shooes, and his Shepherds Crook that ſtuck to it, when he fed his Flocks in *India*, where he was a Shepherd.

Others call it *Siderites*, which in Greek ſignifies Iron. By us it is called a Load-ſtone, alluding to the two Stars in the Tail of the Cœleſtial Bear, called *Helice* and *Cynoſura*, which were antiently called Load-ſtars, or Leading-ſtars; and therefore this Stone bears that appellation which now performs the ſame office.

This Magnet, or Load-ſtone, is found in diverſe parts of the World, and moſt commonly in Iron Mines; and though it be pondrous and weighty, yet it is not found to be of the Iron Ore, neither containeth in it any mettal of it ſelf, but hath a certian affinity and ſympathy with Iron and Steel.

Of theſe there are of divers ſorts, different each from other, as well in goodneſs as in colour, weight and force, but not in property (although many have judged that the cauſe of the variation of the Needle, to be according to the diſtance of the Mine from whence the Stone was taken, and the place where it is uſed, but there is no ſuch thing) for all Stones whatſoever have all one point of direction.

The firſt and beſt ſort of theſe Stones come out of *Eaſt-India*, from the Coaſt of *China* and *Bengala*, and are of the colour of Iron, or Sanguine colour: Theſe Stones are maſſy and weighty, and will draw or lift up the juſt weight of themſelves in Iron or Steel; and theſe are of the fineſt ſort, and are commonly ſold for their weight in Silver in the *Eaſt-Indies*, where they grow, becauſe the beſt or fineſt are very rare to be found, for it is commonly an entire Stone lying in the Earth by it ſelf, and no piece or part of any other.

There is alſo another ſort of a rediſh colour, found in *Arabia*, and the Red Sea; growing broad and flat, much like unto a Tile of a Chimney Hearth: theſe are not ſo weighty as thoſe of *China*, but are very near as good, and the virtue continueth long on the Compaſs or Needle that is touched upon theſe Stones.

There are of theſe Stones likewiſe in the *Levant*, in the Iſland called *Elba*,

Elba, hard by a Town in that Island called *Porta Feraro*, and are called there *Calamita Preta*, that is to say the *Black Magnet*; because there is another sort that are white and light, like unto a piece of dry Fullers Clay, and are called *Calamita Blanca*. These black Stones of *Elba* are mingled with white Veins: They are of no great force, nor their virtue of long continuance.

Also there are of these Stones in high *Almany*, that are full of holes like a Hony Comb, and lighter than the other, but better than they; these are of an Iron Colour.

Another sort there are in *Norway*, in the Iron Mines, as in *Longsound*, and other places; their Colour is black mixed with gray: These are also of an indifferent force.

There are also some in the Mines of *Caraca*, and *Cantabria* in *Spain*; and some there are found in *England*, but of no great force.

There are some found also in *Bohemia*, and several other places.

All these Stones are different one from another as well in force, as in Colour and Weight, yet all of one Operation in the Needle, shewing all one point of direction: which is a most wonderful and admirable providence of God to cause it so to be, for infinite would the distractions be if it were otherwise in the practical use of the Compass: For true it is, that God is mighty and marvellous in all his works; and truly his power is greatly shewn in this wonderful Miracle of Nature, as in any Stone in the whole Creation.

Of the Attractive Virtue of the Load-Stone.

That this Stone hath an attractive Operation, is apparently manifest; for if you apply a piece of Iron unto either of the Poles thereof, it will there hold it, and at a distance will also dray or attract a small piece of Iron, according to the vigor or imbecility of the Stone; but what strength soever it hath, it may be artificially improved to be greater than can by it self be discovered, which is to be performed by applying a smooth and bright piece of Iron to either Pole of the Stone, and it will immediately deliver its virtue unto it, the virtue being herein contracted in this piece of Iron, the Stone doth manifest it self to have ten times more strength; for this Cause therefore are Load-stones capped with Iron, for the artificial augmentation of their strength.

And

And this virtue is freely communicated from it self to any thing else that is capable of its reception, so that a piece of Steel, having received strength from the Stone, that will also attract another piece of Steel in proportion to that virtue that it hath received.

This experiment I have often tried upon my Load-stone, for by touching of a Knife upon it, it shall take up a Key of two ounces weight; and that within the Sphere of the Stone it shall deliver the virtue into a piece of Iron, and not touch the Stone at all; and likewise over the Stone it shall cause one piece of Iron to hang to another; so wonderful is the attractive quality of this Stone, manifested in these and the like Experiments.

Of the Sympathetical and Antipathetical Property of the Load-Stone.

If a Magnetical Needle being touched upon the Load-stone, the North and South end of this Needle will apply it self respectively to those Poles from whence it received its Magnetical Life, to wit, the North end of the Needle will fly to the North end of the Stone, and the South end of the Needle will fly to the South end of the Stone, which denotes their mutual Sympathy; but putting the North end of the Stone to the South end of the Needle when it is upon a Pin, the South end of the Needle will immediately fly away; and if you put the South end of the Stone to the North end of the Needle, it will also discover an opposite and antipathetical Nature.

But a contrary Operation there is yet in the two Needles to that of the Load-stone; for if one of the Needles being hung upon a Pin, and you apply the North end of the one Needle to the North end of that upon the Pin, it shall immediately fly away, which denoteth a contrary Operation in the Needle to that of the Load-stone, and the South end of one Needle will immediately come to the North end of the other.

The same property of Sympathetical Coition, and Antipathetical Repulsion, is also discovered by two Load-stones floating in two little Boots, in a great Bason of Water, the two Poles of either Stone being disposed parallel to the plain of the Horizon; and if you put both the South Poles together, they shall avoid the Contact of one another by a natural antipathy; but if the North Pole of one be direct to the South Pole of the other, they

they will immediately manifeſt their natural Sympathy one to another, and will cleave together by a ſtrong attraction.

This is alſo apparently evident between the great Magnet the earth, and a Load-ſtone, for if you put a Load-ſtone in a ſmall ſtring, and let it hang in the Air, or elſe to float in the Water in a wooden Diſh, and putting the North end of the ſmall Magnet towards the North end of the great Magnet the Earth, it ſhall immediately change its poſition, and turn its North Pole towards the South Pole of the ſaid great Magnet.

Of the Conſequences that follow the various dividing and cutting of the Load-ſtone.

IF a Load-ſtone be confuſedly broken by violence into many pieces, each of the individual pieces ſhall be an entire Load-ſtone, having both its Poles diſtinctly of it ſelf, with all the other properties that were in the Stone before it was broken.

But if a Loadſtone be divided in the midſt, between the two Poles, in the Equinoctial, then it is abſolutely two entire Load-ſtones, and thoſe parts which were the Equinoctials before, are now become two Poles, and the two Poles that were Poles before, do continue the ſame.

But if a Stone be cut meridionally quit through the two Poles thereof, ſo that one Axes is now converted into two, and each of them remove into each Stone, ſo that it is alſo become two intire Load-ſtones, and the Axis of them will retire into the gravity of either piece, directly parallel to the Axis, that was before the Stone was divided; and if you joyn theſe two pieces together again, the two Axes will again become one, which is moſt admirable to behold.

But if you cut off a piece of the Stone at the very Pole, in a Parallel Section, the virtue of that piece will immediately retire from it unto the maine Stone, and will ſcarcely have any virtue at all therein; but applying this ſmall piece that was cut off, to the ſame place again, the Stone will forthwith impart the ſame virtue as was before, into this piece ſo cut off, ſo long as it doth abide in that place; but when it is removed, it doth again recall its virtue from the ſaid piece. This I have experienced in a Stone of a very conſiderable piece.

And in the ſame manner, if you apply a weak Stone to the Poles of a

ſtrong one, the ſtrong Stone will impart of its virtue to the weak Stone, making it to be as ſtrong as it ſelf, ſo long as it is its Neighbour; but when this weak Magnet deſerts this neighbourly propinquity, the ſtrong Magnet will draw its virtue to it ſelf again, and will truſt it no further than the power of its recall.

To find the Poles of a Stone.

THere are ſeveral wayes for the performance of this Experiment;

Firſt, You may have a thin piece of Steel about an inch in length, and ⅛ of an Inch broad; this piece of thin Steel being bent circular and laid on the Stone, will immediately lye parallel to the Axis of the Stone, and direct which way the Poles do lye. Which being diſcovered near where they lie, you may find them more exactly, by a ſmall piece of a ſewing Needle, which being laid on the Stone, if it be near either of the Poles, will elevate one end thereof; then move it farther and farther till it doth erect it ſelf perpendicular, and that very point will be the Pole of the Stone.

Now to know which Pole it is, you may apply a ſmall Needle of a Dial to it, and if the Pole draw the North end of the Needle, then is that the North Pole of the Stone, and the contrary.

Or otherwiſe, You may find the Pole by a ſewing Needle and a Thread, by hanging it over the Stone where you ſuppoſe the Pole to be, and keep it a little ſhort from the Stone, and the end of the Needle will directly point to the Pole of the Stone,

Whether Onions or Garlick do obſtruct the Operation of the Load-Stone.

THere is a common received Opinion, that if a Load-ſtone be rubbed over with Garlick or Onions, that it will obſtruct the virtue thereof; or if a Kniſe being touched upon the Load-ſtone, and afterwards cut an Onion or Garlick therewith, that it will immediately looſe its virtue.

This conceit hath alſo been countenanced by the Antients; but if you

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are pleaſed to make trial of it, you will find it to be but a meer fallacy. It is alſo as falſe that the Diamond doth hinder the virtue of the Load-ſtone while it is near it.

A delightful Experiment performed by the Load-Stone, *repreſenting the Engaging of two Armies in Battel.*

FOR the performance hereof, you muſt have a Braſs or Pewter plate, and upon this Plate put on ſeveral little heaps of the filings of Iron, with ſome ſhort bitts of ſewing Needles, and put them in order of a Battel, one main Body againſt another, alſo with their right and left Wings, and their Forlorne Hopes; this being done, bring the Load-Stone under the plate with one of the Poles upward, and put it firſt toward one of the right Wings of the Army, and they will immediately receive an Alarm, and as it were, ſtand to their Arms; then move the Stone toward the other Wing of the Enemy, and they alſo will receive the like Alarm; and then by moving the Stone to and fro under the Plate, you will put both parties in a motion, in a Charging poſture, and one to charge the other in a deſperate Engagement, and one to come within the other, and ſo you may at laſt engage the main Bodies of the Armies; and there you may ſee that ſometimes they are Conquerours, and ſometimes conquered, which is cauſed by the ingenious motion of the Stone with your hand under the Plate; and the ſhort bits of the Needles may repreſent their Generals and Commanders, which will be very full of action, where you may ſee ſometimes that there will be twenty or more of the Common Soulders to fall foul of the ſaid Commanders: And if between theſe Armies you put ſmall Breaſt-works and Trenches made with Sand, and filings put in the Trenches, you will then have repreſented the ſudden riſing of them one againſt another, as if they lay in ambuſh, waiting for an opportunity againſt their Enemies.

To make a Sewing Needle ſwim upon the ſurface of the Water, and to play up and down like a Fiſh; and alſo to find out the Magnetical Meridian.

Take a ſmall Sewing Needle, and touch the two ends thereof upon the two Poles of the Stone; and having a glaſs of Water before you, take the Needle very lightly between your finger and thumb, and lay it lightly on the Surface of the Water, ſo that it break not through, and there it will lye; then take a Knife that hath been touched with the Load-ſtone, and bring it to and again upon the edge of the Glaſs, and the Needle will follow it up and down; and will play up and down on the ſuperficies of the Water like a Fiſh, and then take away the Kniſe, and the Needle will immediately poſite it ſelf to the Meridian, pointing due North and South.

Such an inferiour inſtrument as this may ſtand men in great ſtead, in time of great Straits and Exigences, if they ſhould be at Sea, and their Compaſs be taken from them; for if you put a Needle, being toucht, through a ſmall piece of Cork, it will then perform this effect exceeding well in all Storms and Tempeſts whatſoever, being born up by the Cork on the top of the Water, and the poſition thereof will be continually in the Meridian.

To infuse Magnetical Virtue into a Needle without the help of the Load-Stone.

IRon being a Mineral of the Earth, and having a Sympathetical quality with the *Load-stone* | equiring this *Verticity* from the *Magnatism* of the *Earth*, being dispensed according to the various positions thereof; for all *Iron*, whose position is *Parallel* to the *Axis* of the World, or *Perpendicular* to the *Horizon*, the upper part thereof shall have or *North Virtue*, and the lower part *South Virtue*, as Bars in Windows, Casements, Tongs and Fire-Forks, and all such things, *&c.* And according to the length of the time of the *position* of any such piece of *Iron*, the stronger *Virtue* it doth contract; so that once I made *Experiment* upon a smooth piece of *Iron*, which had for several years been in a *perpendicular* posture, and I filed the upper end thereof bright, and touched a small new Needle thereon, the *South* end I touched upon the *North* or upper part of the *Iron*, and the *North* end upon the *South* or lower end of the *Iron*, and I found the Needle to play indifferently well, and to conform it self to the *Magnetical Meridian*.

The Reason of this is from the Nature of the *Iron*, it being a *Mettal* deducted out of the *Load-stone*, or out of a *Mine* of that kind; the best *Iron-Mine* and *Load-stone* is the same thing; for it being placed Artificially in the *Air*, or upon the *Water*, moveth *North* and *South*, attracteth other *Iron* unto it, and performeth the same *Conclusions* as the *Magnet* it self.

A delightful Experiment performed with two Sewing Needles, being touched upon the Load-Stone.

IF you touch two *Sewing Needles* contrary one to another, that is to say, the point of the one *Northerly*, and the point of the other Southerly, and put them into two small pieces of Cork, and put them thus in.

in a Baſon of *Water*, one at the one ſide, and the other at the other ſide of the Baſon, you ſhall ſee them as it were quickned with a *Vital Spirit*, even ſo to move one towards the other; at the firſt, fair and ſoftly, but when they draw near, they will ruſh together with great violence, the point of the one ſtriking preciſely at the point of the other: you muſt place the Needle that is touched from the *North*, on the *South* ſide of the Baſon, and the other on the other ſide, otherwiſe the heads and not the points will run together.

Of Cementing and Piecing of Load-Stones.

IF a *Load-ſtone* chance to be broken, it will not at all be detrimental to the *Virtue* of the *Stone*, provided that they be joyned together in the ſame place where they were broken off, which may be ſet together very ſtrongly, by the help of a *Cement* prepared for that purpoſe, which is thus made.

Take the fine pouder of *Load-ſtone*, and half ſo much pouder of Brick made very ſmall, one part of *Burgundy Pitch*, half ſo much *Roſin*, and a ſmall portion of unwrought *Wax*; Mingle theſe over a ſoft fire, and heat the two pieces of the *Load-ſtone* very hot, then take of this *Cement*, while it is hot, and lay it on very thin upon the two pieces, and then joyn them together very hard, and as cloſe as you can, and let it ſo ſtand until it be cold, and you ſhall have it fully as ſtrong as if it were an entire *Stone*, and not to be ſevered but by a great fire.

A Table

Beginning with 1672.

M.	Moons Age.	D.	H.	M
January.	Full moon.	03	23	30
	Last quarter	11	10	24
	New moon.	18	12	02
	First quarter	26	16	15
February.	Full moon.	02	12	22
	Last quarter	10	07	27
	New moon.	18	02	47
	First quarter	24	23	32
March.	Full moon.	03	02	27
	Last quarter	11	03	29
	New moon.	18	14	38
	First quarter	25	06	36
April.	Full moon.	01	17	34
	Last quarter	09	21	01
	New moon.	16	23	51
	First quarter	23	14	27
May.	Full moon.	01	08	54
	Last quarter	09	11	18
	New moon.	16	07	10
	First quarter	22	23	56
	Full moon.	30	23	44
June.	Last quarter	07	22	26
	New moon.	14	13	47
	First quarter	21	11	53
	Full moon.	24	14	45
July.	Last quarter	07	06	31
	New moon.	13	20	57
	First quarter	21	02	11
	Full moon.	29	04	56
August.	Last quarter	05	12	48
	New moon.	12	05	38
	First quarter	19	19	04
	Full moon.	27	18	16
September.	Last quarter	03	18	29
	New Moon.	10	17	01
	First quarter	18	13	48
	Full moon.	26	06	34
October.	Last quarter	03	00	56
	New moon.	10	07	01
	First quarter	18	09	39
	Full moon.	25	17	48
November.	Last quarter	01	09	27
	New moon.	08	23	44
	First quarter	17	04	26
	Full moon.	24	04	24
	Last quarter	30	20	41
December.	New moon.	08	18	31
	First quarter	16	20	55
	Full moon.	23	14	42
	Last quarter	30	11	04

Four Eclipses this Year, two of the Sun, and two of the Moon.

1. Of the Sun, *Feb* 18. 02*h*. 47*m*. and is visible near the *Caspian Mountains*, *Nova Granada*, *Azores*, *Brasil*. 2. Of the Sun, *Aug*. 12. 05*h*. 38*m*. *P.M.* and is visible in the North part of *America*, *Nova Francia*, *Mexico*, *Cuba*. 3. Of the Moon, *March* 3. 02*h*. 27*m*. *P.M.* visible in *New Guiny*, *Japan*, *Cathay*, *New Spain*, *Persia*, *Tartaria*, *Egypt*, *Muscovia*, *Russia*, *Lapland*. 4. Of the Moon, *Aug* 27. 18*h*. 16*m*. *P.M.* visible in *Peru* and *Jucatan*, *Mexico*, *Florida*, *Barbary*, *Mediterranean Sea*, *France*, West part of *Germany*, North of *America*, St. Martins, *Iseland*, *Friezland*, *Greenland*

A Table of the Moons Age for the Year

1673.

M.	Moons Age.	D.	H.	M
January.	New Moon.	07	14	04
	First quart.	15	09	55
	Full moon.	22	01	18
	Last quart.	29	04	10
February.	New moon.	06	09	28
	First quart.	13	19	44
	Full moon.	20	12	22
	Last quart.	27	23	04
March.	New moon.	07	00	41
	First quart.	15	03	06
	Full moon.	21	23	58
	Last quart.	29	11	53
April.	New moon.	06	13	25
	First quart.	13	09	13
	Full moon.	20	12	20
	Last quart.	28	13	05
May.	New moon.	05	22	21
	First quart.	12	15	18
	Full moon.	20	01	29
	Last quart.	28	05	22
June.	New moon.	04	07	10
	First quart.	10	22	15
	Full moon.	18	15	47
	Last quart.	26	18	48
July.	New moon.	03	14	07
	First quart.	10	07	12
	Full moon.	18	07	01
	Last quart.	26	05	26
August.	New moon.	01	21	14
	First quart.	08	19	02
	Full moon.	16	22	48
	Last quart.	24	14	03
	New moon.	31	05	25
September.	First quart.	07	10	23
	Full moon.	15	14	10
	Last quart.	22	21	35
	New moon.	29	15	29
October.	First quart.	07	05	11
	Full moon.	15	04	46
	Last quart.	22	04	58
	New moon.	29	04	02
November.	First quart.	06	02	21
	Full moon.	13	18	07
	Last quart.	20	13	05
	New moon.	27	19	29
Decemb.	First quart.	05	23	36
	Full moon.	13	06	24
	Last quart.	19	22	27
	New moon.	27	13	34

Two Eclipses of the Sun.

1. *Feb.* 6. 09*h.* 28*m.* P.M. Visible at the *Cape of Good Hope, New Guiny, California, New Spain, Mexico, Florida, Virginia, New France.*

2. *Aug.* 1. 21*h.* 14*m.* P.M. Visible in the *Atlantick-Sea, Arabia, India, China, New Holland, Madagascar.*

A Table of the Moons Age for the Year 2

1674.

M.	Moons Age.	D.	H.	M
January.	First quarter	04	18	26
	Full moon.	11	17	32
	Last quarter	18	09	57
	New moon.	26	08	52
February.	First quarter	03	09	53
	Full moon.	10	03	41
	Last quarter	16	23	37
	New moon.	25	03	33
March.	First quarter	04	21	37
	Full moon.	11	13	09
	Last quarter	18	15	48
	New moon.	26	20	08
April.	First quarter	03	06	03
	Full moon.	09	22	24
	Last quarter	17	09	30
	New moon.	25	09	53
May.	First quarter	02	12	18
	Full moon.	09	08	22
	Last quarter	17	03	30
	New moon.	24	21	09
	First quart.	31	17	21
June.	Full moon.	07	19	35
	Last quarter	15	20	40
	New moon.	23	06	30
	First quarter	29	22	27

M.	Moons Age.	D.	H.	M
July.	Full moon.	07	09	35
	Last quarter	15	12	12
	New moon.	22	14	35
	First quarter	29	05	14
August.	Full moon.	05	23	29
	Last quarter	14	01	58
	New moon.	20	22	13
	First quarter	27	14	51
September.	Full moon.	04	15	46
	Last quarter	12	13	52
	New Moon.	19	06	14
	First quarter	26	04	13
October.	Full moon.	04	08	38
	Last quarter	12	00	18
	New moon.	18	15	35
	First quarter	25	22	03
November.	Full moon.	03	01	27
	Last quarter	01	09	17
	New moon.	17	03	06
	First quarter	24	18	50
December.	Full moon.	02	17	24
	Last quarter	09	17	30
	New moon.	16	17	17
	First quarter	24	16	38

Two Eclipses of the Sun, and two of the Moon.

1. Of the Sun, *Jan.* 26. 08*h.* 52*m.* P.M. Visible at the *Cape of Good Hope, California, New Britain.* 2. Of the Sun, *July* 22. 14*h.* 35*m.* P.M. Visible at the *Cape of Good Hope, New Holland, China,* and the South Sea. 3. Of the Moon, *Jan* 11. 17*h.* 32*m.* P.M. Visible in the Tartarian Ocean, *Natolia,* Mediterranean Sea, *Egypt, Pacifick-Sea.* 4. Of the Moon, *July* 7. 09*h.* 35*m* P.M. Visible in *Japan, Lythvania,* Moscovy, *Poland, Germany, Mayork, Minyork, Barbary, Guiny.*

A Table of the Moons Age for the Year

1675.

M.	Moons Age.	D.	H.	M
January.	Full moon.	01	07	39
	Last quarter	08	01	42
	New moon.	15	09	41
	First quarter	23	13	18
	Full moon.	30	19	47
Febr.	Last quarter	06	10	56
	New moon.	14	03	25
	First quarter	22	06	30
March.	Full Moon.	01	05	43
	Last quarter	07	21	46
	New moon.	15	21	00
	First quarter	23	21	05
	Full moon.	30	14	09
April.	Last quarter	06	10	39
	New moon.	14	13	28
	First quarter	22	07	27
	Full moon.	28	21	58
May.	Last quarter	06	01	15
	New moon.	14	04	20
	First quarter	21	12	48
	Full moon.	28	06	15
June.	Last quarter	04	17	11
	New moon.	12	17	22
	First quarter	19	19	35
	Full moon.	26	15	46
July.	Last quart.	04	10	15
	New moon.	12	04	34
	First quart.	19	00	09
	Full moon.	26	03	10
August.	Last quarter	03	03	13
	New moon.	10	14	14
	First quarter	17	05	53
	Full moon.	24	16	46
September.	Last quarter	01	20	22
	New moon.	08	23	03
	First quarter	15	14	03
	Full moon.	23	08	40
October.	Last quarter	01	11	54
	New moon.	08	07	44
	First quarter	15	01	36
	Full moon.	23	02	27
	Last quarter	31	01	27
November.	New moon.	06	18	31
	First quarter	13	16	59
	Full moon.	21	21	15
	Last quarter	29	12	34
Decemb.	New moon.	06	04	14
	First quarter	13	03	49
	Full moon.	21	15	22
	Last quarter	28	21	51

Five Eclipses, Two of the Sun, and three of the Moon.

1. Of the Sun, *June* 12. 17*h*. 22*m*. P.M. Visible in *Greenland, Tartaria, Cathay.* 2. Of the Sun, *Decemb.* 6. 4*h*. 14*m*. P.M. Visible in the *Æthiopean Sea, Cape of Good Hope, England, Spain,* and *Barbary.* 3. Of the Moon, *Jan.* 1. 7*h*. 39*m*. P.M. Visible in *Guiny, Moreco, Friezland, Groenland, Japan, Java, Indian Sea, Brasil, Nova France, Nova Albion.* 4. Of the Moon, *June* 26. 15*h*. 46*m*. P.M. Visible in the *Red Sea, Syrean Sea, Baltick Sea, Norway Sea, New Spain,* St. *Lawrence.* 5. Of the Moon, *Decemb.* 21. 15*h*. 22*m*. P.M. Visible in *Groenland, Tartaria, Persia, Bazorion Sea, Barbary,* Magellanica, *California, Cyprus.*

1676.

M.	Moons Age.	D.	H.	M
January.	New Moon.	04	16	55
	First quart.	12	08	52
	Full moon.	20	07	20
	Last quart.	27	05	54
February.	New moon.	03	06	59
	First quart.	11	06	15
	Full moon.	18	20	27
	Last quart.	25	13	44
March.	New moon.	03	22	10
	First quart.	12	01	52
	Full moon.	19	06	46
	Last quart.	25	22	02
April.	New moon.	02	13	59
	First quart.	10	17	56
	Full moon.	17	15	06
	Last quart.	24	07	35
May.	New moon.	02	05	57
	First quart.	10	06	03
	Full moon.	16	22	23
	Last quart.	23	18	44
	New moon.	31	21	27
June.	First quart.	08	14	46
	Full moon.	15	05	39
	Last quart.	22	08	09
	New moon.	30	11	51

M.	Moons Age.	D.	H.	M
July.	First quart.	07	21	18
	Full moon.	14	13	40
	Last quart.	21	23	58
	New moon.	30	00	54
August.	First quart.	06	02	46
	Full moon.	12	23	20
	Last quart.	20	18	01
	New moon.	28	12	32
September.	First quart.	04	08	36
	Full moon.	11	11	36
	Last quart.	19	13	05
	New moon.	26	23	17
October.	First quart.	03	15	50
	Full moon.	11	02	45
	Last quart.	19	07	36
	New moon.	26	09	34
November.	First quart.	02	01	23
	Full moon.	09	20	49
	Last quart.	18	00	18
	New moon.	24	19	58
December.	First quart.	01	14	14
	Full moon.	09	16	27
	Last quart.	17	14	08
	New moon.	24	06	34
	First quart.	31	06	30

Two Eclipses of the Sun.

1. *May* 31. 22*h*. 27*m*. *P.M.* Visible in *Groenland*, *Terra Nova*, *Hispaniola*, *Cuba*, *Lybia*, *Newmidia*, *Crete*, *Cyprus*, *Mediterranean Sea*, *Arabia*, *Indian Sea*. 2. *Novemb*. 24. 19 *h*. 58 *m*. *P. M.* Visible in the *Æthiopian Sea*, *Madagascar*, *New Guiny*.

1677.

M.	Moons Age.	D.	H.	M
January.	Full moon.	08	11	41
	Last quart.	16	01	23
	New moon.	22	17	35
	First quart.	30	01	41
February.	Full Moon.	07	04	50
	Last quart.	14	10	20
	New moon.	21	05	25
	First quart.	28	22	19
March.	Full moon.	08	19	05
	Last quart.	15	17	25
	New moon.	22	17	57
	First quart.	30	18	04
April.	Full moon.	07	06	29
	Last quart.	13	23	43
	New moon.	21	07	47
	First quart.	29	11	18
May.	Full moon.	06	15	34
	Last quart.	13	06	29
	New moon.	20	22	27
	First quart.	29	01	35
June.	Full moon.	04	23	04
	Last quart.	11	14	42
	New moon.	19	13	38
	First quart.	27	14	53

M.	Moons Age.	D.	H.	M
July.	Full moon.	04	05	50
	Last quart.	11	01	29
	New moon.	19	04	52
	First quart.	26	21	58
August.	Full moon.	02	12	57
	Last quart.	09	15	02
	New moon.	17	19	18
	First quart.	25	05	27
	Full moon.	31	21	28
September.	Last quart.	08	09	04
	New moon.	16	09	21
	First quart.	23	12	08
	Full moon.	30	08	39
October.	Last quart.	08	04	44
	New moon.	15	22	49
	First quart.	22	19	06
	Full moon.	29	22	56
November.	Last quart.	07	01	11
	New moon.	14	11	15
	First quart.	21	03	24
	Full moon.	28	16	14
Decemb.	Last quart.	06	20	40
	New moon.	13	22	44
	First quart.	20	14	09
	Full moon.	28	11	15

Two Eclipses of the Sun, and two of the Moon.

1. Of the Sun, *May* 20. 22*h*. 27*m* P.M. Visible at St *Helena*, S. *Mary*, *Madagascar*, St. *Martins*, *Britania*. 2. Of the Sun, *Nov.* 14. 11*h*. 15*m*. P.M. Visible in *China*, *Japan*, *South Sea*, *America*, *New Granada*, St. *Thomas*, *New Spain*. 3. Of the Moon, *May* 6. 15*h*. 34*m*. P.M. Visible in *Brasil*, St. *Lawrence*, *Peland*, *Iseland*, *New Spain*, *Norway*, *Cape of Good Hope*, *Barbary*, *Friezland*, *North America*. 4. Of the Moon, *Octob.* 29. 22*h*. 56*m*. P.M. Visible in *Magellanica*, *Iseland*, *New France*, *Florida*, *Cuba*, *East Sea*, *Malabar*, *Caspian Sea*.

1678.

M.	Moons Age.	D.	H.	M
January.	Last quarter	05	13	41
	New moon.	12	09	08
	First quarter	18	03	45
	Full moon.	27	03	33
February.	Last quarter	04	03	27
	New moon.	10	19	01
	First quarter	17	20	05
	Full moon.	26	00	13
March.	Last quarter	05	13	30
	New moon.	12	04	53
	First quarter	19	14	05
	Full moon.	27	15	47
April.	Last quarter	03	19	41
	New moon.	10	15	28
	First quarter	18	08	25
	Full moon.	26	04	38
May.	Last quarter	03	02	03
	New moon.	10	02	59
	First quarter	18	02	07
	Full moon.	25	14	51
June.	Last quarter	01	07	11
	New moon.	08	15	44
	First quarter	16	18	20
	Full moon.	23	23	06
	Last quarter	30	13	28

M.	Moons Age.	D.	H.	M
July.	New moon.	08	05	37
	First quart.	16	08	38
	Full moon.	23	06	07
	Last quart.	29	22	05
August.	New moon.	06	20	38
	First quarter	14	20	49
	Full moon.	21	13	16
	Last quarter	28	10	00
September.	New moon.	05	12	44
	First quarter	13	06	53
	Full moon.	19	21	38
	Last quarter	27	01	23
October.	New moon.	05	05	09
	First quarter	12	15	23
	Full moon.	19	08	09
	Last quarter	26	20	07
November.	New moon.	03	21	19
	First quarter	10	23	12
	Full moon.	17	21	10
	Last quarter	25	17	35
Decemb.	New moon.	03	11	52
	First quarter	10	07	14
	Full moon.	17	12	42
	Last quarter	25	15	12

Five Eclipses, three of the Sun, and two of the Moon.

1. Of the Sun, *April* 10. 15*h*. 28*m*. P.M. Visible in *Tartaria*. 2. Of the Sun, *Octob*. 5. 5*h*. 9*m*. P.M. Visible in *Magellanica*, and *Terra Incognita*. 3. Of the Sun, *Nov*. 3. 21*h*. 19*m*. P.M. Visible in the North Sea. 4. Of the Moon, *April* 26. 04*h*. 38*m*. P.M. Visible in the North of *America*, Great *Tartaria*, *Caspian* Sea, *Arabia Felix*, *Belgia*, *Baltick* Sea, *Germany*, *Savoy*, *Mediterranean* Sea, *Barbary*, *Libia*, *Guiny*. 5. Of the Moon, *Decemb*. 17. 12*h*. 42*m*. Visible in the North of *America*, *Archipelago*, *Guiny*, *Ducalidonia*, *Iseland*, *Java*, *New France*, *Brasil*.

A Table of the Tydes of the Sea-coasts of *Great Britain, Ireland, Norway, Holland, Flanders, France, Biscay, &c.* Shewing what Moon makes a full Sea in each of these places, at every day of the Moons Age, after the Full or Change.

The Description and Use of the Tables.

FIrst you are to understand that the first Column of the Tables sheweth the Age of the Moon after her Full and Change; and the Second and Third Columns shew the Hour and Minute of Full-Sea at each respective place mentioned in the said Tables; and the fourth Column sheweth the Names of the said Places; and the Fifth sheweth the Setting of the Tydes upon the same Point of the Compass, expresst in the Title. And also in the Tittle you have the Hour when the Moon cometh upon each respective Point of the Compass at Full and Change. The use of which Tables shall be further illustrated by this following

Example.

Suppose you would know what Moon makes Full-Sea at *Dartmouth* and *Torbay*, and at what Hour it cometh to such a Point of the Compass, and the time of High-water any Day of the Moons Age. First, Look for *Torbay* or *Dartmouth*, which you will find in *Page* 12 of the Tables, under the Title of *East by North*, and *West by South*, which doth shew that at the Full and Change of the Moon she cometh on that Point of the Compass, which is at 5^{h} $15'$ in time, when it is Full-Sea in the forementioned places.

So likewise if it be demanded what time it will be Full-Sea when the Moon is six dayes after the Full or Change; Therefore look in the first Column for *6*, and right against it, in the second and third Columns, you will find 10 of the Clock, and 3 minutes past, which is the time of Full-Sea in the forementioned places, at that day of the Moons Age.

North

North and South.

12 *hours*, 10 *minutes*.

D.	H.	M
00	12	00
01	12	48
02	01	36
03	02	24
04	03	12
05	04	00
06	04	48
07	05	36
08	06	24
09	07	12
10	08	00
11	08	48
12	09	36
13	10	24
14	11	12
15	12	00

In the Road of *Gibralter*. On the Coaſt *Flanders*. At the *North-foreland*. At the *Jutland-Iſlands*. Before the *Hever*, *Eider*, and *Elve* on the Coaſt of *Holland*. At *Dover Peer*, on *Beachy* ſhore. At *Orfordneſs*; in the *Condado*; before *Enchuyſen*, *Horn*, and *Vrek*. *Dunkirk*. Half-Tyde at *Newport*. Half-Tyde at *Portſmouth*, and the *Iſle of Wight*. In the *Sleeve* between *Uſhant* and *Silly*. At *Bolem* and *Graveling*. Before *Gherbrough*, and the *Race* of *Blanquet*. At the *Shooe*, *Leight*, and *Kentiſh Knock*; *Spits*, and along the *Swin*.

Setting of the Tydes upon the ſame Point.

From the *Neſs* to *Boleign*.

North by Eaſt, and South by Weſt.

12 *hours*, 45 *minutes*.

D.	H.	M
00	12	45
01	01	33
02	02	21
03	03	09
04	03	57
05	04	45
06	05	33
07	06	21
08	07	09
09	07	57
10	08	45
11	09	33
12	10	21
13	11	09
14		

At *Garnſey*. At *Fluſhing*. Thwart of *Beachy* in the *Offing*. At *Winchelſey*. Within the *Maes*. Within *Terveer*. In the *Chammer* of *Ree*. Weſt end of the *Nower*. At *Rocheſter* and *Maldon*.

Setting of the Tydes upon the ſame Point.

From *Boleign* to the *Some*.

From *Staples* to *Boleign*.

North North-East, and South South-West,

D.	H.	M
00	01	30
01	02	18
02	03	06
03	03	54
04	04	42
05	05	30
06	06	18
07	07	06
08	07	54
09	08	42
10	09	30
11	10	18
12	11	06
13	11	54
14	12	42
15	01	30

01 *hour*, 30 *minutes.*

Before the *Maes* and *Goree*. Before *Terveer*. The *Weilings*. On the Coast of *Zealand*. Before the River of *Thames*. Before *Yarmouth*. In the *Downs*. Thwart of *Dongineſs*. From the Weſt end of *Wight*. Without *Calice* and *Blackneſs*. In *Bluet*. At *Bell-Iſle*, under *Holy-Iſland*. *Tinmouth*, *Graveſ-end*. At *Corpus Chriſti* Point. Before the *Fen* in the Channel. At *Horn*, *Edam*, and before *Camſer*. At *Army*, *Ramkins*, and *Camſer*. At *Barwick*.

Setting of the Tydes on the ſame Point.

From *Calice* to *Boleign*.

North-East by North, and South-West by South,

D.	H.	M
00	02	15
01	03	03
02	03	05
03	04	39
04	05	27
05	06	15
06	07	03
07	07	51
08	08	39
09	09	27
10	10	15
11	11	03
12	11	51
13	12	39
14	01	27
15	02	15

02 *hours*, 15 *minutes.*

Without *Bluet*. Before the *Maes*. Before the *Weilings*. St. *Andrews*. *Denby*. Without *Fountnay*.

Setting of the Tydes upon the ſame Point.

Between *Calice* and *Dover*.

From *Dunkirk* to *Graveling*.

From *Staples* to *Feram*.

From *Dartmouth* to *Exmouth*.

North-East and South-West.

03 *hours*, 00 *minutes*.

D.	H.	M
00	03	00
01	03	48
02	04	36
03	05	24
04	06	12
05	07	00
06	07	48
07	08	36
08	09	24
09	10	12
10	11	00
11	11	48
12	12	36
13	01	24
14	02	12
15	03	00

At *London*, *Amsterdam*, *Dort*, *Roterdam*, *Zierickzee*. Before *Newcastle*. In *Robin-Hoods Bay*. Before the *Tees* and *Hartlepool*. Without the Banks of *Flanders*. Between *Calice* and *Dover*. Before *Conquet*, the *Penns*, *Groy*, *Armentiers*, *Vse*, *Killiars*, *Porthus*. The River *Bourdeaux*. The South Coast of *Bretaign*, *Gascoign* and *Poictou*. The Coast of *Biscay*, *Gallicia*, *Portugal* and *Spain*. *North-Cape*, from the *Race* to the *Pole-head*. Before the River of *Nantz*, and before the Bay of *Tinmouth*. Quarter Tyde at *Flambrough-head*; on the West Coast of *Ireland*. At *Boeckness* and *Orkness*. In *Shotland* and *Fair-Isle*.

Setting of the Tydes upon the same Point

From *Cape de Hague* to *Alderney*, through the Race of *Alderney*.

From *Garnsey* to the *Caskets*.

From *Milford* to *Ramsey*.

North-East by East, and South-West by West.

03 *hours*, 45 *minutes*.

D.	H.	M
00	03	45
01	04	33
02	05	21
03	06	09
04	06	57
05	07	45
06	08	33
07	09	21
08	10	09
09	10	57
10	11	45
11	12	33
12	01	21
13	02	09
14	02	57
15	03	45

Between *Dover* and *Calice*. At the *Maes*. At *Roven*, *Silly*. Before St. *Matthews Point*. At *Brest*. In the *Sound*. Between *Vshant* and the *Main*. Before the *Bass*. At St. *Matthews*. Before *Rochel*. The River of *Bourdeaux* within the Haven: On the Coast of *Spain*, *Portugal*, *Galicia*. The South side of *Bretagn*, *Gascoign*, and the West Coast of *Ireland*. At *Huntclif-foot*. Half-Tyde at *Flambrough-head*. Quarter-Tyde between it and *Bridlington-Bay*.

Setting of the Tydes upon the same Point.

From *Struysaert* to *Deep*

From the *Lizard* to the *Start*.

From *Cape Cleere* unto *Londey*.

East North-East, and West South-West.

D.	H.	M
00	04	30
01	05	18
02	06	06
03	06	54
04	07	42
05	08	30
06	09	18
07	10	06
08	10	54
09	11	42
10	12	30
11	01	18
12	02	06
13	02	54
14	03	42
15	04	30

04 *hour*, 30 *minutes.*

Before *Humber*, *Flambrough*, *Scairbrough*, *Abberwark*. In *Falmouth*. In *Mouſe-hole*. *Sept. Iſles:* Without the Haven, in the Broad Sound. Without the *Fourn*. All the South Coaſt of *Ireland*, as *King-ſale*, *Cork*, *Yough-hall*, *Waterford*, and *Cape Cleer*. In the *Breeſound* and *Vourd*. The *Gleſts* of *Texel*, *Bloy*, and St. *Matthews*. At the Bay within *Uſhant*. At *Calice* in the Creek. *Dungarvan*. *Baltimore*. Within *Mounts-Bay*. In the Sea of *Wales* and *Severn*.

Setting of the Tydes upon the ſame Point.

From *Oſtend* to St. *Kath.* From *Berchfleur* to *Struyſart*. The *Br. Sound* out and in. From *Cape Cleer* to the Iſle of *Saltees*. Between *Londey* and the *Holms* unto *Briſtol*. From *Silly* to the Lands end of *England*. From the *Start* to *Portland*.

East by North, and West by South,

D.	H.	M
00	05	15
01	06	03
02	06	51
03	07	39
04	08	27
05	09	15
06	10	03
07	10	51
08	11	39
09	12	27
10	01	15
11	02	03
12	02	51
13	03	39
14	04	27
15	05	15

05 *hours*, 15 *minutes.*

In *Dartmouth* and *Plymouth*; *Foy* and *Torbay*, *Falmouth*, *Milford*, *Ramſey*. In *Wales*. Thwart of *Londey*. Before *Lin*. In all the Havens on the South Coaſt of *Ireland*, and in the Bay of *Carnarvan*. At the Mouth of *Severn*. Between *Silly* and the *Lizard*. At *Garnſey*, and before St. *Pauls*. At the *Spurn*, *New-caſtle*, and *Humber*. At *Moonles* and *Caldy*.

Setting of the Tydes on the ſame Point.

From the Iſle of *Baſs* to the *Fourn* From the *Dorſeys* to *Cape Cleer*. From *Silly* to the *Lizard*. From *Portland* to *Wight*. From *Wight* to *Beachy*.

East and West.

D.	H.	M
00	06	00
01	06	48
02	07	36
03	08	24
04	09	12
05	10	00
06	10	48
07	11	36
08	12	24
09	01	12
10	02	00
11	02	48
12	03	36
13	04	24
14	05	12
15	06	00

06 hours, 00 minutes.

Before *Bremen*, *Teſſel*, and *Hamburgh*. At *Blackney*, *Wells*, *Hull*, *Concalla*, St. *Mallows*, St. *Powls* in the Haven. Without *Silly* in the Channel. Before *Bourdeaux*. Without *Uſhant*. At *Lin*, Half-Tyde. *Weymouth*, *Londey*, and the *Holms*. At *Briſtol*, *Waterford*, and *Abermorick*.

Setting of th Tydes upon the ſame Point.

From the *Caskets* to *Berchfleur*.

From the Lands end of *England* to the *Lizard*.

East by South, and West by North.

D.	H.	M
00	06	45
01	07	33
02	08	21
03	09	09
04	09	57
05	10	45
06	11	33
07	12	21
08	01	09
09	01	57
10	02	45
11	03	33
12	04	21
13	05	09
14	05	57
15	06	45

06 hours, 45 minutes.

Before St. *Nicholas* and *Podeſſemske*. In *Ruſſia*. At *Weymouth-Key*, *Briſtol-Key*. Between *Foy* and *Falmouth* in the Channel. *Foulneſs*.

Setting of the Tydes upon the ſame Point.

From the *Iſle de Baſs* to *Marwaner*.

East South-East, and West North-West.

D.	H.	M
00	07	30
01	08	18
02	09	06
03	09	54
04	10	42
05	11	30
06	12	18
07	01	06
08	01	54
09	02	42
10	03	30
11	04	18
12	05	06
13	05	54
14	06	42
15	07	30

07 *hours*, 30 *minutes.*

Thwart of *Plymouth*, and off the *Start*, in the Channel. At the *Lizard* by the Land. Between *Mouſe-hole* and *Falmouth*. In the *Offing*. In the midſt of the Channel. At *Kilduyn*. In the Road of the *Texel*. At the *Neſs* by *Wieringhen*. At the Entrance of the *Emes*, or the River of *Emden*. Before the Coaſt of *Friezland* and the *Fly*. *Milford-haven*. At *Cape Clear*.

Setting of the Tydes upon the ſame Point.

From the Iſland *Bryack* to Saint *Maloes*.
From *Berchfleur* to *Seynhead*.

South-East by East, and North-West by West.

D.	H.	M
00	08	15
01	09	03
02	09	51
03	10	39
04	11	27
05	12	15
06	01	03
07	01	51
08	02	39
09	03	27
10	04	15
11	05	03
12	05	51
13	06	39
14	07	27
15	08	15

15 *hours*, 15 *minutes.*

Thwart of the Iſland *Wight* in the Channel. Without the *Caskets* in the Channel. Between the *Wight* and *Beachy* by the ſhoar. Without the *Fly*. To the weſtwards of the *Foreland*. In St. *Magnes* Sound. *Yarmouth*. At St. *Helens*. *Machnels-Caſtle*. *Dublin* and *Lambey*.

Setting of the Tydes upon the ſame Point.

Behind *Garnſey* in the *Fairway*.
Without the *Seven Iſlands*.

South-East and North-West.

D.	H.	M
00	09	00
01	09	48
02	10	36
03	11	24
04	12	12
05	01	00
06	01	48
07	02	36
08	03	24
09	04	12
10	05	00
11	05	48
12	06	36
13	07	24
14	08	12
15	09	00

09 *hours*, 00 *minutes.*

Setting of the Tydes upon the same Point.

In the Bay of *Benviit.*

Between *Morleax* and the *Treacle-Pots.*

Between *Garnſey* and the *Cackets.* At the *Race* of *Portland.* At the Eaſt end of the *Wight.* Within the *Seyn.* Before *Cromer*, *Winterton*, and *Yarmouth.* *Friez*, and *Wieringer-Flat.* On the Coaſt of *Friezland.* Before the *Eaſtern* and *Weſtern-Emes.* Before the *Fly* and *Scholbalgh.* At *Egmont* and *Harlem* of *Baſs.* Before the *Caskets* and *Garnſey.* At *Orkney*, *Dunbar*, and *Kildnie.* At *Fair-Iſles.* *Seven-Clifts.* At *Home-head*, and thwart of *Plymouth* and *Dartmouth.* *Iſle of Man*, and *Cateneſs.*

South-East by South, and North-West by West.

D.	H.	M
00	09	45
01	10	33
02	11	21
03	12	09
04	12	57
05	01	45
06	02	33
07	03	21
08	04	09
09	05	57
10	05	45
11	06	33
12	07	21
13	08	09
14	08	57
15	09	45

09 *hours*, 45 *minutes.*

Setting of the Tydes upon the same Point.

Before *Concalo*, and the Iſland of St. *Michael.*

Thwart of *Leyſtaff* without the Banks. The *Needles* at the *Iſle of Wight.* In the Channel thwart of *Wight.* The *Caskets* thwart of *Garnſey* in the Channel. At *Dunnoſe*, *Tergou*, *Orfordneſs* and *Albrough*; and at *Leyſtaff*, and at *Chamberneſs.*

South South-East, and North North-West.

D.	H	M
00	10	30
01	11	18
02	12	06
03	12	54
04	01	42
05	02	30
06	03	18
07	04	06
08	04	54
09	05	42
10	06	30
11	07	18
12	08	06
13	08	54
14	09	42
15	10	30

10 *hours*, 30 *minutes*.

At St. *Helens* and the *Cows*. At *Orfordneſs*, and *Harwich* without the Banks. In *Yarmouth* and *Leyſtaff-Road*. Before the River of *Thames*. Between the *Iſle of Wight* and the Main. At *Bulleyn-deep* and *Seyn-head*. In the *Foſſe* of *Caen*. At *Struyſaert*, and all the Coaſt of *Normandy* and *Picardy*. *Calice*-Road. In the *Frieth*. At *Leyſtaff*, Quarter-Tyde. *Harwich*, *Dover*, and the *South-Foreland*. Between *Orford* and *Orwel-Waves*. In *Chamberneſs*-Road. In the *Downs*.

Setting of the Tydes upon the ſame Point.

From *Berchfleur* to *Alhonga*.

From *Cape Dorſey* to the Iſland *Dardan*.

South by East, and North by West.

D.	H.	M
00	11	15
01	12	03
02	12	51
03	01	39
04	02	27
05	03	15
06	04	03
07	04	51
08	05	39
09	06	27
10	07	15
11	08	03
12	08	51
13	09	39
14	10	27
15	11	15

11 *hours*, 15 *minutes*.

At *Cows* and *Orfordneſs* within the Sands, and *Hampton*, *Portſmouth*, and *Dunnoſe*. Before the Haven of *Caen*. *Fair-Iſle-Roads*. *Harwich* within. Between the *Naze* and *Warhead* of *Lower*. In the *Chamber* and *Gore* end. Between *Cripple-ſand* and the *Creyl*. In the *Frith*, and before *Margate*.

Setting of the Tydes upon the ſame Point.

From Saint *Matthews-Point* to the *Bake-Ovens*.

From *Fontnay* to Saint *Matthews-Point*.

Days.	Fanuary		February		March		April		May		June	
	Suns right aſcen.		Suns right aſcen.		Suns right aſcen.		Suns right aſcen.		Suns right aſcen.		Suns right aſcen.	
	H	M	H	M	H	M	H	M	H	M	H	M
1	19	35	21	42	23	28	1	21	3	14	5	19
2	19	39	21	46	23	32	1	25	3	18	5	23
3	19	43	21	50	23	36	1	29	3	22	5	27
4	19	47	21	54	23	39	1	33	3	26	5	31
5	19	51	21	58	23	43	1	36	3	30	5	36
6	19	56	22	02	23	46	1	40	3	34	5	40
7	20	00	22	06	23	50	1	44	3	38	5	44
8	20	04	22	10	23	53	1	47	3	42	5	48
9	20	09	22	14	23	57	1	51	3	46	5	52
10	20	13	22	17	0	01	1	54	3	50	5	56
11	20	17	22	21	0	05	1	58	3	54	6	00
12	20	22	22	25	0	08	2	02	3	58	6	04
13	20	26	22	29	0	12	2	06	4	01	6	08
14	20	30	22	33	0	15	2	10	4	06	6	12
15	20	34	22	36	0	19	2	13	4	10	6	17
16	20	38	22	40	0	23	2	17	4	14	6	21
17	20	42	22	44	0	26	2	21	4	18	6	25
18	20	46	22	48	0	30	2	25	4	22	6	29
19	20	50	22	52	0	33	2	29	4	26	6	33
20	20	54	22	55	0	37	2	32	4	30	6	38
21	20	58	22	59	0	41	2	36	4	34	6	42
22	21	03	23	03	0	44	2	40	4	38	6	46
23	21	07	23	06	0	48	2	44	4	42	6	50
24	21	11	23	10	0	52	2	48	4	46	6	54
25	21	15	23	13	0	55	2	51	4	50	6	58
26	21	19	23	17	0	59	2	55	4	54	7	02
27	21	23	23	21	1	03	2	59	4	58	7	06
28	21	27	23	25	1	06	3	03	5	02	7	10
29	21	31			1	10	3	07	5	06	7	14
30	21	35			1	14	3	10	5	11	7	19
31	21	38			1	17			5	15		

Dayes	*July* Suns right aſcen.		*August* Suns right aſcen.		*Septem.* Suns right aſcen.		*Octob.* Suns right aſcen.		*Novem.* Suns right aſcen.		*Decemb.* Suns right aſcen.	
	H	M	H	M	H	M	H	M	H	M	H	M
1	7	23	9	25	11	19	13	08	15	07	17	15
2	7	27	9	29	11	23	13	12	15	11	17	20
3	7	31	9	33	11	26	13	15	15	15	17	25
4	7	35	9	37	11	30	13	19	15	19	17	29
5	7	39	9	40	11	33	13	22	15	23	17	34
6	7	43	9	44	11	37	13	26	15	27	17	38
7	7	47	9	48	11	41	13	30	15	31	17	42
8	7	51	9	51	11	44	13	34	15	36	17	47
9	7	55	9	55	11	48	13	38	15	40	17	51
10	7	59	9	58	11	51	13	41	15	45	17	56
11	8	03	10	02	11	55	13	45	15	49	18	00
12	8	07	10	06	11	59	13	49	15	53	18	05
13	8	11	10	10	12	02	13	53	15	58	18	09
14	8	15	10	14	12	06	13	57	16	02	18	14
15	8	19	10	17	12	09	14	00	16	07	18	19
16	8	23	10	21	12	13	14	04	16	11	18	24
17	8	27	10	25	12	17	14	08	16	15	18	28
18	8	31	10	28	12	20	14	12	16	19	18	33
19	8	35	10	32	12	24	14	16	16	23	18	37
20	8	39	10	35	12	27	14	20	16	28	18	41
21	8	43	10	39	12	31	14	24	16	32	18	45
22	8	47	10	43	12	35	14	28	16	36	18	49
23	8	51	10	46	12	38	14	32	16	40	18	54
24	8	55	10	50	12	42	14	36	16	44	18	58
25	8	58	10	53	12	45	14	39	16	49	19	03
26	9	02	10	57	12	49	14	43	16	53	19	07
27	9	06	11	01	12	53	14	47	16	57	19	11
28	9	10	11	04	12	57	14	51	17	02	19	16
29	9	14	11	08	13	01	14	55	17	06	19	20
30	9	17	11	11	13	04	14	59	17	11	19	25
31	9	21	11	15			15	03			19	30

A Table of the right Aſcenſions and Declinations of ſome of the principal Fixed Stars, for ſome Years to come.

	Right Aſcen.		Declination.		N. or S.	Magnit.
	H.	M.	D.	M.		
Pole Star.	00	31	87	34	N	2
Andromedas Girdle.	00	50	33	50	N	2
Whales Belly.	01	35	12	00	S	3
Rams Head.	01	48	21	49	N	3
Meduſa's Head.	02	44	02	42	N	2
Whales mouth.	02	46	39	35	N	3
Perſeus right Side.	02	59	48	33	N	2
Bulls Eye.	04	16	15	46	N	1
Goat.	04	52	45	37	N	1
Orions left Foot.	04	58	8	38	S	1
Orions left Shoulder.	05	6	5	59	N	3
Firſt in Orions Girdle.	05	15	00	35	S	3
Second in Orions Girdle.	05	19	1	27	S	3
Third in Orions Girdle.	05	23	2	9	S	3
Orions right Shoulder.	05	36	7	18	N	2
The Waggoner.	05	39	44	56	N	2
Bright Foot of the Twins.	06	18	16	39	N	3
Great Dog.	06	30	16	13	S	1
Caſtor.	07	12	32	30	N	2
The little Dog.	07	22	6	6	N	2
Pollux.	07	24	28	28	N	2
Hidra's Heart.	09	10	07	10	S	1
Lions Heart.	09	50	13	39	N	1
Lions Neck.	09	50	21	41	N	3
Great Bears Rump.	10	40	58	43	N	2
Lions Back.	11	30	22	4	N	2
Lions Tail,	11	31	16	30	N	1

A Table of the right Aſcenſions and Declinations of ſome of the principal Fixed Stars, for ſome Years to come.

	Right Aſcen.		Declination.		N. or S.	Magni.
	H.	M.	D.	M.		
The Virgins Girdle.	12	38	5	20	N	3
Firſt in the great Bears Tail next the Rump.	12	38	57	51	N	2
Vindemiatrix.	12	44	15	51	N	3
Virgins Spike.	13	7	9	19	S	1
Middlemoſt in the great Bears Tail.	13	10	56	45	N	2
Laſt in the end of the great Bears Tail.	13	34	51	05	N	2
Arcturus.	14	00	21	03	N	1
South Ballance.	14	32	14	33	S	2
Brighteſt in the Crown.	15	24	27	43	N	3
North Ballance.	15	58	08	03	S	3
Serpentarius's left Hand.	15	56	02	46	S	3
Scorpions Heart.	16	08	25	35	S	1
Serpentarius's left Knee.	16	18	09	46	S	3
Serpentarius's right Knee.	16	49	15	12	S	3
Hercules Head.	16	59	14	51	N	3
Serpentarius Head.	17	19	12	52	N	3
Dragons Head.	17	48	51	36	N	3
Brighteſt in the Harp.	18	25	38	30	N	1
The Vultures Heart.	19	34	08	00	N	2
Upper horn of Capricorn.	19	58	13	32	S	3
Swans Tail.	20	30	44	05	N	2
Left ſhoulder of Aquarius.	21	13	07	02	S	3
Pegaſus Mouth.	21	27	08	19	N	3
Right ſhoulder of Aquarius.	21	48	11	58	S	3
Fomahant.	22	39	31	17	S	3
Pegaſus upper Wing, or Marchab.	22	48	13	21	N	2
Pegaſus lower Wing.	23	55	33	25	N	2

To know the hour when any Star cometh upon the Meridian.

The Rule.

FIrſt ſeek the *Right Aſcenſion* of that Star required in the fore-going Tables (of the *Right Aſcenſion* of the Stars) and alſo the *Right Aſcenſion* of the Sun: from the *Right Aſcenſion* of the Sun, ſubſtract the *Right Aſcenſion* of the Star; But when the *Right Aſcenſion* of the Star is leſs than the *Right Aſcenſion* of the Sun, then add 24 hours thereto, and the Remainder will ſhew you the hour Afternoon when the Star commeth upon the Meridian, and if it do exceed 12 hours, then ſubſtract 12 hours therefrom, and the remainder ſhall ſhew the hour and minute of the Stars coming upon the Meridian after Midnight.

Example 1.

Upon the 10th of *April*, I would know when the *Lyons Heart* cometh upon the Meridian. Therefore if you look in the Tables of *Right-Aſcenſion* for that Star, you will find it to be 9 hours 50′. Then look in the Tables of *Right Aſcenſion* of the Sun, and right againſt the 10th of *April* you will find the *Right Aſcenſion* of the Sun to be 1 hour 54 min. which ſubſtracted from the *Right Aſcenſion* of the Star, there remaines 7 hours 56 minutes, which is the true time that the Star cometh to the Meridian Afternoon.

Example 2.

Upon the fifth of *November*, I deſire to know when the *Bulls Eye* cometh upon the *Meridian*: The *Right Aſcenſion* thereof by the Tables, you will find to be 4 hours 16 minutes: the *Right Aſcenſion* of the Sun that day is 15 hours 23 minutes. Therefore becauſe the *Right Aſcenſion* of the Star is leſs than the *Right Aſcenſion* of the Sun, I add 24 hours to the *Right Aſcenſion* of the Star, which maketh 28 hours 16 minutes: From which ſubſtract the *Right Aſcenſion* of the Sun, and the remainder is 12 hours 53 minutes: From which I Subſtract the 12 hours, and the remainer is 53 minutes after *Midnight*, then the ſaid Star cometh upon the *Meridian*.

And here note, That the Table of *Right-Aſcenſion* of the Sun, is calculated for Noon every day; and that it doth increaſe by about four minutes each day; ſo that it may be proportioned, for every ſix hours to allow one minute for the time afternoon.

A Table

A Table of the Latitudes and Longitudes of the principal Ports, Harbours, Capes and Islands in most of the known parts of the World: Beginning from the Meridian of Pico Teneriffa. *Collected from the best Charts, Descriptions, and Observations of several able and experienced Navigators of our own and other Nations.*

		Latitude. D.	M.		Long. D.	M.
The Sea Coast of *Greenland.*	*Hacluits Head-land,*	79	50	N	26	55
	Fair Fore-dand,	79	15	N	24	50
	Black Point.	78	32	N	25	10
	Point Loook-out.	76	25	N	32	00
	Cape Blanco.	78	25	N	38	00
	Point Negro.	77	10	N	42	00
	Hopeless Isles.	77	00	N	42	30
Island in the North Sea.	*Hope Island.*	76	13	N	41	50
	Cherry Island.	74	34	N	34	10
	South Point of Trinity Island.	71	00	N	07	55
	Youngs Fore-land in Trinity Island.	71	23	N	10	20
The Sea Coast of *Nova-Zemblia.*	*Orange Island.*	78	25	N	91	35
	Ice Point.	77	45	N	90	50
	Admiralties Island.	75	50	N	73	55
	Langeness.	74	55	N	68	50
	Cross Point.	72	25	N	68	05
	Fretum Burrough.	70	40	N	75	00
	The River Obij *in the Tartarian Sea.*	69	12	N	80	49
	Mauritius Isle.	71	24	N	72	10
Sea Coast in the *White Sea*	*Archangel.*	63	22	N	55	28
	Swelgenose.	69	10	N	61	38
	Cape Candenose.	69	35	N	58	02
	Orlogenose.	66	55	N	54	56

		Latitude.			Latit.	
		D.	M.		D.	M.
Sea Coast of *Lapland* and *Norway*.	*Fox Noſe.*	64	12	N	37	07
	Cape Grace.	65	17	N	39	30
	Cape Gallant.	67	11	N	39	32
	Cape Race.	65	49	N	40	04
	Iſland Kildunym.	68	54	N	38	05
	North Cape.	71	22	N	32	35
	Roſs Iſles.	67	01	N	25	06
	Cats-neſs.	61	54	N	18	42
	Bomel.	59	32	N	19	38
	Naze of Norway.	58	00	N	21	02
The Sea Coaſt in the *Sound*.	*The Nyding.*	57	00	N	25	40
	Cape Cole.	56	46	N	26	12
	Scarlet Iſland.	56	02	N	26	38
	Falſterborne.	56	53	N	26	25
	Abbo.	61	08	N	34	30
	Wyborrough.	61	16	N	40	18
	Dagaret.	59	44	N	34	31
	Dormamel.	56	55	N	34	31
	Gotland.	58	20	N	31	05
	Horroſound.	58	48	N	32	58
	Gothſound.	59	15	N	32	29
	Earth Holme.	56	10	N	28	14
	Burnt-Holme.	56	00	N	28	16
	Elſenore.	56	40	N	25	57
The Sea Coaſt of *Flanders* from the *Scaw* to *Callice*.	*The Schaw.*	57	52	N	24	27
	Bovenbergh.	56	20	N	23	56
	Holy-land.	54	30	N	22	14
	The Texel.	53	20	N	20	56
	The Brill.	52	08	N	19	44
	Callice.	51	13	N	17	52

		Latitude. D.	M.		Long. D.	M.
Sea Coast of *Island.*	*Langeneſs.*	67	20	N	03	45
	Grinſe.	67	00	N	352	05
	Maze.	68	25	N	351	10
	Andifer.	66	30	N	345	00
	Snowhill.	65	40	N	344	40
	Alcra Point.	64	08	N	344	20
	Weſtmonia Iſles	63	35	N	349	00
	Merchants Foreland.	63	36	N	358	40
	Whale Back.	65	18	N	003	00
Iſlands near the Coaſt of *Scotland.*	*St. Kilda.*	58	02	N	05	56
	Skie Iſland.	57	40	N	10	08
	Lewis Iſland.	58	30	N	08	00
	Faire Iſlands.	61	43	N	09	00
	Shotland.	60	22	N	14	30
	Fair Iſle.	59	30	N	14	20
	Iſles of Orkney.	58	50	N	13	25
Sea Coaſt of *Scotland, England,* and *Ireland.*	*Cateneſs.*	58	37	N	13	24
	Buchaneſs.	58	00	N	14	32
	St. Abbs Head.	56	25	N	14	12
	Tinmouth.	55	08	N	15	00
	Flamborrough Head.	54	08	N	16	26
	The Sporne.	53	45	N	16	58
	Wintertonneſs.	52	52	N	18	00
	Orfordneſs.	52	20	N	18	02
	The North Foreland.	51	32	N	17	40
	The South Foreland.	51	22	N	17	42
	Dongeneſs.	51	09	N	17	14
	Iſle of Wight.	50	24	N	14	47
	Portland.	50	20	N	13	46
	The Start.	50	27	N	13	09
	The Lizard.	50	00	N	12	37
	Iſlands of Silly.	50	07	N	09	47
	Londys Iſle.	51	22	N	11	57
	St. Davids Head.	51	54	N	11	18

		Latitude.			Longit.	
		D.	M.		D.	M.
Sea Coast of *Scotland*, *England*, and *Ireland*.	*Bradsey Isle.*	52	46	N	11	39
	Holy Head.	54	44	N	11	44
	Isle of Man.	54	25	N	11	45
	Coswel-Point.	54	36	N	11	18
	Fair Fore-land.	55	35	N	10	16
	Aron Isle.	53	21	N	8	30
	Black Rock.	53	52	N	6	00
	Slime Head.	53	16	N	6	00
	Blasque.	52	15	N	5	20
	Cape Clear.	51	15	N	6	28
	Old-Head.	51	40	N	7	32
	Hearn-Point.	52	05	N	10	04
Sea Coast of *France*, *Spain* and *Portugal*.	*Sain Head.*	50	04	N	16	50
	Cape Hage.	50	04	N	15	05
	Caskets.	50	07	N	14	30
	Garnsey.	49	43	N	14	20
	Jersey.	49	30	N	14	46
	Uhant.	48	40	N	11	16
	Oleroon.	45	58	N	11	00
	Cape de Machicaca.	44	22	N	14	20
	Cape Pinas.	44	04	N	11	10
	Cape Ortegal.	44	08	N	9	16
	Cape Finisterre.	43	10	N	6	58
	The Rock of Lisbon.	38	52	N	6	43
	Cape Saint Vincent.	37	00	N	7	20
	Cape Saint Maria.	37	05	N	8	42
	The Straits of Gibralter.	36	00	N	10	40

		Latitude.			Longit.	
		D.	M.		D.	M.
The Sea Coasts on the *Main Continent* in the *Straits.*	*Cape de Gata.*	36	47	N	16	08
	Cape Saint Martin.	38	46	N	18	57
	Cape Daga Frito.	41	41	N	21	49
	Cape Larei.	42	58	N	24	28
	Cape Melle.	43	51	N	26	21
	Terracina.	41	26	N	31	26
	Cape Sparteventura.	37	46	N	36	06
	Cape Collom.	38	50	N	37	30
	Cape Saint Maria.	39	52	N	38	16
	Angello.	41	31	N	36	28
	Ancana.	43	25	N	32	40
	Cape Ceſta.	43	27	N	34	55
	Raguſa.	42	29	N	37	36
	Cape Linga.	40	19	N	38	50
	Cape Matopan.	36	28	N	42	00
	Cape Saint Angelo.	37	15	N	42	56
	Cape Doro.	39	14	N	45	12
	Cape Barbarnou.	37	58	N	46	19
	Cape Saradoni.	35	35	N	48	46
	Cape Pollopollo.	34	54	N	55	34
	Cape de Becur.	32	40	N	50	48
	Cape Roatini.	32	18	N	43	32
	Cape Rozato.	32	58	N	40	28
	Cape Bona.	37	05	N	30	12
	Collo.	37	09	N	24	52
	Tunis.	36	40	N	19	46
	Cape Falcon.	36	08	N	17	28
	Cape Tres forcas.	35	40	N	15	24
	Tangier.	35	36	N	11	35
Iſlands within the Straits	*Alboran.*	37	52	N	15	18
	Formentara.	38	44	N	19	38
	Ivica.	39	05	N	19	50
	Majorca.	39	38	N	21	20
	Minorca.	39	55	N	22	30

		Latitude. D.	M.		Longit. D	M.
Islands within the *Straits.*	*Gallatta.*	37	57	N	27	50
	Cape Pulo in Sardinia.	38	56	N	27	36
	Cape Corso in Corsica.	42	51	N	27	32
	Lilbo.	42	51	N	29	00
	Palmorolla.	40	50	N	31	12
	Ustica.	38	46	N	32	48
	Maritimo.	37	52	N	30	54
	Pantalaria.	36	53	N	31	00
	Limpadosa.	55	58	N	31	52
	Limosa.	36	25	N	32	05
	Malta.	36	00	N	33	12
	Cape Passaro in Sicilia.	37	10	N	34	52
	Messina.	38	07	N	35	8
	Lissa.	43	00	N	35	22
	Trinity.	41	50	N	35	14
	Pallagosa.	42	17	N	35	50
	Augusta.	42	36	N	36	12
	Mallida.	42	37	N	37	04
	Corfu.	39	25	N	39	18
	Cephalonia.	38	28	N	40	29
	Zant.	37	37	N	40	40
	West end of Candia.	35	15	N	43	00
	East end of Candia.	35	04	N	46	28
	Rhodes.	35	40	N	48	00
	West end of Cyprus.	34	22	N	51	34
	East end of Cyprus.	34	48	N	54	35
Sea Coast of *Barbary* and *Ginny.*	*Cape Spartel.*	35	38	N	11	35
	Cape Cantin.	32	27	N	7	35
	Cape Bojador.	26	55	N	2	24
	Cape Blanco.	20	32	N	358	56
	Cape Verde.	14	36	N	358	50
	Sirre Leone.	08	00	N	03	32
	The South side of Saint Anne.	06	40	N	01	11

		Latitude.			Longit.	
		D.	M.		D.	M.
Sea-Coast of *Barbary* & *Guiny*	*Cape de Palmas.*	04	10	N	10	00
	Cape Tres Puntas.	04	06	N	16	00
	Cape Formosa.	04	10	N	24	15
	The North Point of Fernando.	03	25	N	27	25
	Island Principas.	01	50	N	28	20
	Island Chocos.	00	40	N	03	32
	Island St. Thoma.	00	10	N	27	30
	Cape Lupus.	01	00	S	27	40
	Cape Negro.	16	00	S	30	50
	Cape Sacos.	29	40	S	36	20
	Cape Bona Esperanza.	34	24	S	38	10
Western Islands.	*The West side of Corva.*	40	00	N	345	30
	The West side of Flores.	39	40	N	345	30
	The Road before Fyal.	38	50	N	347	47
	The West end of Pico.	38	40	N	348	18
	The West end of St. George.	39	00	N	348	30
	The West end of Tercera.	30	00	N	349	10
	The East end of St. Michaels.	38	00	N	351	40
	The East end of St. Maries.	37	00	N	351	30
The *Canary* Islands.	*The North part of Ferro.*	27	40	N	358	25
	The East side of Palme.	28	36	N	358	43
	Gomera.	28	10	N	359	15
	Pico Tenerifa.	28	20	N	00	00
	The East end of Madera.	32	32	N	00	10
	The East end of Port Santto.	33	00	N	01	00
	The North-east Point of Canaria.	28	10	N	01	00
	The N. E. Point of Forteventura.	28	20	N	02	50
	The East part of Lancerotta.	28	30	N	03	10

		Latitude.			Longit.	
		D.	M.		D.	M.
Cape de Verde Islands.	The West side of Antonio.	17	00	N	350	00
	The East Point of St. Vincent.	17	40	N	350	08
	The East side of St. Lucia.	16	50	N	351	40
	Isle Brava.	14	40	N	351	08
	Isle Fogo.	14	00	N	351	30
	The East side of St. Jago.	15	00	N	352	30
	East side of de Mayo Isle.	15	00	N	353	04
	East side of the Isle of Sall.	16	00	N	353	04
	East side of Bona Vista.	16	00	N	353	04
	St. Matthews.	01	40	S	11	32
	Island Anabona.	01	22	S	26	20
	Ascension.	08	00	S	04	30
	St. Helena.	16	00	S	13	50
	St. Helena Nova.	16	03	S	24	48
	Island Degiaialica.	37	56	S	12	00
	Island Desistian.	36	57	S	12	42
Sea-Coast on the Main Continent in the *East-India*.	Cape Anquilhar.	35	00	S	39	30
	Cape Corintes.	23	30	S	56	00
	Cape de Guada.	15	17	S	59	56
	Cape de Guardasin.	11	40	N	74	15
	Cape de Rasalgate.	22	07	N	84	10
	Surrat.	21	04	N	96	20
	Goa.	15	40	N	97	00
	Cape Comerin.	07	52	N	99	12
	The S. W. Point of Cylon.	06	00	N	101	56
	River Bengale.	22	09	N	110	20
	River de Care.	10	45	N	119	10
	Fobr.	01	25	N	125	06
	Siam.	14	52	N	122	45

Cambodia

		Latitude.			Longit.	
		D.	M.		D.	M.
Sea-Coast on the Main-Continent in *East-India.*	*Cambodia.*	12	42	N	126	00
	Vischers Point.	20	18	N	131	00
	The Point of Cavallos.	25	16	N	140	58
	Cape Somber.	28	07	N	142	50
	Ninghai.	36	40	N	142	26
	Corea.	36	05	N	146	00
Islands in the East-India.	*Romeyros.*	28	19	S	89	40
	John de Lisbone.	25	24	S	75	52
	Diego Roize.	20	05	S	85	05
	St. Branda.	17	13	S	87	50
	Dolgatias.	15	20	S	82	15
	Moroslau.	20	10	S	78	36
	Domascaicaes.	20	50	S	74	00
	St. Apolonia.	20	50	S	74	00
	South end of St. Lawrence.	25	37	S	68	00
	North end of St. Lawrence.	11	03	S	73	00
	Bastos de India.	22	10	S	60	40
	John de Nova.	17	20	S	63	15
	Mayotta.	12	40	S	66	30
	Comore.	11	20	S	65	10
	De Natall.	08	20	S	68	05
	Cosmolede.	09	40	S	72	08
	John de Nova.	09	00	S	79	46
	De Almiranta.	03	57	S	76	00
	Domescaicubas.	03	21	S	80	26
	St. Hermanas.	03	02	S	84	00
	Diego Gratiosa.	08	03	S	92	20
	De Gamo.	02	40	S	99	05
	Adu.	05	39	S	99	00
	Apoluria.	09	20	S	100	40
	Island Pracel.	10	23	N	93	14

		Latitude.			Longit.	
		D.	M.		D.	M.
Ilands in the East India.	Cubile.	8	53	N	93	30
	Molique.	9	05	N	94	25
	Andaro.	11	30	N	95	38
	The North West point of Sumatra.	5	30	N	116	00
	South East end of Sumatra.	5	52	S	125	40
	Bantam.	6	15	S	126	30
	Batavia.	6	10	S	127	05
	Combava.	8	36	S	138	00
	Flores.	8	50	S	140	48
	Timor.	9	52	S	145	53
	Ceram.	3	26	S	148	20
	Amboina.	3	52	S	147	25
	South end of Celebes.	5	45	S	139	30
	North Point of Celebes.	2	16	N	144	6
	The middle of Gilolo.	00	00	X	147	20
	Bachian.	00	03	N	146	10
	Machian.	00	14	N	146	6
	Motir.	00	25	N	146	8
	Pottobackers.	00	32	N	146	10
	Tidore.	00	41	N	146	16
	Miserra.	00	43	N	146	14
	Ternate.	00	47	N	146	12
	Saint Johannes.	4	10	N	138	50
	South Point of Burneo.	4	16	S	135	4
	North Point of Burneo.	7	40	N	134	35
	West end of Mindano.	6	50	N	141	25
	Anamba.	2	38	N	126	42
	Natura.	3	30	N	127	45
	Saint Juan.	8	16	N	146	20
	Tandaia.	12	00	N	145	05
	Masbat.	11	50	N	143	35
	Sebu.	9	55	N	143	10
	Pandi.	11	05	N	142	00
	Mindora.	12	50	N	140	28
	Paragoa.	9	40	N	136	30
	South end of Lucon.	12	42	N	143	45

		Latitude.			Longit.	
		D.	M.		D.	M.
Islands in the *East India.*	*North end of Lucon.*	18	42	N	141	56
	The middle of Aynam.	19	00	N	131	00
	South end of Formosa.	21	20	N	142	5
	North end of Formosa.	28	10	N	143	16
	Firando Isle.	33	00	N	147	15
	West end of Japan.	34	00	N	150	5
	North end of Cikoko.	34	5	N	150	10
	Tonsa.	33	25	N	153	00
	North Point of Japan.	40	5	N	163	20
	Cape Eroen in Jeso.	42	50	N	183	20
	Cape Patience in Jeso.	49	00	N	186	00
The Coast of *America* in the South-Sea.	*The Straits of Anian.*	57	10	N	251	56
	Cape Blanco.	42	00	N	245	10
	Sir Francis Drakes *Bay.*	38	16	N	246	30
	Island Peraros.	30	8	N	253	50
	Cape St. Lucas.	23	10	N	266	10
	Cape Corintes.	20	28	N	270	56
	Aquatulco.	16	45	N	283	50
	Gulf of Salina.	10	00	N	288	20
	Cape St. Maria.	7	8	N	293	6
	Cape Corintas.	5	26	N	295	20
	Cape de Francisco.	1	25	N	292	20
	Cape de Passao.	00	00	X	291	35
	Payta.	4	30	S	293	00
	Truxilla.	8	5	S	295	00
	Villa la Nasca.	15	10	S	297	50
	Arica.	18	35	S	302	00
	Island Ferando.	33	47	S	292	20
	Baldivia.	40	00	S	297	35
	P. St. Cyprian.	43	16	S	296	38
	West Entrance of Magellan.	53	00	S	296	42
	Cape Horn.	57	54	S	303	00

A Table of Latitude and Longitude.

		Latitude.			Longi	
		D.	M.		D.	
Islands in the great South-Sea.	Honder Island.	14	00	S	237	3
	Water Islands.	14	50	S	229	00
	Island Tiburones.	12	00	S	218	5
	St. Pedro.	22	10	S	229	10
	Prince Williams Islands.	18	14	S	204	50
	Islands of Good Hope.	17	12	S	195	40
	States Land.	38	00	S	92	00
	Green Islands.	4	00	S	172	00
	Salteadores Isle.	6	40	N	172	5
	Miracomo.	6	24	N	175	40
	Islands de Ladrones.	10	00	N	170	00
	Nadadores.	4	22	N	186	55
	Barbadoes Isles.	7	00	N	195	5
	St. Peters Isle.	11	14	N	205	00
	Hermanes Isle.	15	10	N	181	5
Sea-Coast of the Main-Continent of America.	Lemairs Straight.	55	00	S	310	16
	Cape Pennas.	53	45	S	307	20
	East Entrance of Magelan.	52	20	S	305	00
	Cape Blanco.	47	30	S	309	45
	Cape St. Antonio.	36	38	S	325	00
	Cape St. Maria.	35	00	S	325	40
	Cape Frio.	22	52	S	338	38
	Baja de todas Santos.	13	00	S	341	50
	Cape St. Augustine.	8	40	S	345	40
	Black Point.	3	10	S	343	00
	River Cassepore.	4	00	N	328	5
	Suranam.	5	5	N	323	40
	Cape three Points.	11	18	N	314	20
	Cape de Coquibocao.	12	42	N	305	24
	Carthagene.	10	25	N	298	25
	Cape de Gratias.	15	32	N	291	55
	Cape de Catoche.	21	23	N	287	00
	Cape Rexo.	22	40	N	275	26
	Cape Blanco.	26	55	N	274	56

		Latitude.			Longit.	
		D.	M.		D.	M.
Sea-Coasts of the Main-Continent of *America*.	*Cape Escondido.*	29	52	N	285	40
	La Florida.	25	51	N	272	16
	Cape Fair.	34	02	N	298	25
	Cape Henry.	37	00	N	300	40
	Cape Charles.	37	48	N	300	54
	Cape May.	39	55	N	302	00
	The East end of Long Island.	40	45	N	303	17
	Cape Codd.	42	20	N	308	40
	Cape Ann.	42	45	N	308	16
	Cape Furcu.	44	00	N	314	10
	East end of the Isle of Sables.	43	40	N	323	00
	Cape Britain.	45	30	N	323	50
	Cape Raze.	46	36	N	328	30
	Conception Bay.	48	22	N	327	50
	Bay of Bulls.	47	27	N	328	05
	Cape Bona Vista.	49	19	N	328	36
	Pingwins Isle.	50	02	N	328	40
	Cape Gate.	52	00	N	325	32
	Bell Isle.	52	25	N	325	30
Islands in the *West-India*.	*Bermudas.*	32	18	N	310	50
	Behama.	27	57	N	295	20
	North-east Point of Lucaioneque.	27	52	N	298	20
	Signates.	26	18	N	300	00
	Guatro.	25	47	N	301	00
	Guamina.	25	15	N	301	40
	Tiango.	24	33	N	302	20
	Maiagana.	23	05	N	303	00
	Caicos.	22	05	N	304	05
	Ibagua.	21	19	N	301	40
	Yamata.	22	32	N	301	20
	Samana.	24	20	N	295	45
	Yamia.	24	30	N	301	05

		Latitude.			Longit.	
		D.	M.		D.	M.
Ilands in the *West-India.*	*Anguilla.*	18	48	N	313	35
	St. Chriſtophers.	17	30	N	313	30
	South end of Barbada.	17	36	N	316	00
	Antego.	16	32	N	315	10
	Gadalupa.	16	00	N	314	40
	Marigallatta.	15	41	N	315	25
	Dominica.	15	09	N	314	50
	Martineco.	14	30	N	316	36
	St. Lucia.	13	13	N	315	20
	Barbadoes.	13	12	N	319	40
	St. Vincent.	12	50	N	313	45
	Granada.	12	10	N	314	40
	Tabago.	11	12	N	317	00
	Point de Gallaia.	10	45	N	316	55
	Mevis.	17	00	N	314	00
	Monſerat.	16	20	N	314	20
	Margaretta.	11	28	N	312	25
	Tortogas.	11	30	N	313	30
	Doikilla.	12	19	N	310	30
	Bonayre.	12	32	N	308	35
	Quiſſa.	12	25	N	307	30
	East end of Hiſpaniola.	18	47	N	308	10
	West end of Hiſpaniola.	18	25	N	300	10
	Port Royal in Jamaica.	18	15	N	297	10
	East end of Cuba.	20	27	N	301	20
	West end of Cuba.	22	00	N	288	26
	Camnamis.	19	41	N	294	45
	Great Caiman.	19	21	N	293	30
	Santa Villa.	17	28	N	294	00
	Moſquito.	14	50	N	294	12
	Guanabo.	16	33	N	287	14
	Guanabimo.	16	10	N	286	20
	Cozumal.	19	25	N	287	10
	Laſalleiranes.	22	00	N	284	40

		Latitude. D.	M.		Longit. D.	M.
The Northern parts of *America.*	Cape Canus.	53	40	N	226	52
	Resolution Isles.	61	00	N	309	00
	The Kings Foreland.	61	50	N	295	30
	Queen Anns Foreland.	63	52	N	293	40
	Cape Charles.	62	55	N	291	42
	North end of Mansfields Isle.	62	40	N	284	39
	Prince Ruperts River.	51	00	N	289	12
	Cape *Monmouth.*	54	40	N	283	00
	Cape *Heneretta.*	56	16	N	279	10
	Port Nelson.	58	32	N	267	50
	Cape *South-hampton.*	62	30	N	279	25
	Seahorse Point.	64	46	N	282	20
	Sir Dudly Digs Cape.	75	10	N	298	00
	Sandersons Tower.	68	00	N	314	08
	Cape *Walsingham.*	65	42	N	311	20
	Cape Comfort.	62	21	N	321	20
	Cape *Desolation.*	61	20	N	325	05
	Cape *Farewell.*	59	45	N	329	02

The Use of the Table of the Latitudes and Longitudes of Places.

In this *Table* there are two *Columns*, the one shewing the *Latitude*, the other the *Longitude* of Places: The *Latitudes* are distinguished by the *Letters* N. *and* S. which sheweth the Latitude of the place to be either *Northerly* or *Southerly*; the *Longitudes* are all accounted easterly, from the *Meridian* of *PICO* on the *Island of Teneriff*; an *Example* or two will make it plain.

Example 1.

What is the Latitude and Longitude of the Lizard *upon the Coast of* England?

Against the *Lizard* you will find 50° 00′ *North Latitude*, and 12° 37′ of *Longitude*.

Example

Example 2.

What is the Latitude and Longitude of Bermudas, *one of the West-India Islands.*

Against *Bermudas* you will find *Lat.* 30° 20′ North, *Long.* 314° 00′.

2. *To find the Difference of Longitude between any two places.*

Take the *Longitudes* of the two *Places* out of the *Tables*, and substract the leſſer *Longitudes* out of the greater; and if the *Remainder* be *leſs* than 180°, that is the *Difference of Longitude*; but if the *Remainder* be *more* then 180°, ſubſtract it from 360°; the *laſt Remainder* is the *Difference of Longitude.*

Example 1.

What is the Difference of Longitude between Bermudas *and* Cape Raze *in* New-found-Land?

The *Longitude* of *Cape Raze* is	328°	30′
of *Bermudas*	314°	00′
The *Remainder* is the *Difference of Longitude*	14°	30′

Example 2.

What is the Difference of Longitude between the Lizard *&* Cape Raze?

The *Longitude* of *Cape Raze* is	328°	30′
of the *Lizard*	12°	37′
The *Remainder* is *greater* than 180°	315°	53′
Therefore ſubſtract it from	360°	00′
The *laſt Remainder* is the *Difference* of *Longitude*	44°	07′

3. *To know whether the Longitude between any two places be Eaſterly or Weſterly.*

1. When the *Remainder* firſt found is *leſs* than 180°, then if you are bound to that place which hath the *leſs Longitude*, your *Difference* of *Longitude* is *Weſterly*, and therefore you muſt ſayl to the *Weſtward*; but if you are bound to that which hath the *greater*, your *Difference* of *Longitude* is *Eaſterly*, and you muſt ſayl thither *Eaſtward.*

2. When the firſt *Remainder* is greater than 180°, then if you ſayl to that place, having the *greater Longitude*, your *Difference* of *Longitude* is *Weſterly*; if to that which hath the *leſs*, *Eaſterly.*

Here followeth a Table of Meridional Parts.

M	0 d.	1 d.	2 d.	3 d.	4 d.	5 d.	6 d.	7 d.	8 d.	9 d.	10 d	11 d
0	0	60	120	180	240	300	361	421	481	542	603	664
1	1	61	121	181	241	301	362	422	482	543	604	665
2	2	62	122	182	242	302	363	423	483	544	605	666
3	3	63	123	183	243	305	364	424	484	545	606	667
4	4	64	124	184	244	304	365	425	485	546	607	668
5	5	65	125	185	245	305	366	426	486	547	608	669
6	6	66	126	186	246	306	367	427	488	548	609	670
7	7	67	127	187	247	307	368	428	489	549	610	671
8	8	68	128	188	248	308	369	429	490	550	611	672
9	9	69	129	189	249	309	370	430	491	551	612	673
10	10	70	130	190	250	310	371	431	492	552	613	674
11	11	71	131	191	251	311	372	432	493	553	614	675
12	12	72	132	192	252	312	373	433	494	554	615	676
13	13	73	133	193	253	313	374	434	495	555	616	677
14	14	74	134	194	254	314	375	435	496	556	617	678
15	15	75	135	195	255	315	376	436	497	557	618	679
16	16	76	136	196	256	316	377	437	498	558	619	680
17	17	77	137	197	257	317	378	438	499	559	620	681
18	18	78	138	198	258	318	379	439	500	560	621	682
19	19	79	139	199	259	319	380	440	501	561	622	683
20	20	80	140	200	260	320	381	441	502	562	623	684
21	21	81	141	201	261	321	382	442	503	563	624	685
22	22	82	142	202	262	322	383	443	504	564	625	686
23	23	83	143	203	263	323	384	444	505	565	626	687
24	24	84	144	204	264	324	385	445	506	566	627	688
25	25	85	145	205	265	325	386	446	507	567	628	689
26	26	86	146	206	266	326	387	447	508	568	629	690
27	27	87	147	207	267	327	388	448	509	569	630	691
28	28	88	148	208	268	328	389	449	510	570	631	692
29	29	89	149	209	269	329	390	450	511	571	632	694
30	30	90	150	210	270	330	391	451	512	573	633	695
31	31	91	151	211	271	331	392	452	513	574	634	696
32	32	92	152	212	272	332	393	453	514	575	635	697
33	33	93	153	213	273	333	394	454	515	576	636	698
34	34	94	154	214	274	334	395	455	516	577	638	699
35	35	95	155	215	275	335	396	456	517	578	639	700
36	36	96	156	216	276	336	397	457	518	579	640	701
37	37	97	157	217	277	337	398	458	519	580	641	702
38	38	98	158	218	278	338	399	459	520	581	642	703
39	39	99	159	219	279	339	400	460	521	582	643	704
40	40	100	160	220	280	340	401	461	522	583	644	705
41	41	101	161	221	281	341	402	462	523	584	645	706
42	42	102	162	222	282	342	403	463	524	585	646	707
43	43	103	163	223	283	343	404	464	525	586	647	708
44	44	104	164	224	284	344	405	465	526	587	648	709
45	45	105	165	225	285	345	406	466	527	588	649	710
46	46	106	166	226	286	346	407	467	528	589	650	711
47	47	107	167	227	287	347	408	468	529	590	651	712
48	48	108	168	228	288	348	409	469	530	591	652	713
49	49	109	169	229	289	349	410	470	531	592	653	714
50	50	110	170	230	290	350	411	471	532	593	654	715
51	51	111	171	231	291	351	412	472	533	594	655	716
52	52	112	172	232	292	353	413	473	534	595	656	717
53	53	113	173	233	293	354	414	474	535	596	657	718
54	54	114	174	234	294	355	415	475	536	597	658	719
55	55	115	175	235	295	356	416	476	537	598	659	720
56	56	116	176	236	296	357	417	477	538	599	660	721
57	57	117	177	237	297	358	418	478	539	600	661	722
58	58	118	178	238	298	359	419	479	540	601	662	723
59	59	119	179	239	299	360	420	480	541	602	663	724

M.	12 d	13 d	14 d	15 d	16 d	17 d	18 d	19 d	20 d	21 d	22 d	23 d
0	725	787	848	910	973	1035	1038	1 00	1225	1289	1354	1419
1	726	788	848	911	974	36	1039	62	26	90	55	20
2	727	789	850	912	975	37	1100	63	27	91	56	21
3	728	790	851	913	976	38	1101	65	28	92	57	22
4	729	791	852	914	977	39	1102	66	29	93	58	23
5	730	792	854	916	978	40	1103	67	30	94	59	24
6	731	793	855	917	979	41	1104	63	31	96	60	25
7	732	794	856	918	980	42	1105	69	32	97	61	26
8	733	795	857	919	981	44	1107	70	34	98	62	27
9	734	796	858	920	982	45	1108	71	35	99	63	28
10	735	797	859	921	983	1046	1109	1172	1236	1300	1364	1429
11	736	798	860	922	984	47	10	73	37	01	65	30
12	737	799	861	923	985	48	11	74	38	02	67	31
13	738	800	862	924	986	49	12	75	39	03	68	33
14	740	801	863	925	987	50	13	76	40	04	69	34
15	741	802	864	926	988	51	14	77	41	05	70	35
16	742	803	865	927	989	52	15	78	42	06	71	36
17	743	804	866	928	990	53	16	79	43	07	72	37
18	744	805	867	929	991	54	17	80	44	08	73	38
19	745	806	868	930	992	55	18	81	45	09	74	39
20	746	807	869	931	993	1056	1119	1183	1246	1311	1375	1440
21	747	808	870	932	994	57	20	84	47	12	76	41
22	748	809	871	933	996	58	21	85	48	13	77	42
23	749	810	872	934	997	59	22	86	50	14	78	44
24	750	811	873	935	998	60	23	87	51	15	79	45
25	751	812	874	936	999	61	24	88	52	16	81	46
26	752	813	875	937	1000	62	25	89	53	17	82	47
27	753	814	876	938	1001	63	27	90	54	18	83	48
28	754	815	877	939	1002	64	28	91	55	19	84	49
29	755	816	878	940	1003	66	29	92	56	20	85	50
30	756	817	879	941	1004	1067	1130	1193	1257	1321	1386	1451
31	757	819	880	942	05	68	31	94	58	22	87	52
32	758	820	881	944	06	69	32	95	59	23	88	53
33	759	821	882	945	07	70	33	96	60	25	89	54
34	760	822	883	946	08	71	34	97	61	26	90	56
35	761	823	884	947	09	72	35	98	62	27	91	57
36	762	824	886	948	10	73	36	1200	63	28	92	58
37	763	825	887	949	11	74	37	1201	64	29	94	59
38	764	826	888	950	12	75	38	1202	66	30	95	60
39	765	827	889	951	13	76	39	1203	67	31	96	61
40	766	828	890	952	1014	1077	1140	1204	1268	1332	1397	1462
41	767	829	891	953	15	78	41	05	69	33	98	63
42	768	830	892	954	16	79	42	06	70	34	99	64
43	769	831	893	955	17	80	43	07	71	35	1400	65
44	770	832	894	956	18	81	44	08	72	36	1401	66
45	771	833	895	957	20	82	46	09	73	37	1402	68
46	772	834	896	958	21	83	47	10	74	38	1403	69
47	773	835	897	959	22	84	48	11	75	40	1404	70
48	774	836	898	960	23	85	49	12	76	41	1405	71
49	775	837	899	961	24	87	50	13	77	42	1407	72
50	776	838	900	962	1025	1088	1151	1214	1278	1343	1408	1473
51	777	839	901	963	26	89	52	15	79	44	09	74
52	778	840	902	964	27	90	53	16	81	45	10	75
53	779	841	903	965	28	91	54	18	82	46	11	76
54	780	842	904	966	29	92	55	19	83	47	12	77
55	782	843	905	967	30	93	56	20	84	48	13	78
56	783	844	906	968	31	94	57	21	85	49	14	80
57	784	845	907	969	32	95	58	22	86	50	15	21
58	785	846	908	971	33	96	59	23	87	51	16	82
59	786	847	909	972	34	97	60	24	88	52	17	83

M	24 d	25 d	26 d	27 d	28 d	29 d	30 d	31 d	32 d	33 d	34 d	35 d
0	1484	1550	1616	1683	1751	1819	1888	1958	2028	2099	2171	2244
1	85	51	17	85	52	20	89	59	29	2101	73	45
2	86	52	19	86	53	22	91	60	31	02	74	47
3	87	53	20	87	54	23	92	61	32	03	75	48
4	88	54	21	88	56	24	93	63	33	04	76	49
5	89	55	22	89	57	25	94	64	34	05	77	50
6	91	57	23	90	58	26	95	65	35	07	79	52
7	92	58	24	91	59	27	96	66	37	08	80	53
8	93	59	25	92	60	28	98	67	38	09	81	54
9	94	60	26	94	61	30	99	68	39	10	82	55
10	1495	1561	1628	1695	1762	1831	1900	1970	2040	2111	2183	2256
11	96	62	29	96	64	32	01	71	41	13	85	58
12	97	63	30	97	65	33	02	72	42	14	86	59
13	98	64	31	98	66	34	03	73	44	15	87	60
14	99	65	32	99	67	35	04	74	45	16	88	61
15	1500	66	33	1700	68	37	06	75	46	17	90	63
16	01	68	34	01	99	38	07	77	47	19	91	64
17	03	69	35	03	70	39	08	78	48	20	92	65
18	04	70	36	04	71	40	09	79	50	21	93	66
19	05	71	38	05	73	41	10	80	51	22	94	67
20	1506	1572	1639	1706	1774	1842	1911	1931	2052	2123	2196	2269
21	07	73	40	07	75	43	13	82	53	25	97	70
22	08	74	41	08	76	45	14	84	54	26	98	71
23	09	75	42	09	77	46	15	85	55	27	99	72
24	10	76	43	10	78	47	16	86	57	28	2200	74
25	11	78	44	12	79	48	17	87	58	29	02	75
26	12	79	45	13	81	49	18	88	59	31	03	76
27	14	80	46	14	82	50	20	89	60	32	04	77
28	15	81	48	15	83	51	21	91	61	33	05	78
29	16	82	49	16	84	53	22	92	63	34	06	80
30	1517	1583	1650	1717	1785	1854	1923	1993	2064	2135	2208	2281
31	18	84	51	18	86	55	24	94	65	37	09	82
32	19	85	52	19	87	56	25	95	66	38	10	83
33	20	86	53	21	89	57	26	97	67	39	11	85
34	21	87	54	22	90	58	28	98	69	40	13	86
35	22	89	55	23	91	59	29	99	70	41	14	87
36	23	90	57	24	92	61	30	2000	71	43	15	88
37	25	91	58	25	93	62	31	01	72	44	16	90
38	26	92	59	26	94	63	32	02	73	45	17	91
39	27	93	60	27	95	64	33	04	74	46	19	92
40	1528	1594	1661	1728	1797	1865	1935	2005	2076	2147	2220	2293
41	29	95	62	30	98	66	36	06	77	49	21	94
42	30	96	63	31	99	68	37	07	78	50	22	96
43	31	97	64	32	1800	69	38	08	79	51	23	97
44	32	99	65	33	01	70	39	09	80	52	25	98
45	33	1600	67	34	02	71	40	11	82	53	26	99
46	34	01	68	35	03	72	42	12	83	55	27	2301
47	36	02	69	36	04	73	43	13	84	56	28	02
48	37	03	70	37	06	74	44	14	85	57	30	03
49	38	04	71	39	07	76	45	15	86	58	31	04
50	1539	1605	1672	1740	1808	1877	1946	2017	2088	2159	2232	2306
51	40	06	73	41	09	78	47	18	89	61	33	07
52	41	07	74	42	10	79	49	19	90	62	34	08
53	42	09	75	43	11	80	50	20	91	63	36	09
54	43	10	77	44	12	81	51	21	92	64	37	11
55	44	11	78	45	14	83	52	22	93	65	38	12
56	45	12	79	47	15	84	53	24	95	67	39	13
57	47	13	80	48	16	85	54	25	96	68	41	14
58	48	14	81	49	17	86	56	26	97	69	42	15
59	49	15	82	50	18	87	57	27	98	70	43	17

M.	36 d	37 d	38 d	39 d	40 d	41 d	42 d	43 d	44 d	45 d	46 d	47 d
0	2318	2393	2468	2545	2623	2702	2782	2863	2946	3030	3116	3203
1	19	94	69	46	24	03	83	64	47	31	17	04
2	20	95	71	47	25	04	84	66	47	33	18	06
3	22	96	72	49	27	06	86	67	50	34	20	07
4	23	98	73	50	28	07	87	69	51	36	21	09
5	24	99	75	51	29	08	88	70	53	37	23	10
6	25	2400	76	53	30	10	90	71	54	38	24	12
7	27	01	77	54	32	11	91	73	56	40	26	13
8	28	03	78	55	33	12	92	74	57	41	27	14
9	29	04	80	56	34	14	94	75	58	43	29	16
10	2330	2405	2481	2558	2636	2715	2795	2877	2960	3044	3130	3217
11	32	06	82	59	37	16	97	78	61	46	31	19
12	33	08	83	60	38	17	98	80	63	47	33	20
13	34	09	85	62	40	19	99	81	64	48	34	22
14	35	10	86	63	41	20	2801	82	65	50	36	23
15	36	11	87	64	42	21	02	84	67	51	37	25
16	38	13	89	66	44	23	03	85	68	53	39	26
17	39	14	90	67	45	24	05	86	69	54	40	28
18	40	15	91	68	46	25	06	88	71	55	41	29
19	41	16	92	69	48	27	07	89	72	57	43	31
20	2343	2418	2494	2571	2649	2728	2808	2890	2974	3058	3144	3232
21	44	19	95	72	50	29	10	92	75	60	46	34
22	45	20	96	73	51	31	11	93	76	61	47	35
23	46	21	97	75	53	32	13	95	78	63	49	37
24	48	23	99	76	54	33	14	96	79	64	50	38
25	49	24	2500	77	55	35	15	97	81	65	52	40
26	50	25	01	78	57	36	17	99	82	67	53	41
27	51	26	03	80	58	37	18	2900	83	68	55	43
28	53	28	04	81	59	39	20	02	85	70	56	44
29	54	29	05	82	61	40	21	03	86	71	57	45
30	2355	2430	2506	2583	2661	2741	2822	2904	2988	3073	3159	3247
31	56	32	08	85	63	43	24	06	89	74	60	48
32	58	33	09	86	65	44	25	07	90	75	62	50
33	59	34	10	88	66	45	26	09	92	77	63	51
34	60	35	12	89	67	47	28	10	93	78	65	53
35	61	37	13	90	69	48	29	11	95	80	66	54
36	63	38	14	91	70	49	30	13	96	81	68	56
37	64	39	15	93	71	51	32	14	98	83	69	57
38	65	40	17	94	73	52	33	15	99	84	71	59
39	66	42	18	95	74	54	34	17	3000	85	72	60
40	2368	2443	2519	2597	2675	2755	2836	2918	3002	3087	3173	3262
41	69	44	20	98	76	56	37	19	03	88	75	63
42	70	45	22	99	78	58	39	21	05	90	76	65
43	71	47	23	2601	79	59	40	22	06	91	78	66
44	73	48	24	02	80	60	41	24	07	93	79	68
45	74	49	26	03	82	61	43	25	09	94	81	69
46	75	50	27	04	83	63	44	26	10	95	82	71
47	76	52	28	06	84	64	45	28	12	97	84	72
48	78	53	29	07	86	66	47	29	13	98	85	74
49	79	54	31	08	87	67	48	31	14	3100	87	75
50	2380	2456	2532	2610	2688	2769	2849	2933	3016	3101	3188	3277
51	81	57	33	11	90	70	51	33	17	03	90	78
52	83	58	35	12	91	71	52	35	19	04	91	80
53	84	59	36	14	92	72	54	36	20	06	93	81
54	85	61	37	15	94	74	55	37	22	07	94	83
55	86	62	38	16	95	75	56	39	23	08	95	84
56	88	63	40	17	96	76	58	40	24	10	97	86
57	89	64	41	19	98	78	59	42	26	11	98	87
58	90	66	42	20	99	79	60	43	27	13	3200	89
59	91	67	44	21	2700	80	62	45	29	14	01	90

M	48 d	49 d	50 d	51 d	52 d	53 d	54 d	55 d	56 d	57 d	58 d	59 d
0	3292	3382	3473	3569	3665	3765	3865	3968	4074	4183	4294	4409
1	93	84	76	70	67	67	66	70	76	85	96	11
2	95	85	78	72	69	69	68	72	78	86	98	13
3	96	87	79	74	70	70	70	73	79	88	4300	15
4	98	88	81	75	72	72	72	75	81	90	02	17
5	99	90	82	77	73	73	73	77	83	92	04	19
6	3301	91	84	78	75	75	75	79	85	93	06	21
7	02	93	85	80	77	77	77	80	87	96	08	23
8	04	94	87	82	78	78	78	82	88	97	10	25
9	05	96	89	83	80	79	80	84	90	99	12	27
10	3307	3397	3490	3585	3682	3780	3882	3986	4092	4201	1413	4429
11	08	99	92	86	83	82	83	87	94	03	15	31
12	10	3400	93	88	85	84	85	89	97	05	17	33
13	11	02	95	90	87	85	87	91	99	07	19	35
14	13	03	96	91	88	87	89	93	4100	09	21	37
15	14	05	98	93	90	89	90	94	01	10	23	39
16	16	07	99	94	91	91	92	96	03	12	25	41
17	17	08	3501	96	93	92	94	98	05	14	27	43
18	19	10	03	98	95	94	95	4000	06	16	29	44
19	20	11	04	99	96	96	97	01	08	18	31	46
20	3322	3413	3506	3600	3698	3797	3899	4003	4110	4220	4332	4448
21	23	14	07	02	3700	99	3901	05	12	22	34	50
22	25	16	09	04	01	3801	02	07	14	23	36	52
23	26	17	10	05	03	02	04	08	15	25	38	54
24	28	19	12	07	05	04	05	10	17	27	40	56
25	29	20	14	09	06	06	07	12	19	29	42	58
26	31	22	15	10	08	07	09	14	21	32	44	60
27	32	23	17	12	09	09	11	15	23	33	46	62
28	34	25	18	14	11	11	13	17	24	35	48	64
29	35	27	20	15	13	12	14	19	26	36	50	66
30	3337	3428	3521	3617	3714	3814	3916	4021	4128	4238	4352	4468
31	38	30	23	18	16	16	18	22	30	40	53	70
32	40	31	25	20	18	17	20	24	32	42	55	72
33	41	33	26	22	19	19	21	26	33	44	57	74
34	43	34	28	23	21	21	23	28	35	46	59	76
35	44	36	29	25	23	22	25	30	37	48	61	78
36	46	37	31	26	24	24	26	31	39	49	63	80
37	47	39	32	28	26	26	28	33	41	51	65	82
38	49	40	34	30	28	27	30	35	43	53	67	84
39	50	42	36	31	29	29	32	37	44	55	69	86
40	3352	3443	3537	3633	3731	3831	3933	4038	4146	4257	4371	4488
41	53	45	39	35	32	33	35	40	48	59	73	90
42	55	47	40	36	34	34	37	42	50	61	75	92
43	56	48	42	38	36	36	39	44	52	63	77	94
44	58	49	43	39	37	38	40	46	54	64	78	96
45	59	51	45	41	39	39	42	47	55	66	80	98
46	61	53	47	43	41	41	44	49	57	68	82	4500
47	62	54	48	44	42	43	45	51	59	70	84	02
48	64	56	50	46	44	44	47	53	61	72	86	04
49	65	57	51	48	46	46	49	54	63	74	88	06
50	3367	3459	3553	3649	3747	3848	3951	4056	4164	4276	4390	4508
51	68	61	55	51	49	49	52	58	66	78	92	10
52	70	62	56	52	51	51	54	60	68	79	94	12
53	71	64	58	54	52	53	56	62	70	81	96	14
54	73	65	59	56	54	55	58	63	72	83	98	16
55	74	67	61	57	56	56	59	65	74	85	4400	18
56	76	68	62	59	57	58	61	67	75	87	02	20
57	78	70	64	60	59	60	63	69	77	89	04	22
58	79	71	66	62	61	61	65	70	79	91	05	24
59	81	73	67	64	62	63	66	72	81	93	07	26

M	60 d	61 d	62 d	63 d	64 d	65 d	66 d	67 d	68 d	69 d	70 d	71 d
0	4528	4649	4775	4905	5040	5179	5324	5474	5631	5795	5967	6146
1	30	52	77	07	42	82	26	77	34	98	70	50
2	32	54	80	10	44	84	29	80	37	5801	72	53
3	34	56	82	12	47	86	31	82	39	04	75	56
4	36	58	84	14	49	89	34	85	42	06	78	59
5	38	60	86	16	51	91	36	87	45	09	81	62
6	40	62	88	19	53	93	39	90	47	12	84	65
7	42	64	90	21	56	96	41	92	50	15	87	68
8	44	66	92	23	58	98	44	95	53	18	90	71
9	46	68	95	25	60	5201	46	98	55	20	93	74
10	4548	4670	4797	3927	5063	5203	5349	5500	5658	5823	5996	6177
11	50	72	99	30	65	05	51	03	61	26	99	80
12	52	74	4801	32	67	08	54	05	64	29	6002	83
13	54	76	03	34	70	10	56	08	66	32	05	87
14	56	78	05	36	72	12	59	11	69	34	08	90
15	58	81	07	38	74	15	61	13	72	37	11	93
16	60	83	10	41	76	17	64	16	74	40	14	96
17	62	85	12	43	79	20	66	18	77	43	17	99
18	64	87	14	45	81	22	68	21	80	46	20	6202
19	66	89	16	47	83	24	71	23	82	49	23	05
20	4568	4691	4818	2950	5086	5227	5373	5526	5685	5851	6026	6208
21	70	93	20	52	88	29	76	29	88	54	29	12
22	72	95	22	54	90	32	78	31	91	57	32	15
23	74	97	25	56	93	34	81	34	93	60	34	18
24	76	99	27	59	95	36	83	37	96	63	38	21
25	78	4701	29	61	97	39	86	39	99	66	40	24
26	80	04	31	63	5100	41	88	42	5701	68	43	27
27	82	06	33	65	02	44	91	44	04	71	46	30
28	84	08	35	67	04	46	93	47	07	74	49	34
29	86	10	38	70	07	48	96	49	10	77	52	37
30	4588	4712	4840	4972	5109	5251	5398	5552	5712	5880	6055	6240
31	90	14	42	74	11	53	5401	55	15	83	58	43
32	92	16	44	76	14	56	03	57	18	86	61	46
33	94	18	46	79	16	58	06	60	21	88	64	49
34	96	20	48	81	18	61	09	63	23	91	67	52
35	98	22	51	83	20	63	11	65	26	94	70	56
36	4600	24	53	85	23	65	14	68	29	97	73	59
37	02	27	55	88	25	68	16	70	32	5900	76	62
38	04	29	57	90	27	70	19	73	34	03	79	65
39	06	31	59	92	30	73	21	76	37	06	82	68
40	4608	4733	4861	4994	5132	5275	5424	5578	5740	5909	6085	6271
41	10	35	64	97	35	78	26	81	42	11	89	75
42	13	37	66	99	37	80	29	84	45	14	92	78
43	15	39	68	5001	39	82	31	86	48	17	95	81
44	17	41	70	03	42	85	34	89	51	20	98	84
45	19	43	72	06	44	87	36	92	54	23	6101	87
46	21	46	75	08	46	90	39	94	56	26	04	91
47	23	48	77	10	49	92	41	97	59	29	07	94
48	25	50	80	12	51	95	44	99	62	32	10	97
49	27	52	81	15	53	97	46	5602	65	35	13	6200
50	4629	4754	4883	5017	5156	5299	5449	5605	5767	5937	6116	6303
51	31	56	85	20	58	5302	52	07	70	40	20	07
52	33	58	88	22	60	04	54	10	73	43	22	10
53	36	60	90	24	63	07	58	13	76	46	25	13
54	37	63	92	26	65	09	59	15	78	49	28	16
55	38	65	94	28	67	12	62	18	81	52	31	19
56	41	67	96	31	70	14	64	21	84	55	34	23
57	42	69	99	33	72	17	67	23	87	58	37	26
58	35	71	4901	35	74	19	69	26	90	61	40	29
59	47	73	03	38	77	21	72	29	92	64	43	32

M	p 72	p 73	p 74	p 75	p 76	p 77	p 78	p 79	p 80	p 81	p 82	p 83
0	6330	6535	6717	6971	7211	7469	7746	8017	8377	8741	9148	9509
1	39	39	50	75	15	73	51	53	83	48	55	17
2	42	42	54	77	20	76	56	58	89	54	63	20
3	45	46	58	83	24	82	61	63	95	61	70	34
4	49	49	61	87	28	86	65	69	8400	67	77	42
5	52	52	65	91	32	91	70	74	06	74	84	50
6	55	56	69	95	36	95	75	79	12	80	91	59
7	58	59	72	99	40	7500	80	84	18	87	99	67
8	62	63	76	7003	45	04	85	90	24	93	9206	75
9	65	66	80	06	49	09	90	95	30	99	14	84
10	6368	6573	6733	7010	7253	7513	7795	8100	8435	8806	9221	9692
11	71	73	87	14	57	18	99	06	41	13	28	9701
12	75	77	91	18	61	22	7804	11	47	19	36	09
13	78	80	94	22	65	27	09	16	53	25	43	18
14	81	84	98	26	70	31	14	22	59	32	50	26
15	85	87	6802	30	74	36	19	27	65	39	58	35
16	88	90	05	34	78	40	24	32	71	45	65	43
17	91	94	09	38	82	45	29	38	77	52	73	52
18	95	97	13	42	87	50	34	43	83	59	80	60
19	98	6601	16	46	91	54	39	49	89	65	88	69
20	6401	6605	6820	7050	7295	7559	7844	8154	8494	8872	9295	9777
21	04	08	24	54	99	63	49	59	8500	78	9303	86
22	08	11	27	58	7303	68	54	65	06	85	10	95
23	11	15	31	61	08	72	59	70	12	91	18	9803
24	14	18	35	65	12	77	64	76	18	98	25	12
25	18	22	39	69	16	82	69	81	24	8905	33	21
26	21	25	42	73	21	86	74	87	30	12	40	30
27	24	29	46	77	25	91	79	92	36	19	48	38
28	27	32	50	81	29	95	84	98	42	25	56	47
29	31	36	54	85	33	7600	89	8203	49	32	63	56
30	6434	6633	6857	7089	7336	7605	7934	8208	8555	8939	9371	9865
31	37	43	61	93	42	09	99	14	01	46	79	74
32	41	47	65	97	46	14	7904	19	67	52	88	82
33	44	50	69	7101	50	19	09	25	73	59	94	91
34	47	54	72	05	55	23	14	31	79	66	9402	9900
35	51	57	76	09	59	28	19	36	85	73	10	09
36	54	61	80	13	63	32	24	42	91	80	17	18
37	57	64	84	17	68	37	29	47	97	87	25	27
38	61	68	87	21	72	42	34	53	8603	93	33	36
39	64	71	91	26	76	46	39	58	10	9000	41	45
40	6468	6675	6895	7130	7381	7651	7944	8264	8610	9007	9449	9954
41	71	78	99	34	85	56	49	69	22	14	56	63
42	74	82	6903	38	89	61	54	75	28	21	64	73
43	78	86	00	42	94	65	59	80	34	28	72	81
44	81	89	10	46	98	70	65	86	41	35	80	91
45	84	93	14	50	7403	75	70	92	47	42	88	10000
46	88	96	18	54	07	79	75	97	53	49	96	009
47	91	6700	22	58	11	84	80	8303	59	56	9504	018
48	94	03	25	62	16	89	85	09	65	63	12	028
49	98	07	29	66	20	94	90	15	72	70	20	037
50	6501	6711	6933	7170	7424	7698	7995	8320	8678	9077	9528	10046
51	05	14	37	74	29	7703	8001	26	84	84	36	056
52	05	18	41	78	33	08	05	31	91	91	44	065
53	11	21	44	82	38	13	11	37	97	98	52	074
54	15	25	48	87	42	17	16	43	8703	9105	60	084
55	18	29	52	91	46	22	21	49	10	12	68	093
56	22	32	56	95	51	27	27	54	16	20	76	10103
57	25	36	60	99	55	32	32	60	22	27	85	112
58	28	39	64	7203	59	37	35	66	29	34	93	122
59	32	43	68	07	64	41	42	71	35	41	9601	131

M	84 d	85 d	86 d	87 d	88 d	89 d
0	10141	10770	11539	12521	13920	16317
1	150	781	553	540	919	376
2	160	793	568	559	978	435
3	170	804	582	579	14007	495
4	179	816	597	598	037	557
5	189	827	611	618	067	619
6	199	839	626	638	097	683
7	209	851	641	658	127	748
8	218	863	656	678	158	814
9	228	875	671	698	189	881
10	10238	10886	11686	12718	14220	16950
11	248	899	701	738	252	17020
12	258	910	716	759	284	092
13	268	922	731	779	316	165
14	278	934	746	800	348	240
15	288	946	761	821	381	316
16	298	958	777	842	414	394
17	308	971	792	863	448	474
18	318	983	808	884	482	556
19	328	995	823	906	515	640
20	10338	11007	11839	12927	14550	17726
21	348	020	855	949	584	814
22	358	032	870	970	619	904
23	368	044	886	992	655	997
24	379	057	902	13014	691	18093
25	389	070	918	037	727	191
26	399	082	934	059	764	292
27	410	095	950	081	800	396
28	420	107	967	104	838	503
29	430	120	983	127	876	615
30	10441	11133	11999	13150	14914	18729
31	451	146	12016	172	952	848
32	462	158	032	196	991	971
33	472	171	049	219	15031	19098
34	483	184	066	243	071	230
35	494	197	083	267	111	368
36	504	210	099	291	152	511
37	515	223	116	315	194	660
38	526	236	133	339	236	817
39	536	248	150	363	278	980
40	10547	11263	12167	13388	15321	20152
41	558	276	185	413	365	333
42	569	289	202	437	409	524
43	579	303	220	463	453	728
44	590	316	237	488	499	941
45	601	330	255	513	545	21170
46	612	343	273	539	591	416
47	623	357	290	565	638	680
48	634	371	308	591	686	967
49	645	384	326	617	734	22279
50	10656	11398	12344	13643	15783	22613
51	668	412	363	670	833	23005
52	679	426	381	697	884	23435
53	690	440	399	724	935	23910
54	701	454	418	751	987	24409
55	713	468	426	779	16040	25786
56	724	482	445	807	094	26046
57	735	496	464	834	148	27192
58	747	510	483	863	204	28911
59	758	555	502	891	260	32348

The Use of the Table of Meridional Parts.

In this *Table*, the left hand Column upon every Page under M, begining at 1 and ending at 59, contains the *minutes* answering to every *degree* of *Latitude:* The other Columns, distinguished by 1 *d*, 2 *d*, &c. to 89 *d*, contains the *Meridional Parts* answering to every *degree* of *Latitude*. The *use* of these Columns together, is to find the *Meridional Parts* for every *degree* and *minute* of *Latitude*; an *Example* or two will sufficiently explain it.

Example 1.

The *Latitude* of 51 *deg.* 12 *min.* to find the *Meridional Parts.*

In the Column under 51 *d.* and right against 12 M. in the *left hand Column*, stands 88, and joyning 35, the two figures in the same *Column*, that stand next above 88 towards the *left hand*, the whole is 3588, the *Meridional Parts* required.

Example 2.

The *Latitude* of 87 *deg.* 52 *min.* to find the *Meridional Parts.*

In the *Column* under 57 *d.* and right against 52 M. in the *left hand Column*, stands 667, to which joyning 13 towards the *left hand*, the whole is 13667. the *Meridional Parts* required.

The Use of these *Meridional Parts* are shown in the *Problem* of *Mercators Sayling*, *Chap.* 5.

A New and Exact Kalender, shewing the *Prime*, *Epact*, *Dominical Letters*, and *Leap-years*, for 28 years. Also the dayes of the Month, and remarkable dayes: With Tables of the Suns true place in the Ecliptick: And the Declination of the Sun for 60 years to come, and may indifferently serve for as many more: Calculated from those Excellent Tables of Mr. *Tho. Street*, in his Book called *Astr. Car.* &c.

Years	Prime.	Epact.	Domin.	Cycle ☉	Shrove-Sunday.	Easter-Sunday.	Whit-Sunday.
1669	17	7	C	26	*Feb.* 21	*April* 11	*May* 30
1670	18	18	B	27	13	3	22
1671	19	29	A	28	5	23	*June* 11
1672	1	11	G F	1	*Mar.* 18	7	*May* 26
1673	2	22	E	2	*Feb.* 9	*Mar.* 30	18
1674	3	3	D	3	*Mar.* 1	*April* 19	*June* 7
1675	4	14	C	4	*Feb.* 14	4	*May* 23
1676	5	25	B A	5	6	*Mar.* 26	4
1677	6	6	G	6	25	*April* 15	*June* 3
1678	7	17	F	7	10	*Mar.* 31	*May* 19
1679	8	28	E	8	*Mar.* 2	*April* 20	*June* 8
1680	9	9	D C	9	*Feb.* 22	11	*May* 30
1681	10	20	B	10	13	3	22
1682	11	1	A	11	26	16	*June* 4
1683	12	12	G	12	18	8	*May* 27
1684	13	23	F E	13	10	*Mar.* 30	18
1685	14	4	D	14	*Mar.* 1	*April* 19	*June* 7
1686	15	15	C	15	*Feb.* 14	4	*May* 23
1687	16	26	B	16	6	*Mar.* 27	15
1688	17	7	A G	17	26	*April* 15	*June* 13
1689	18	18	F	18	10	*Mar.* 31	*May* 19
1690	19	29	E	19	*Mar.* 2	*April* 20	*June* 8
1691	1	11	D	20	*Feb.* 23	12	*May* 31
1692	2	22	C B	21	7	*Mar.* 27	15
1693	3	3	A	22	26	*April* 16	*June* 4
1694	4	14	G	23	18	8	*May* 27
1695	5	25	F	24	3	25	12
1696	6	6	E D	25	23	12	31

January hath XXXI dayes.

Month days	Week days	Remarkable dayes, & southing of Stars at midnight.	First Year, 1669. ☉ Pla	First Year, 1673. ☉ dec.	Second Year, 1670. ☉ pla	Second Year, 1674. ☉ dec.	Third Year, 1671. ☉ pla	Third Year, 1675. ☉ dec.	Leap Year, 1672. ☉ pla.	Leap Year, 1676. ☉ dec
			D. M	D. M.	D. M	D. M.	D. M	D. M.	D. M.	D. M.
			♑	South.	♑	South.	♑	South.	♑	South.
01	A	*N. years d.*	21 51	21 42	22 43	21 45	21 28	21 47	21 15	21 40
02	B		22 55	21 32	22 44	21 35	22 25	21 37	22 15	21 39
03	C		24 00	21 22	23 45	21 24	23 31	21 27	23 16	21 29
04	D		25 01	21 11	24 47	21 14	24 32	21 16	24 17	21 19
05	E		26 03	21 00	25 48	21 02	25 33	21 05	25 18	21 08
06	I	Epiphania	27 04	20 48	26 49	20 51	26 34	20 54	26 15	20 56
07	G		28 05	20 36	27 50	20 39	27 35	20 42	27 20	20 45
08	A		29 06	20 24	28 51	20 27	28 36	20 30	28 21	20 33
09	B	☉ in ♒	♒ 07	20 11	29 52	20 14	29 37	20 17	29 22	20 20
10	C	A.B. *Cant.*	01 08	19 57	♒ 53	20 01	♒ 38	20 04	♒ 23	20 07
11	D	Bch. 1644	02 09	19 44	01 54	19 47	01 39	19 51	01 25	19 54
12	E		03 10	19 30	02 55	19 33	02 40	19 37	02 26	19 40
13	I		04 11	19 16	03 56	19 19	03 41	19 23	03 27	19 26
14	G		05 12	19 01	04 57	19 05	04 42	19 08	04 28	19 12
15	A		06 13	18 46	05 58	18 50	05 43	18 52	05 29	18 57
16	B		07 14	18 31	06 59	18 34	06 44	18 38	06 30	18 42
17	C	So. arms of	08 15	18 15	08 00	18 19	07 45	18 23	07 31	18 26
18	D	the Crab.	09 16	17 59	09 01	18 03	08 46	18 07	08 31	18 11
19	E	13d. 8m. ☽	10 17	17 43	10 02	17 47	09 47	17 51	09 32	17 55
20	F		11 18	17 26	11 03	17 30	10 48	17 34	10 33	17 38
21	G		12 18	17 09	12 04	17 13	11 49	17 17	11 34	17 21
22	A		13 19	16 52	13 04	16 56	12 50	17 00	12 35	17 04
23	B	Term beg.	14 20	16 33	14 05	16 39	13 51	16 43	13 36	16 47
24	C		15 20	16 16	15 06	16 21	14 51	16 25	14 37	16 30
25	D	Hydra's	16 22	15 58	16 07	16 03	15 52	16 07	15 37	16 12
26	E	heart, *ad.*	17 23	15 40	17 08	15 44	16 53	15 49	16 38	15 53
27	F	*Iam. S.*	18 23	15 21	18 08	15 26	17 54	15 30	17 39	15 35
28	G		19 24	15 02	19 09	15 07	18 54	15 12	18 40	15 16
29	A		20 24	14 43	20 10	14 48	19 55	14 53	19 40	14 57
30	B		21 25	14 24	21 10	14 29	20 56	14 33	20 41	14 38
31	C		22 26	14 04	22 11	14 09	21 56	14 14	21 42	14 19

Month days.	Week dayes.	Remarkable dayes, & southing of Stars at Mid.night.	First Year, 1669. ☉ pla.		1673. ☉ dec.		Second Year, 1670. ☉ pla.		1674. ☉ dec.		Third Year, 1671. ☉ pla		1675. ☉ dec.		Leap Year, 1672. ☉ pla.		1676 ☉ dec.	
			D.	M.	D.	M	D.	M.	D.	M.	D.	M	D.	M.	D.	M.	D.	M
			♒		South		♒		South.		♒		South.		♒		South.	
01	D		23	26	13	44	23	12	13	49	22	57	13	54	22	42	13	55
02	E		24	27	13	24	24	12	13	29	23	57	13	34	23	43	13	35
03	F	Lions hear	25	27	13	04	25	13	13	09	24	58	13	14	24	43	13	15
04	G	13.36.N.	26	28	12	44	26	13	12	49	25	58	12	54	25	44	12	55
05	A	Lions neck	27	28	12	25	27	14	12	28	26	59	12	33	26	44	12	38
06	B	25. 5. N.	28	29	12	02	28	14	12	07	27	59	12	11	27	45	12	17
07	C		29	29	11	41	29	15	11	46	29	00	11	51	28	45	11	56
08	D	☉ in ♓.	♓	30	11	19	♓	15	11	25	♓	00	11	30	29	46	11	35
09	E		01	30	10	58	01	15	11	03	01	01	11	09	♓	46	11	14
10	F		02	30	10	36	02	16	10	42	02	01	10	47	01	46	10	52
11	G		03	31	10	15	03	16	10	20	03	01	10	25	02	47	10	31
12	A		04	31	09	53	04	16	09	58	04	02	10	03	03	47	10	09
13	B		05	31	09	31	05	16	09	36	05	02	09	41	04	47	09	47
14	C	(58.12.N.	06	31	09	08	06	17	09	14	06	02	09	19	05	47	09	25
15	D	G.Bear fid	07	31	08	46	07	17	08	52	07	02	08	57	06	48	09	02
16	E	Gr. Bears back, 63.	08	32	08	24	08	17	08	29	08	02	08	35	07	48	08	40
17	F	55. N.	09	32	08	01	09	17	08	06	09	03	08	12	08	48	08	17
18	G		10	32	07	38	10	17	07	44	10	03	07	49	09	48	07	55
19	A		11	32	07	15	11	17	07	21	11	03	07	27	10	48	07	32
20	B		12	32	06	52	12	17	06	58	12	03	07	04	11	48	07	09
21	C	Lions back	13	32	06	29	13	17	06	35	13	03	06	41	12	48	06	46
22	D	22.22.N.	14	32	06	06	14	17	06	12	14	03	06	18	13	48	06	23
23	E		15	32	05	43	15	17	05	49	15	03	05	54	14	48	06	00
24	F	*Matthias.*	16	32	05	20	16	17	05	26	16	03	05	31	15	48	05	37
25	G		17	31	04	57	17	17	05	02	17	02	05	08	16	48	05	14
26	A		18	31	04	33	18	17	04	39	18	02	04	44	17	48	04	50
27	B		19	31	04	10	19	17	04	15	19	02	04	21	18	48	04	27
28	C		20	31	03	46	20	16	3	52	20	02	03	58	19	47	04	03
29	D														20	47	03	40

When it is Leap year, *Feb.* hath 29 dayes, and then St. *Matthias* is on the 25th day.

March hath XXXI dayes.

Month days.	Week days.	Remarkable dayes, & southing of Stars a Midnight.	First Year, 1669. / 1673. ☉ pla.	First Year, 1669. / 1673. ☉ dec.	Second Year, 1670. / 1674. ☉ pla.	Second Year, 1670. / 1674. ☽ dec.	Third Year, 1671. / 1675. ☉ pla.	Third Year, 1671. / 1675. ☉ dec.	Leap Year, 1672. / 1676. ☉ pla.	Leap Year, 1672. / 1676. ☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			♓	South.	♓	South.	♓	South.	♓	South.
01	D	*David.* (N	21 30	03 23	21 16	03 28	21 02	03 34	21 47	03 16
02	E	L. T. 16. 28	22 30	02 59	22 16	03 05	22 01	03 10	22 46	02 52
03	F	Gr. Bear	23 30	02 35	23 15	02 41	23 01	02 47	23 46	02 29
04	G	high, 55 36 N.	24 29	02 12	24 15	02 17	24 01	02 23	24 46	02 05
05	A		25 29	01 48	25 15	02 54	25 00	01 59	25 45	01 42
06	B		26 29	01 24	26 14	01 30	26 00	01 36	26 45	01 18
07	C		27 28	01 01	27 14	01 06	26 59	01 12	27 44	00 54
08	D		28 28	00 37	28 13	00 43	27 59	00 48	28 44	00 30
09	E		29 27	00 13	29 13	00 19	28 58	00 25	29 43	00 07
10	F	☉ in ♈.	♈ 26	*Nor* 11	♈ 12	*Nor* 05	29 58	00 01	♈ 43	*Nor* 17
11	G		01 26	00 34	01 11	00 28	♈ 57	*Nor* 23	01 42	00 41
12	A		02 25	00 58	02 11	00 52	01 56	00 46	02 41	01 04
13	B		03 24	01 21	03 10	01 16	02 56	01 10	03 40	01 28
14	C		04 24	01 45	04 09	01 39	03 55	01 34	04 40	01 51
15	D		05 23	02 09	05 08	02 03	04 54	01 57	05 39	02 15
16	E		06 22	02 32	06 08	02 26	05 53	02 21	06 38	02 38
17	F		07 21	02 55	07 07	02 50	06 52	02 44	07 37	03 02
18	G		08 20	03 19	08 06	03 13	07 52	03 08	08 36	03 25
19	A		09 19	03 42	09 05	03 37	08 51	03 31	09 35	03 48
20	B	First in Gr	10 18	04 05	10 04	04 00	09 50	03 54	10 34	04 12
21	C	Bears tayl 57 50 N.	11 17	04 29	11 03	04 23	10 49	04 17	11 33	04 35
22	D		12 16	04 52	12 02	04 46	11 48	04 41	12 32	04 58
23	E		13 15	05 15	13 01	05 09	12 47	05 04	13 31	05 21
24	F		14 14	05 38	14 00	05 32	13 46	05 27	14 30	05 44
25	G	*Anun. Ma*	15 13	06 00	14 59	05 55	14 45	05 49	15 29	06 07
26	A		16 12	06 23	15 58	06 18	15 43	06 12	16 28	06 29
27	B		17 11	06 46	16 56	06 40	16 42	06 35	17 27	06 52
28	C	Virg. spik (9 12 S.	18 10	07 08	17 55	07 03	17 41	06 57	18 26	07 14
29	D	and in Gr	19 08	07 31	18 54	07 25	18 40	07 20	19 24	07 37
30	E	Bears tayl	20 07	07 53	19 53	07 48	19 39	07 42	20 23	07 59
31	F	56 44 N.	21 06	08 15	20 51	08 10	20 37	08 04	21 22	08 21

Month days.	Week dayes.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669 1673. ☉ pla.	First Year, 1669 1673. ☉ dec.	Second Year, 1670. 1674 ☉ pla.	Second Year, 1670. 1674 ☉ dec.	Third Year, 1671. 1675. ☉ pla.	Third Year, 1671. 1675. ☉ dec.	Leap Year, 1672. 1676 ☉ pla.	Leap Year, 1672. 1676 ☉ dec
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			♈	North.	♈	North.	♈	North.	♈	North.
01	G		22 04	08 37	21 50	08 32	21 36	08 26	22 20	08 43
02	A		23 03	08 59	22 49	08 54	22 34	08 48	23 19	09 05
03	B		24 01	09 21	23 47	09 15	23 33	09 10	24 17	09 26
04	C		25 00	09 42	24 46	09 37	24 32	09 32	25 16	09 48
05	D	3d in G.B Bears tayl,	25 58	10 03	25 44	09 58	25 30	09 53	26 14	10 09
06	E	51. 3. N.	26 57	10 25	26 43	10 20	26 29	10 14	27 13	10 30
07	F		27 55	10 46	27 41	10 41	27 27	10 36	28 11	10 51
08	G	Centaur's shoulder.	28 54	11 07	28 40	11 02	28 25	10 56	29 10	11 12
09	A	35. 16. S.	29 52	11 27	29 38	11 22	29 24	11 17	♉ 08	11 33
10	B	☉ in ♉.	♉ 51	11 48	♉ 36	11 43	♉ 22	11 38	01 06	11 53
11	C		01 49	12 08	01 35	12 04	01 21	11 58	02 05	12 14
12	D	Arcturus	02 47	12 28	02 33	12 23	02 19	12 18	03 03	12 34
13	E	21. 1. N.	03 45	12 48	03 31	12 43	03 17	12 38	04 01	12 53
14	F		04 44	13 08	04 29	13 03	04 15	12 58	04 59	13 13
15	G		05 42	13 27	05 28	13 23	05 14	13 18	05 58	13 33
16	A		06 40	13 46	06 26	13 42	06 12	13 37	06 56	13 52
17	B		07 38	14 06	07 24	14 01	07 10	13 56	07 54	14 11
18	C		08 36	14 24	08 22	14 20	08 08	14 15	08 52	14 29
19	D		09 34	14 43	09 20	14 38	09 06	14 34	09 50	14 48
20	E	S. Ballance	10 32	15 01	10 18	14 57	10 04	14 52	10 48	15 06
21	F	14. 34. S.	11 30	15 19	11 16	15 15	11 02	15 11	11 46	15 24
22	G		12 28	15 37	12 14	15 33	12 00	15 29	12 44	15 42
23	A		13 26	15 55	13 12	15 51	12 58	15 46	13 42	15 59
24	B		14 24	16 12	14 10	16 08	13 56	16 04	14 40	16 17
25	C		15 22	16 29	15 08	16 25	14 54	16 21	15 38	16 34
26	D		16 20	16 46	16 06	16 42	15 52	16 38	16 36	16 50
27	E	(75. 38. N. Form. gar.	17 18	17 02	17 04	16 58	16 50	16 54	17 34	17 07
28	F	N. Ballanc 8. 5. S.	18 16	17 19	18 02	17 15	17 48	17 11	18 32	17 23
29	G		19 14	17 35	19 00	17 31	18 46	17 27	19 29	17 39
30	A		20 11	17 50	19 57	17 46	19 43	17 43	20 27	17 54

Month days.	Week dayes.	Remarkable dayes, & scouthing of Stars at Midnight.	First Year, 1669. / 1673. ☉ pla.	☉ dec.	Second Year, 1670. / 1674. ☉ pla.	☉ dec.	Third Year, 1671. / 1675. ☉ pla.	☉ dec.	Leap Year, 1672. / 1676. ☉ pla.	☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			♉	North.	♉	North.	♉	North.	♉	North.
01	B	*Phil.* & *Ja*	21 09	18 06	20 55	18 02	20 41	17 58	21 25	18 10
02	C	(27. 53. N.	22 07	18 21	21 53	18 17	21 39	18 13	22 23	18 25
03	D	Luc. coron	23 05	18 35	22 51	18 32	22 37	18 28	23 20	18 39
04	E	Hind. quar	24 02	18 50	23 48	18 46	23 34	18 43	24 18	18 54
05	F	73 16. N.	25 00	19 04	24 46	19 00	24 32	18 57	25 16	19 08
06	G	Serp. Neck	25 58	19 18	25 44	19 14	25 30	19 11	26 13	19 21
07	A	7. 33. N.	26 55	19 31	26 41	19 28	26 27	19 25	27 11	19 35
08	B		27 53	19 44	27 39	19 41	27 25	19 38	28 09	19 48
09	C		28 50	19 57	28 36	19 54	28 22	19 51	29 06	20 01
10	D	☉ in ♊.	29 48	20 10	29 34	20 07	29 20	20 04	♊ 04	20 13
11	E		♊ 45	20 22	♊ 32	20 19	♊ 18	20 16	01 01	20 25
12	F		01 43	20 33	01 29	20 31	01 15	20 28	01 59	20 37
13	G		02 40	20 45	02 27	20 42	02 13	20 39	02 56	20 48
14	A		03 38	20 56	03 24	20 53	03 10	20 51	03 54	20 59
15	B		04 35	21 07	04 22	21 04	04 08	21 02	04 51	21 10
16	C	Scor. heart	05 33	21 17	05 19	21 15	05 05	21 12	05 49	21 20
17	D	25. 35. S.	06 30	21 27	06 16	21 25	06 03	21 22	06 46	21 30
18	E		07 28	21 37	07 14	21 34	07 00	21 32	07 43	21 39
19	F		08 25	21 46	08 11	21 44	07 57	21 41	08 41	21 48
20	G		09 23	21 55	09 09	21 53	08 55	21 50	09 38	21 57
21	A		10 20	22 03	10 06	22 01	09 52	21 59	10 36	22 06
22	B		11 17	22 11	11 03	22 09	10 49	22 07	11 33	22 13
23	C		12 15	22 19	12 01	22 17	11 47	22 15	12 30	22 21
24	D		13 12	22 26	12 58	22 25	12 44	22 23	13 28	22 28
25	E	Serp. Knee	14 09	22 33	13 55	22 32	13 41	22 30	14 25	22 35
26	F	15. 14. S.	15 07	22 40	14 53	22 38	14 39	22 37	15 22	22 42
27	G	Herc. head	16 04	22 46	15 50	22 45	15 36	22 43	16 20	22 48
28	A	14. 50.	17 01	22 52	16 47	22 51	16 33	22 49	17 17	22 53
29	B	*K. Ch II.*	17 58	22 57	17 44	22 56	17 31	22 55	18 14	22 58
30	C	*Nat & Re*	18 56	23 02	18 42	23 01	18 28	23 00	19 11	23 03
31	D	1660.	19 52	23 07	19 39	23 06	19 25	23 05	20 09	23 08

Month days.	Week days.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669 | 1673. ☉ pla. D. M.	☉ dec. D. M.	Second Year, 1670. 1674 ☉ pla. D. M.	☉ dec. D. M.	Third Year, 1671. 1675. ☉ pla. D. M.	☉ dec. D. M.	Leap Year, 1672 | 1676. ☉ pla. D. M.	☉ dec. D. M.
			♊	North.	♊	North.	♊	North.	♊	North.
01	E		20 50	23 11	20 36	23 10	20 22	23 09	21 06	23 12
02	F		21 47	23 15	21 33	23 14	21 20	23 13	22 03	23 16
03	G	*Dutch* Engagement, 1652. 65.	22 45	23 18	22 31	23 17	22 17	23 16	23 00	23 19
04	A		23 42	23 21	23 28	23 20	23 14	23 20	23 57	23 22
05	B		24 39	23 23	24 25	23 23	24 11	23 22	24 55	23 24
06	C		25 36	23 26	25 22	23 25	25 08	23 25	25 52	23 26
07	D	Sagit. Ar. head, 30. S.	26 33	23 27	26 19	23 27	26 06	23 27	26 49	23 28
08	E	Drag. head	27 30	23 29	27 17	23 28	27 03	23 28	27 46	23 29
09	F	51. 36. N.	28 28	23 29	28 14	23 29	28 00	23 29	28 43	23 30
10	G		29 25	23 30	29 11	23 30	28 57	23 30	29 41	23 30
11	A	☉ in ♋	♋ 22	23 30	♋ 08	23 30	29 54	23 30	♋ 38	23 30
12	B		01 19	23 30	01 05	23 30	♋ 52	23 30	01 35	23 29
13	C		02 16	23 29	02 02	23 29	01 49	23 29	02 32	23 28
14	D		03 14	23 28	03 00	23 28	02 46	23 28	03 29	23 27
15	E		04 11	23 26	03 57	23 26	03 43	23 27	04 26	23 25
16	F		05 08	23 24	04 54	23 25	04 40	23 25	05 23	23 23
17	G	Lyra, 38.	06 05	23 22	05 51	23 22	05 37	23 23	06 21	23 21
18	A	30. N.	07 02	23 19	06 48	23 19	06 34	23 20	07 18	23 18
19	B		07 59	23 16	07 45	23 16	07 32	23 17	08 15	23 15
20	C		08 56	23 12	08 43	23 13	08 29	23 14	09 12	23 11
21	D		09 54	23 08	09 40	23 09	09 26	23 10	10 09	23 07
22	E		10 51	23 03	10 37	23 04	10 23	23 06	11 06	23 02
23	F		11 48	22 58	11 34	23 00	11 20	23 01	12 04	22 57
24	G	*John Bap.*	12 45	22 53	12 31	22 54	12 17	22 56	13 01	22 52
25	A		13 42	22 48	13 28	22 49	13 15	22 50	13 58	22 46
26	B		14 39	22 41	14 26	22 43	14 12	22 44	14 55	22 40
27	C		15 37	22 35	15 23	22 37	15 09	22 38	15 52	22 33
28	D		16 34	22 28	16 20	22 30	16 06	22 32	16 49	22 26
29	E	(27. 17. N.	17 31	22 21	17 17	22 23	17 03	22 25	17 47	22 19
30	F	Swans Bil	18 28	22 13	18 14	22 15	18 00	22 17	18 44	22 11

Month days.	Week days.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669. | 1673. ☉ pla.		☉ dec.		Second Year, 1670. | 1674. ☉ pla.		☉ dec.		Third Year, 1671. | 1675. ☉ pla.		☉ dec.		Leap Year, 1672. | 1676. ☉ pla.		☉ dec.	
			D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
			♑		North.		♑		North.		♑		North.		♑		North.	
01	G		19	25	22	05	19	11	22	07	18	58	22	09	19	41	22	03
02	A		20	22	21	57	20	09	21	59	19	55	22	01	20	38	21	55
03	B	(35.27.S.	21	20	21	48	21	06	21	50	20	52	21	53	21	35	21	46
04	C	Sagit.thig.	22	17	21	39	22	03	21	41	21	49	21	44	22	33	21	37
05	D	and Vult. heart, 8.2.	23	14	21	30	23	00	21	32	22	46	21	34	23	30	21	27
06	E	N.	24	11	21	20	23	58	21	22	23	44	21	25	24	27	21	17
07	F		25	09	21	10	24	55	21	12	24	41	21	15	25	24	21	07
08	G		26	06	20	59	25	52	21	02	25	38	21	04	26	22	20	56
09	A		27	03	20	48	26	49	20	51	26	35	20	53	27	19	20	45
10	B		28	00	20	37	27	47	20	40	27	33	20	42	28	16	20	34
11	C		28	58	20	25	28	44	20	28	28	30	20	31	29	13	20	22
12	D		29	55	20	13	29	41	20	16	29	27	20	19	♌	11	20	10
13	E	☉ in ♌.	♌	52	20	01	♌	38	20	04	♌	25	20	07	01	08	19	57
14	F		01	50	19	48	01	36	19	51	01	22	19	54	02	05	19	45
15	G		02	47	19	35	02	33	19	38	02	19	19	42	03	03	19	32
16	A		03	44	19	22	03	30	19	25	03	17	19	28	04	00	19	18
17	B	Swans tail	04	42	19	08	04	28	19	12	04	14	19	15	04	57	19	04
18	C	44. 06. N.	05	39	18	54	05	25	18	58	05	11	19	01	05	55	18	50
19	D	Dog dayes	06	36	18	40	06	23	18	44	06	09	18	47	06	52	18	36
20	E	begin.	07	34	18	25	07	20	18	29	07	06	18	33	07	50	18	21
21	F		08	31	18	11	08	17	18	14	08	04	18	18	08	47	18	07
22	G		09	29	17	56	09	15	17	59	09	01	18	03	09	44	17	51
23	A		10	26	17	40	10	12	17	44	09	58	17	48	10	42	17	36
24	B		11	24	17	24	11	10	17	28	10	56	17	32	11	39	17	20
25	C	*James Ap*	12	21	17	08	12	07	17	12	11	53	17	16	12	37	17	04
26	D		13	20	16	52	13	05	16	55	12	51	17	00	13	34	16	47
27	E		14	16	16	35	14	02	16	39	13	48	16	43	14	32	16	31
28	F		15	14	16	19	15	00	16	23	14	46	16	27	15	30	16	14
29	G		16	11	16	01	15	57	16	06	15	44	16	10	16	27	15	57
30	A		17	09	15	44	16	55	15	48	16	41	15	53	17	25	15	39
31	B		18	07	15	27	17	53	15	31	17	39	15	35	18	22	15	22

August hath XXXI dayes.

Month dayes.	Week dayes.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669.		1673.		Second Year, 1670.		1674.		Third Year, 1671.		1675.		Leap Year, 1672.		1676.	
			☉ pla.		☉ dec.		☉ pla.		☉ dec.		☉ pla.		☉ dec.		☉ pla.		☉ dec.	
			D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
			♌		North.		♌		North.		♌		North.		♌		North.	
01	C	(8.24 N.	19	04	15	09	18	50	15	13	18	36	15	17	19	20	15	04
02	D	Peg Mouth	20	02	14	50	19	48	14	55	19	34	14	59	20	18	14	45
03	E	2 bright *	21	00	14	32	20	46	14	37	20	32	14	41	21	15	14	27
04	F	Capr. tail,	21	57	14	13	21	43	14	18	21	29	14	23	22	13	14	08
05	G	18. 2. S.	22	55	13	55	22	41	13	59	22	27	14	04	23	11	13	49
06	A		23	53	13	36	23	39	13	40	23	25	13	45	24	09	13	30
07	B		24	51	13	16	24	37	13	21	24	23	13	26	25	06	13	11
08	C		25	48	12	57	25	34	13	02	25	20	13	06	26	04	12	52
09	D		26	46	12	37	26	32	12	42	26	18	12	47	27	02	12	32
10	E		27	44	12	17	27	30	12	22	27	16	12	27	28	00	12	12
11	F		28	42	11	57	28	28	12	02	28	14	12	07	28	58	11	52
12	G		29	40	11	37	29	26	11	42	29	12	11	47	29	56	11	31
13	A		♍	38	11	17	♍	24	11	22	♍	10	11	27	♍	54	11	11
14	B		01	36	10	56	01	22	11	01	01	08	11	06	01	52	10	50
15	C		02	34	10	35	02	20	10	40	02	06	10	45	02	50	10	29
16	D		03	32	10	14	03	18	10	19	03	04	10	24	03	48	10	08
17	E		04	30	09	53	04	16	09	58	04	02	10	03	04	46	09	47
18	F		05	28	09	32	05	14	09	37	05	00	09	42	05	44	09	26
19	G		06	26	09	10	06	12	09	16	05	58	09	21	06	42	09	04
20	A		07	24	08	49	07	10	08	54	06	56	08	59	07	40	08	43
21	B	(31.20.S	08	23	08	27	08	08	08	32	07	54	08	38	08	38	08	21
22	C	Fomahant	09	21	08	05	09	07	08	10	08	53	08	16	09	37	07	59
23	D	Peg. shold	10	19	07	43	10	05	07	48	09	51	07	54	10	35	07	37
24	E	26.15.N.	11	17	07	21	11	03	07	26	10	49	07	32	11	33	07	15
		Barthol.																
25	F		12	15	06	59	12	01	07	04	11	47	07	10	12	31	06	53
26	G		13	14	06	36	13	00	06	42	12	46	06	47	13	30	06	30
27	A		14	12	06	14	13	58	06	19	13	44	06	25	14	28	06	08
28	B	Dog dayes	15	11	05	51	14	56	05	57	14	42	06	02	15	26	05	45
		end.																
29	C		16	09	05	29	15	55	05	34	15	41	05	40	16	25	05	23
30	D		17	07	05	06	16	53	05	11	16	39	05	17	17	23	05	00
31	E		18	06	04	43	17	52	04	49	17	38	04	54	18	22	04	37

Month days	Week days	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669. ☉ pla.	First Year, 1673. ☉ dec.	Second Year, 1670. ☉ pla.	Second Year, 1674 ☉ dec.	Third Year, 1671. ☉ pla.	Third Year, 1675. ☉ dec.	Leap Year, 1672. ☉ pla.	Leap Year, 1676. ☉ dec.
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			♍	North.	♍	North.	♍	North.	♍	North.
01	F	(by fire, 66	19 04	04 20	18 50	04 26	18 36	04 31	19 20	04 14
02	G	L. deHeyd	20 03	03 57	19 49	04 03	19 35	04 08	20 19	03 51
03	A	*Oli Crom*	21 02	03 34	20 47	03 40	20 33	03 45	21 18	03 28
04	B	died, 1658	22 00	03 11	21 46	03 16	21 32	03 22	22 16	03 04
05	C		22 59	02 48	22 45	02 53	22 30	02 59	23 15	02 41
06	D		23 57	02 24	23 43	02 30	23 29	02 36	24 13	02 18
07	E	*Nat. Eliz.*	24 56	02 01	24 42	02 07	24 28	02 12	25 12	01 55
08	F	*Nat. Mary*	25 55	01 38	25 41	01 43	25 26	01 49	26 11	01 31
09	G	(27. 14. N	26 54	01 14	26 39	01 20	26 25	01 26	27 10	01 08
10	A	Cap. Ardr	27 53	00 51	27 38	00 57	27 24	01 02	28 09	00 44
11	B	Cas. chair.	28 51	00 27	28 37	00 33	28 23	00 39	29 07	00 21
12	C	57. 18. N.	29 50	00 04	29 36	00 10	29 22	00 15	♎ 06	*So.* 30
13	D	☉ in ♎.	♎ 49	*So.* 20	♎ 35	*So.* 14	♎ 21	*So.* 08	01 05	00 20
14	E		01 48	00 43	01 34	00 37	01 20	00 32	02 04	00 50
15	F		02 47	01 07	02 33	01 01	02 19	00 55	03 03	01 13
16	G		03 46	01 30	03 32	01 24	03 18	01 19	04 02	01 37
17	A		04 45	01 54	04 31	01 48	04 17	01 42	05 01	02 00
18	B		05 44	02 17	05 30	02 11	05 16	02 06	06 00	02 24
19	C		06 43	02 41	06 29	02 35	06 15	02 29	07 00	02 47
20	D	Whal. tail.	07 43	03 04	07 28	02 58	07 14	02 53	07 59	03 10
21	E	19. 15. S.	08 42	03 27	08 27	03 22	08 13	03 16	08 58	03 34
22	F	Pole Star,	09 41	03 51	09 27	03 45	09 12	03 39	09 57	03 57
23	G	87. 30. N.	10 40	04 14	10 26	04 08	10 12	04 03	10 56	04 20
24	A		11 40	04 37	11 25	04 32	11 11	04 26	11 56	04 44
25	B		12 39	05 01	12 25	04 55	12 10	04 49	12 55	05 07
26	C	South in	13 38	05 24	13 24	05 18	13 10	05 13	13 55	05 30
27	D	Ardrom	14 38	05 47	14 23	05 41	14 09	05 36	14 54	05 53
28	E	girdle, 33	15 37	06 10	15 23	06 04	15 08	05 59	15 53	06 16
29	F	62. N.	16 37	06 33	16 22	06 27	16 08	06 22	16 53	06 39
30	G	*Mich Arck*	17 36	06 56	17 22	06 50	17 07	06 45	17 52	07 02

Month days.	Week days.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669. / 1673. ☉ pla. D. M.	☉ dec. D. M.	Second Year 1670. / 1674. ☉ pla. D. M.	☉ dec. D. M.	Third Year, 1671. / 1675. ☉ pla. D. M.	☉ dec. D. M.	Leap Year, 1672. / 1676. ☉ pla. D. M.	☉ dec. D. M.
			♎	South.	♎	South.	♎	South.	♎	South.
01	A		18 36	07 18	18 21	07 13	18 07	07 07	18 52	07 25
02	B		19 35	07 41	19 21	07 35	19 06	07 30	19 52	07 47
03	C	Edge Hill	20 35	08 03	20 21	07 58	20 06	07 53	20 51	08 10
04	D	Battel, 1642.	21 35	08 26	21 20	08 21	21 06	08 15	21 51	08 32
05	E		22 34	08 48	22 20	08 43	22 05	08 37	22 51	08 54
06	F		23 34	09 10	23 20	09 05	23 05	09 00	23 50	09 16
07	G		24 34	09 32	24 19	09 27	24 05	09 22	24 50	09 38
08	A	(19.09. N.	25 34	09 54	25 19	09 49	25 05	09 44	25 50	10 00
09	B	17. 38. N.	26 33	10 16	26 19	10 11	26 04	10 06	26 50	10 22
10	C	N. & S. in	27 33	10 38	27 19	10 33	27 04	10 27	27 50	10 44
11	D	the R. horn	28 33	10 59	28 19	10 54	28 04	10 49	28 50	11 05
12	E	(21.51. N.	29 33	11 21	29 19	11 15	29 04	11 10	29 49	11 26
13	F	Ramshead	♏ 33	11 42	♏ 19	11 37	♏ 04	11 31	♏ 49	11 47
14	G	☉ in ♏.	01 33	12 03	01 19	11 58	01 04	11 52	01 49	12 08
15	A		02 33	12 23	02 19	12 18	02 04	12 13	02 49	12 29
16	B		03 33	12 44	03 19	12 39	03 04	12 34	03 50	12 49
17	C		04 33	13 04	04 19	12 59	04 04	12 54	04 50	13 10
18	D		05 33	13 24	05 19	13 20	05 04	13 15	05 50	13 30
19	E		06 34	13 44	06 19	13 40	06 04	13 35	06 50	13 50
20	F		07 34	14 04	07 19	13 59	07 05	13 55	07 50	14 09
21	G		08 34	14 24	08 19	14 19	08 05	14 14	08 50	14 29
22	A		09 34	14 43	09 20	14 38	09 05	14 33	09 51	14 48
23	B		10 35	15 02	10 20	14 57	10 05	14 53	10 51	15 07
24	C		11 35	15 21	11 20	15 16	11 06	15 12	11 51	15 26
25	D		12 35	15 39	12 21	15 35	12 06	15 30	12 52	15 44
26	E		13 36	15 58	13 21	15 53	13 06	15 49	13 52	16 02
27	F	Whal. jaw	14 36	16 16	14 21	16 11	14 07	16 07	14 52	16 20
28	G	2. 44. N.	15 36	16 33	15 22	16 29	15 07	16 24	15 53	16 38
29	A	*Sim. & Ju*	16 37	16 51	16 22	16 47	16 08	16 42	16 53	16 5[illegible]
30	B	Perse. side.	17 37	17 08	17 23	17 04	17 08	17 00	17 54	17 1[illegible]
31	C	48. 33. N.	18 38	17 25	18 23	17 21	18 09	17 17	18 54	17 2[illegible]

November hath XXX dayes.

Month days.	Week days.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669. ☉ pla.		1673. ☉ dec.		Second Year, 1670. ☉ pla.		1674 ☉ dec.		Third Year, 1671. ☽ pla.		1675. ☉ dec.		Leap Year, 1672. ☽ pla.		1676. ☉ dec.	
			D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.	D.	M.
				m	South.			m	South.			m	South.			m	South.	
01	D		19	38	17	42	19	24	17	37	19	09	17	33	19	55	17	46
02	E	Long Parl.	20	39	17	58	20	24	17	54	20	10	17	50	20	56	18	02
03	F	began,	21	40	18	14	21	25	18	10	21	10	18	06	21	56	18	18
04	G	1640.	22	40	18	29	22	26	18	25	22	11	18	22	22	57	18	33
05	A	*Pow. Plot*	23	41	18	44	23	26	18	41	23	11	18	37	23	57	18	49
06	B		24	42	18	59	24	27	18	56	24	12	18	52	24	58	19	03
07	C	Pers. foot,	25	42	19	14	25	28	19	11	25	13	19	07	25	59	19	18
08	D	50. 52. N.	26	43	19	28	26	28	19	25	26	14	19	21	27	00	19	32
09	E		27	44	19	42	27	29	19	39	27	14	19	36	28	00	19	46
10	F		28	45	19	56	28	30	19	53	28	15	19	49	29	01	19	59
11	G		29	45	20	09	29	31	20	06	29	16	20	03	♐	02	20	13
12	A	☉ in ♐.	♐	46	20	22	♐	31	20	19	♐	16	20	16	01	03	20	25
13	B		01	47	20	34	01	32	20	31	01	18	20	28	02	04	20	38
14	C		02	48	20	46	02	33	20	43	02	18	20	40	03	04	20	50
15	D		03	49	20	58	03	34	20	55	03	19	20	52	04	05	21	01
16	E		04	50	21	09	04	35	21	07	04	20	21	04	05	06	21	12
17	F		05	51	21	20	05	36	21	18	05	21	21	15	06	07	21	23
18	G	Bulls eye,	06	52	21	31	06	37	21	28	06	22	21	26	07	08	21	33
19	A	15. 47. N.	07	53	21	41	07	38	21	38	07	23	21	36	08	09	21	43
20	B		08	54	21	50	08	39	21	48	08	24	21	46	09	10	21	53
21	C		09	55	22	00	09	40	21	57	09	25	21	55	10	11	22	02
22	D		10	56	22	08	10	41	22	06	10	26	22	04	11	12	22	11
23	E		11	57	22	17	11	42	22	15	11	27	22	13	12	13	22	19
24	F		12	58	22	25	12	43	22	23	12	28	22	21	13	14	22	27
25	G	The Goat,	13	59	22	32	13	44	22	30	13	29	22	29	14	15	22	34
26	A	45. 37. N.	15	00	22	39	14	45	22	38	14	30	22	36	15	16	22	41
27	B	Orio. foot,	16	01	22	46	15	46	22	44	15	31	22	43	16	18	22	48
28	C	8. 33. S.	17	02	22	52	16	47	22	51	16	32	22	49	17	19	22	54
29	D	Or. l shol.	18	03	22	58	17	48	22	56	17	33	22	55	18	20	22	59
30	E	6. 0. N.	19	04	23	03	18	49	23	02	18	35	23	00	19	21	23	04

Month dayes.	Week dayes.	Remarkable dayes, & southing of Stars at Midnight.	First Year, 1669 ⊙ pla.	First Year, 1673 ⊙ dec	Second Year, 1670. ⊙ pla.	Second Year, 1674. ⊙ dec.	Third Year. 1671. ⊙ pla.	Third Year. 1675. ⊙ dec.	Leap Year, 1672. ⊙ pla.	Leap Year, 1676. ⊙ dec
			D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.	D. M.
			♈	South.	♈	South.	♈	South.	♈	South.
01	F	1st In Orions gird.	20 05	23 08	19 51	23 07	19 36	23 05	20 22	23 09
02	G	00.35.S.	21 07	23 12	20 52	23 11	20 37	23 10	21 23	23 13
03	A		22 08	23 16	21 53	23 15	21 38	23 14	22 24	23 17
04	B	(44.52.N.	23 09	23 29	22 54	23 19	22 39	23 18	23 26	23 21
05	C	Wag. shol.	24 10	23 22	23 55	23 22	23 40	23 21	24 27	23 25
06	D	Orion. rig.	25 11	23 25	24 56	23 24	24 42	23 24	25 28	23 29
07	E	sholder,	26 13	23 27	25 58	23 26	25 43	23 26	26 29	23 27
08	F	7.58.N.	27 14	23 28	26 59	23 28	26 44	23 28	27 30	23 29
09	G		28 15	23 29	28 00	23 29	27 45	23 29	28 32	23 29
10	A		29 16	23 30	29 01	23 30	28 46	23 30	29 33	23 30
11	B	⊙ in ♈.	♈ 17	23 30	♈ 03	23 30	29 48	23 30	♈ 34	23 30
12	C		01 19	23 30	01 04	23 30	♈ 49	23 30	01 35	23 29
13	D		02 20	23 29	02 05	23 29	01 50	23 29	02 36	23 28
14	E	Polluxfoot	03 21	23 28	03 06	23 28	02 51	23 28	03 38	23 27
15	F	16.39.N.	04 22	23 26	04 07	23 26	03 53	23 27	04 39	23 25
16	G		05 24	23 23	05 09	23 24	04 54	23 25	05 40	23 23
17	A		06 25	23 21	06 10	23 21	05 55	23 22	06 41	23 20
18	B		07 26	23 17	07 11	23 18	06 56	23 19	07 43	23 16
19	C		08 27	23 14	08 12	23 15	07 58	23 16	08 44	23 13
20	D		09 29	23 10	09 14	23 11	08 59	23 12	09 45	23 08
21	E	*Thomas.*	10 30	23 05	10 15	23 06	10 00	23 07	10 46	23 04
22	F		11 31	23 00	11 16	23 01	11 01	23 02	11 48	22 58
23	G		12 32	22 54	12 17	22 56	12 03	22 57	12 49	22 53
24	A		13 33	22 48	13 19	22 50	13 04	22 51	13 50	22 47
25	B	*Na. Christ*	14 35	22 42	14 20	22 44	14 05	22 45	14 51	22 40
26	C	*Stephen.*	15 36	22 35	15 21	22 37	15 06	22 39	15 53	22 33
27	D	*Jo. Evang*	16 37	22 28	16 22	22 30	16 07	22 31	16 54	22 26
28	E	*Innocents.*	17 38	22 20	17 23	22 22	17 09	22 24	17 55	22 18
29	F		18 40	22 12	18 25	22 14	18 10	22 16	18 56	22 09
30	G	Little dog.	19 41	22 03	19 26	22 05	19 11	22 07	19 57	22 01
31	A	6. 5. N.	20 42	21 54	20 27	21 56	20 12	21 59	20 59	21 52

An Explanation of the precedent Kalendar.

In each Page there are eleven Columns; the first sheweth the day the Month; the second, the dayes of the Week, expressed by the Week day Letters; as in the year 1669, in the Month of *May*, you will find B for Saturday, and C for Sunday, which is the Dominical Letter for that Year, (as you see in the Page before the Kalendar). The third Column, sheweth some remarkable Dayes, and the Southing of several Stars at Midnight, with their Declinations from the Equinoctial; as in the aforesaid Month you will find against the third Day, there stands *Lucida Coronæ*, which sheweth, that the said Star comes to the Meridian the third day, at twelve of the Clock at Midnight. The fourth Column, sheweth the place of the Sun for the first Year after Leap-Year, (according to Mr. *Streets* Tables, in the Appendix to *Astro. Car.*) as against the forementioned Day you will find the Sun to be 23*d*. 05*m*. in *Taurus*. The fifth Column, sheweth the Declination of the Sun, for the first Year after Leap-Year, as against the third day aforesaid you will find the Sun's Declination to be 18*d*. 35*m*. And according to the same Rule and Reason, the other six Columns are to be used; as against the said third day of *May* you will find in the sixth Column, in the second Year after Leap-Year, that the Sun's place is 22*d*. 51*m*. in *Taurus*: And in the seventh Column, the Sun's Declination to be 18*d*. 32*m*. And in the eighth Column, and in the third Year after Leap-Year, the Sun's place 22*d*. 37*m*. in *Taurus*; and in the ninth Column, the Declination of the Sun is 18*d* 28*m* And in the tenth Column, in the Leap Year, the Suns place is 23*d*. 20*m*. in *Taurus*: and in the eleventh Column, the Sun's Declination is 18*d*. 39*m*.

How

How to find the Day of the Month, or Week Day, for any time past or to come, by the precedent Kalendar.

First, You must find the *Dominical Letter* by the *Table* before the *Kalendar*, or else by the *Rule* delivered in *Chap.* 7. *Sect.* 3. and thereby you may discover the Day of the Month; as follows.

Example 1.

What Day of the Month was the first Monday in August in the Year 1645?

By the former *Rule* you will find the *Dominical Letter* was E; then turning to the Month of *August*, call E *Sunday*, and the F that follows is *Monday*, and the first Monday is the 4th day of the Month.

Example 2.

What day of the Week will the tenth of February be in the Year 1680?

This Year will be *Leap-Year*, and in the Table hath two *Dominical Letters*, D and C; the first of them serving from the first of *January* till the 25th of *February*, and the other from thence to the years end: Therefore against the 10th of *February* stands F; then calling D *Sunday*, E is *Monday*, and F is *Tuesday*, the Week Day sought.

Example 3.

What day of the Month is the second Thursday in the Month of August, in the Year 1680?

The *Dominical Letter* for the latter part of the Year is C, therefore C stands for *Sunday*, D for *Monday*, E for *Tuesday*, F for *Wednesday*, G for *Thursday*; and against the *second* G in *August*, is the 12th day of the Month, which was required.

A Table

A Table of the Variation of the Sun's Declination, to be applyed for Years to come, according to the Titles on the right hand; but for years past contrarily.

Years.	4	8	12	16	20	24	28	32	36	40	44	48	52	56	60	
Month days.	′	′	′	′	′	′	′	′	′	′	′	′	′	′	′	
January, 1	00	01	01	01	01	02	02	02	02	03	03	03	04	04	04	North
11	00	01	01	01	02	02	03	03	04	04	04	05	05	05	06	
21	00	01	01	02	02	03	03	04	04	05	05	06	06	07	07	
February, 1	01	01	02	02	03	03	04	05	05	06	06	07	08	08	09	
11	01	01	02	03	03	04	05	05	06	06	07	08	08	09	10	
12	01	01	02	03	03	04	05	05	06	07	08	08	09	10	10	
March, 1	01	01	02	03	04	04	05	06	06	07	08	08	09	10	11	
11	01	01	02	03	04	04	05	06	06	07	08	09	09	10	11	
21	01	01	02	03	04	04	05	06	06	07	08	08	09	10	11	
April, 1	01	01	02	03	03	04	05	05	06	07	07	08	09	10	10	
11	01	01	02	03	03	04	04	05	06	06	07	08	08	09	10	
21	01	01	02	02	03	03	04	05	05	06	06	07	07	08	08	
May, 1	00	01	01	02	02	03	03	04	04	05	05	06	06	07	07	
11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	06	
21	00	01	01	01	01	02	02	02	02	03	03	03	03	04	04	
June, 1	00	00	00	01	01	01	01	01	01	01	01	02	02	02	02	South.
11	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	
21	00	00	00	01	01	01	01	01	01	01	01	02	02	02	02	
July, 1	00	01	01	01	01	02	02	02	02	03	03	03	03	04	04	
11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	06	
21	00	01	01	02	02	03	03	04	04	05	05	06	06	07	07	
August, 1	01	01	02	02	03	03	04	05	05	06	06	07	07	08	09	
11	01	01	02	03	03	04	04	05	06	06	07	08	08	09	10	
21	01	01	02	03	03	04	05	05	06	07	08	08	09	10	10	
September, 1	01	01	02	03	04	04	05	06	06	07	08	09	09	10	11	
11	01	01	02	03	04	04	05	06	06	07	08	09	09	10	11	
21	01	01	02	03	04	04	05	06	06	07	08	09	09	10	11	
October, 1	01	01	02	03	03	04	05	05	06	07	08	08	09	10	10	
11	01	01	02	03	03	04	04	05	06	06	07	08	08	09	10	
21	01	01	02	02	03	03	04	05	05	06	06	07	07	08	09	
November, 1	00	01	01	02	02	03	03	04	04	05	05	06	06	07	07	
11	00	01	01	02	02	02	03	03	03	04	04	05	05	05	06	
21	00	01	01	01	01	02	02	02	02	03	03	03	03	04	04	
December, 1	00	00	00	01	01	01	01	01	01	01	01	02	02	02	02	02	
11	00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	North.
21	00	00	00	01	01	01	01	01	01	01	01	02	02	02	02	02

A Table of Variation of the Sun's Declination in Hours.

Hours from the Meridian of London.

Diurnal variat.	1	2	3	4	5	6	7	8	9	10	11	12
Minutes	m	m	m	m	m	m	m	m	m	m	m	m
2	0	0	0	0	0	0	1	1	1	01	01	01
3	0	0	0	0	1	1	1	1	1	01	01	01
4	0	0	0	1	1	1	1	1	1	02	02	02
5	0	0	1	1	1	1	1	2	2	02	02	02
6	0	0	1	1	1	1	2	2	2	02	03	03
7	0	1	1	1	1	2	2	1	3	03	03	03
8	0	1	1	1	2	2	2	3	3	03	04	04
9	0	1	1	1	2	2	3	3	3	04	04	04
10	0	1	1	2	2	2	3	3	4	04	05	05
11	0	1	1	2	2	3	3	4	4	05	05	05
12	0	1	1	2	2	3	3	4	4	05	05	06
13	1	1	2	2	3	3	4	4	5	05	06	06
14	1	1	2	2	3	3	4	5	5	06	06	07
15	1	1	2	2	3	4	4	5	6	06	07	07
16	1	1	2	3	3	4	5	5	6	07	07	08
17	1	1	2	3	4	4	5	6	6	07	08	08
18	1	1	2	3	4	4	5	6	7	07	08	09
19	1	2	2	3	4	5	6	6	7	08	09	09
20	2	2	2	3	4	5	6	6	7	08	09	10
21	1	2	3	3	4	5	6	7	8	09	10	10
22	1	2	3	4	5	5	6	7	8	09	10	11
23	1	2	3	4	5	6	7	8	9	10	11	11
24	1	2	3	4	5	6	7	8	9	10	11	12

Expla-

Examples of the Uſe of the foregoing Tables. *For the Sun's Declination for Years to come*, &c.

Example 1.

Anno 1695, *May* the firſt, The declination of the Sun is required.

Firſt, From the year 1695, I deduct all the hundreds and ſcores, that is 1680; and the reſidue 15, I divide by 4; the laſt remainer 3, ſhews it is *the third after Leap Year*. Therefore,

Secondly, In the Kalendar for four years, I look for the *third after Leap Year*, and do find it anſwer to 1671. In which year, on the firſt day of *May*, the *Declination* of the Sun is 17° 58′ North.

Thirdly, Then out of 1695, I ſubſtract 1671, and with the reſidue 24, I enter the *Table of the Variation of the Sun's Declination for years*, &c. where under 24 years, in the head of the Table, and againſt *May* the firſt, on the left hand I find the *Variation* 3′ North. But the aforefound *Declination* was alſo North, therefore to the ſaid *Declination* 17° 58′, I add the *Variation* 3′, and the ſum is 18° 1′ North, the true *Declination* of the Sun, *Anno* 1695, *May* the firſt, in the *Meridian of London*, as was required.

Example 2.

Anno 1728, *September* the firſt, I would know the *Suns Declination*; And from 1728, rejecting the *hundreds and ſcores*, I divide the reſidue which is 8 by 4, the remainer 0, ſhews it is *Leap Year*, under which Title I find 1672, in which, on the firſt day of *September*, the *Declination* of the Sun is 4° 14′ North.

Then from 1728, I ſubſtract 1672, reſts 56 years; under which, and againſt *September*, 1. (in the *Table of Variation in years*) I find the *Variation* 10′ South; which ſubſtracted from the aforefound *Declination* 4° 14′ North, reſts 4° 4′ North, the true *Declination* of the Sun.

And here note, that when the *Declination* and *Variation* are both North, or both South, their ſum is the true *Declination*; but if the one be North, and the other South, it's their difference.

For

For the Declination of the Sun, when he is out of the Meridian of London.

Anno 1672. *April* the 11th day, at 6 of the Clock afternoon, I would know the Sun's Declination?

The 11th day at Noon, I find it in the Kalendar 12*d*.14*m*. North, and the 12th day 12*d*. 34*m*. therefore ſubſtracting the leſſer Declination 12*d*. 14*m*. out of the greater 12*d*. 34*m*. the reſidue 20*m*. is the daily increaſe.

Then in the *Table of Variation in Hours, &c.* under 6 hours in the head, and againſt 20*m*. on the left hand, I find 5*m*. the proportional part, which (becauſe the Hour was Afternoon, and the Declination increaſing) added to the aforefound 12*d*. 14*m*. the ſum is 12*d*. 19*m*. North, the Declination required.

Example 2.

For the Declination of the Sun, *Anno* 1672. *October* the 28th day, at 8 in the morning, that is 4 hours reckoned backward from Noon.

In the Kalendar, the Declination on the 28*th* day of *Octob.* that year is 16*d*.38*m*. and on the 27*th* day 16*d*.20*m*. South; the difference is 18*m*. againſt which, and under 4 hours, in the Table of *Variation in Hours*, &c. I find the proportional part 3*m*. which (in this Example) ſubſtracted from 16*d*.38*m*. there remaineth 16*d*. 35*m*. South, the Declination ſought.

And thus may the true Declination of the Sun be eaſily found at all times, and in all *Meridians*, of which, I ſuppoſe, here will need no more Examples.

The Suns Horizontal Parallax is only 15 ſeconds, therefore the Parallax need not be applyed at all.

Alſo the Suns refraction is demonſtratively equal to that of the fixt Stars, which latter is by the obſervation of *Tycho Brache* in the Horizon 30 minuits, and in the 20 deg. of Alt. Vide *Chap. Sect.* 1.

A Table of Difference of Latitude and Departure.

Distant.	¼ Point.		½ Point.		¾ Point.		1 Point.		1 ¼ Point		1 ½ Point		Distant.
	Lat.	De	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
1	.99	.05	.99	.10	.99	.15	.98	.20	.97	.24	.96	.29	1
2	1.99	.10	1.99	.20	1.98	.29	1.96	.39	1.94	.49	1.91	.58	2
3	2.99	.15	2.99	.29	2.97	.44	2.94	.59	2.91	.73	2.87	.87	3
4	3.99	.20	3.98	.39	3.96	.59	3.92	.78	3.88	.97	3.83	1.16	4
5	4.99	.24	4.98	.49	4.95	.73	4.90	.98	4.85	1.22	4.79	1.46	5
6	5.99	.29	5.97	.59	5.94	.88	5.89	1.17	5.82	1.46	5.74	1.74	6
7	6.99	.34	6.97	.69	6.92	1.03	6.87	1.37	6.79	1.70	6.70	2 03	7
8	7.99	.39	7.96	.78	7.91	1.17	7.85	1.56	7.76	1.94	7 66	2.32	8
9	8.99	.44	8.96	.88	8.90	1.32	8.83	1.76	8.73	2.19	8.62	2.61	9
10	9.99	.49	9.95	.98	9.89	1.47	9.81	1.95	9.70	2 43	9.57	2.90	10
11	10.98	.54	10.94	1.08	10.83	1.62	10.79	2.15	10.67	2.67	10.53	3.19	11
12	11.98	.59	11.94	1.18	11.87	1.76	11.77	2.34	11.64	2.92	11.48	3.48	12
13	12.98	.64	12.94	1.27	12.86	1.91	12.75	2.54	21.61	3 16	12.44	3.77	13
14	13.98	.69	13.93	1.37	13.85	2.06	13.73	2.73	31.58	3.40	13.40	4.06	14
15	14.98	.73	14.93	1.47	14.84	2.20	14.71	2.93	41.55	3.65	14.36	4.36	15
16	15.98	.78	15.92	1.57	15.83	2.35	15.70	3.12	15.52	3.89	15.31	4.64	16
17	16.98	.83	16.92	1.67	16.81	2.50	16.68	3.32	16.49	4.13	16 27	4.93	17
18	17.98	.88	17.91	1.76	17.80	2.64	17.66	3.57	17.46	4.37	17 23	5.22	18
19	18.98	.93	18.91	1.86	18.79	2.79	18.64	3.71	18.43	4.62	18.19	5.51	19
20	19.98	.98	19.92	1.96	19.78	2.93	19.62	3.90	19.40	4.86	19.14	5.81	20
21	20.97	1.03	20.89	2.06	20.77	3.08	20.60	4.10	20.37	5.10	20.10	6 10	21
22	21.97	1.08	21.89	2.16	21.76	3.22	21.58	4.29	21.34	5.35	21.05	6.39	22
23	22.97	1.13	22.89	2.25	22.75	3.37	22.56	4.49	22.31	5.59	22.01	6.68	23
24	23.97	1.18	23.88	2.35	23.74	3.52	23.54	4.68	23.28	5.83	22.97	6.79	24
25	24.97	1.22	24.88	2.45	24.73	3 66	24.52	4.88	24.25	6.08	23.93	7.27	25
26	25.97	1.27	25.87	2.55	25.72	3.81	25.51	5.07	25.22	6.32	24.80	7.55	26
27	26.97	1.32	26.87	2.65	26.70	3.96	26.49	5.27	26.19	6.56	25.84	7.84	27
28	27.97	1.37	27.86	2.74	27.69	4.10	27.47	5.46	27.16	6.80	26.80	8.13	28
29	28.97	1.42	28.86	2.84	28.68	4.25	28.45	5.66	28.13	7 05	27.76	8.42	29
30	29.96	1.47	29.85	2.94	29.67	4.40	29.42	5.85	29.10	7.23	28.71	8.71	30
31	30.95	1.52	30.84	3.04	30.66	4.55	30.40	6.05	30.07	7.53	29.67	9.00	31
32	31.95	1.57	31.84	3.14	31.65	4.69	31.38	6.24	31.04	7.78	30.62	9.29	32
33	32.95	1.62	32.84	3.23	32.64	4.84	32.36	6.44	32.01	8.02	31.58	9.58	33
34	33.95	1.67	33.83	3.33	33.63	4.99	33.34	6.63	32.98	8.26	32.54	9.87	34
35	34.95	1.71	34.83	3.43	34.62	5.13	34.32	6.83	33.95	8.51	33.50	10.17	35
36	35.95	1.76	35.82	3.53	35.61	5.28	35.31	7.02	34.92	8.75	34.45	10.45	36
37	36.95	1.81	36.82	3.63	36.59	5.43	36.29	7.22	35.89	8.99	35.41	10.74	37
38	37.95	1.86	37.81	3.72	37.58	5.57	37.27	7.41	36.86	9.23	36.37	11.03	38
39	38.95	1.91	38 81	3.82	38.57	5.72	38.25	7.61	37.83	9.48	37.33	11.33	39
40	39.95	1.96	39.81	3.92	39.57	5.87	39.23	7.80	38.80	9.72	38 28	11.61	40
41	40.94	2.01	40.80	4.02	40.56	6.02	40.21	8.00	39.77	9.96	39.24	11.90	41
42	41.94	2.06	41.80	4.12	41.55	6.16	41.19	8.19	40.74	10.21	40.19	12.19	42
43	42.94	2.11	42.80	4.21	42.54	6.31	42.17	8.39	41.71	10.45	41.15	12.48	43
44	43.94	2.16	43.79	4.31	43.53	6.46	43.15	8.58	42.68	10 69	42.11	12.77	44
45	44.94	2.20	44.79	4.41	44.52	6.60	44.13	8.78	43.65	10.94	43.07	13.07	45
46	45.94	2.25	45.78	4.51	45.51	6.75	45.12	8.97	44.62	11.18	44.02	13 35	46
47	46.94	2.30	46.78	4.61	46.49	6.90	46.10	9.17	45.55	11.42	44.98	13.64	47
48	47.94	2.35	47.77	4.70	47.48	7.04	47.08	9.36	46.55	11.66	45.94	13 9	48
49	48.94	2.40	48.77	4.80	48.47	7.19	48.06	9.56	47.53	11.91	46 90	14.22	49
50	49.94	2.45	49.76	4.90	49.46	7.34	49 04	9.76	48.50	12.15	47 85	14.51	50
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat	
	7 ½ point.		7 ½ poin.		7 ¼ poin.		7 points.		6 ½ poin.		6 ½ point		

Distant	¼ Point.		½ Point.		¾ Point.		1 Point.		1 ¼ Point		1 ½ Point		Distant.
	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
51	50·93	2·50	50·75	5·00	50·45	7·49	50·02	9·96	49·47	12·39	48·81	14·80	51
52	51·93	2·55	51·75	5·10	51·44	7 63	51·02	10·15	50·44	12·64	49·74	15·09	52
53	52·93	2·60	52 75	5·19	52·43	7·78	51·98	10·35	51·41	12·88	50 72	15·38	53
54	53·93	2·65	53·74	5·29	53·42	7·93	52·95	10·55	52·38	13·12	51·68	15·67	54
55	54·93	2·69	54·74	5·39	54·41	8·07	53·9	10·74	53·35	13·37	52·64	15·97	55
56	55·93	2·74	55·73	5·49	55·40	8·22	54·9	10·94	54 32	13·61	53·59	16·25	56
57	56·93	2·79	56·73	5·59	56·38	8.37	55·91	11·13	55·29	13·85	54·55	16 54	57
58	57·93	2·84	57 72	5·68	57·37	8·51	56·98	11·33	56·26	14·09	55·51	16·83	58
59	58·93	2·89	58·72	5·78	58·36	8·66	57·87	11·52	57·23	14·34	56·47	17·12	59
60	59·93	2·94	59·71	5·88	59·35	8·80	58·85	11·71	58·20	14·58	57·42	17·42	60
61	60·92	2 99	60·70	5 98	60.34	8·95	59·83	11 91	59·17	14·82	58·38	17·71	61
62	61·92	3·04	61.70	6·08	61·33	9.09	60·81	12.10	60·14	15·07	59·33	18·00	62
63	62·92	3 09	62·70	6·17	62·32	9·24	61·79	12·30	61·11	15·31	60·29	18·29	63
64	63·92	3·14	63·69	6·27	63 31	9·39	62·77	12·49	62·08	15·55	61·25	18·58	64
65	64·92	3·18	64 69	6·37	64·30	9·53	63·75	12.69	63·05	15·80	62·21	18 88	65
66	65·92	3·23	65·68	6·47	65229	9.68	64·74	12·88	64·02	16 04	63 16	19 16	66
67	66·92	3·28	66·68	6·57	66.27	9·83	65·72	13 08	64·99	16 28	64·12	19 45	67
68	67·92	3·33	67.67	6.66	67·26	9 97	66·70	13·27	65·96	16·52	65 08	19·74	68
69	68·92	3·38	68.67	6·76	68.25	10·12	67 68	13·47	66 93	16·77	66·04	20 03	69
70	69·92	3.43	69.66	6·86	69.24	10·27	68.66	13 66	67·90	17·01	66·98	20·32	70
71	70·91	3·48	70.65	6·96	70·23	10·42	69·64	13·86	68.87	17·25	67·94	20·61	71
72	71·91	3·53	71·65	7·06	71·22	10·56	70·62	14·05	69 84	17·50	68·89	20·90	72
73	72 91	3·58	72·65	7·15	72·21	10·71	71·60	14·25	70·81	17 74	69 85	21·19	73
74	73·91	3·63	73 6·	7·25	73·20	10·86	72·58	14·35	71·78	17·98	70·81	21·48	74
75	74·91	3·67	74·64	7·35	74·19	11·00	73·56	14·64	72·75	18·23	71·77	21·78	75
76	75·91	3·72	75·63	7·45	75·18	11·15	74·55	14·84	73·72	18·47	72·72	22·06	76
77	76·91	3·77	76.63	7·55	76·16	11·30	75·53	15·03	74·69	18·71	73·68	22·35	77
78	77 91	3·82	77·62	7·64	77·15	11·44	76·51	15·23	75·66	18·95	74·64	22.64	78
79	78·91	3·87	78.62	7·74	78.14	11·59	77·49	15·42	76·63	19·20	75·60	22·93	79
80	79·90	3·92	79·61	7·84	79 13	11·74	78·46	15·61	77·60	19·44	76·56	23·22	80
81	80·89	3·97	80·60	7·94	80 12	11·89	79·44	15·81	78·57	19·68	77·52	23·51	81
82	81·89	4·02	81·60	8·04	81·11	12·03	80·42	16·00	79·54	19 93	78·47	23·80	82
83	82·89	4·07	82·60	8·13	82·10	12·18	81·40	16·20	80·51	20·27	79·43	24·09	83
84	83·89	4·12	83·59	8·23	83·09	12·33	82·38	16·39	81·48	20 41	80·39	24·38	84
85	84·89	4.16	84·59	8·33	84·08	12·47	83·36	16·59	82·45	20.66	81·35	24·68	85
86	85·89	4·21	85·58	8·43	85·07	12 62	84·35	16·78	83·42	20·90	82·30	24·96	86
87	86.89	4·26	86·58	8·53	86·05	12·77	85·33	16·98	84·39	21·14	83·26	25·25	87
88	87 89	4·31	87·57	8·62	87·04	12·91	86 31	17·17	85·36	21 38	84·22	25·54	88
89	88·89	4·36	88·57	8·72	88·03	13·06	87·29	17·37	86·33	21·63	85·18	25·83	89
90	89·89	4·42	89·57	8·82	89 03	13 21	88.27	17·56	87·30	21·87	86 13	26·13	90
91	90.88	4·47	90·56	8·92	90·02	13·36	89·25	17·76	88·27	22·11	87·09	26·42	91
92	91·88	4·52	91·56	9·02	91 01	13·50	90·23	17·95	89·24	22·36	88 04	26·71	92
93	92·88	4·57	92·56	9.11	92·00	13·65	91·21	18·15	90·21	22.60	89·00	27·00	93
94	93·88	4 62	93·55	9·21	92·99	13·80	92·19	18·35	91·18	22.84	89 96	27·29	94
95	94 88	4.66	94 55	9·31	93·98	13·94	93·17	18.54	92·15	23·09	90·92	27·59	95
96	95·88	4·71	95·54	9·41	94 97	14·09	94·16	18·74	93·12	23·33	91·87	27 87	96
97	96·88	4·76	96·54	9 51	95·95	14·24	95·14	18·93	94·09	23·57	92·83	28.16	97
98	97·88	4 81	97·53	9·60	96 94	14·38	96·12	19·12	95·06	23·81	93·79	28·45	98
99	98·88	4·86	98·53	9 70	97·93	14·53	97·10	19·32	96 02	24·06	94·75	28·74	99
100	99·88	4·91	99·52	9·80	98·92	14 67	98·08	19·51	97 00	24·30	95·69	29·03	100
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	7 ¼ poin.		7 ½ Poin.		7 ¾ Poin.		7 Points.		6 ¾ poin.		6 ½ poins		

Distant.	1 ½ poin.		2 Point.		2 ½ Point		2 ⅔ Point		2 ¾ poin.		3 Point.		Distant.
	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
1	·94	·34	·92	·38	·90	·43	·88	·47	·86	·51	·83	·56	1
2	1.88	·67	1.85	·77	1.81	·85	1.76	·94	1 72	1 03	1.66	1.11	2
3	2.83	·01	2·77	1.15	2·71	1.28	2.65	1·41	2.57	1·54	2·49	1.67	3
4	3·77	1.35	3·70	1·53	3.62	1.71	3·53	1.89	3·43	2·06	3·33	2,22	4
5	4·71	1.69	4·62	1·91	4·52	2 14	4·41	2 36	4 29	2.57	4·16	2·78	5
6	5.65	2,02	5·54	2·30	5·42	2·57	5·29	2·83	5·15	3·08	4·99	3·33	6
7	6.59	2.36	6·47	2.68	6·33	2·99	6·17	3·30	6·00	3·60	5·82	3·89	7
8	7.53	2.70	7·39	3·06	7·23	3·42	7·06	3·77	6.86	4·11	6·65	4.44	8
9	8.47	3·03	8·32	3·44	8.14	3.85	7.94	4.24	7·72	4.63	7.48	5·00	9
10	9·42	3·37	9·24	3·83	9 04	4.28	8·82	4·71	8.58	5·14	8.31	5 56	10
11	10.36	3.71	10·16	4·21	9·94	4.71	9.70	5·18	9·44	5·65	9·14	6·12	11
12	11.30	4.04	11·09	4·60	10·85	5·14	10·58	5.65	10 30	6·17	9·97	6.67	12
13	12.25	4.38	12·01	4·98	11·75	5·56	11·47	6.12	11·15	6.68	10·8 1	7·23	13
14	13.19	4·72	12·94	5·36	12·66	5·99	12·35	6·62	12·01	7.20	11·64	7 78	14
15	14.13	5·06	13·86	5 74	13·56	6·42	13 23	7·07	12.87	7·71	12·47	8·34	15
16	15.07	5.39	14·78	6·13	14·46	6.65	14.11	7·54	13·73	8·22	13 30	8.89	16
17	16.01	5·73	15·71	6·51	15·37	7·27	14 99	8·01	14·58	8.74	14·13	9·45	17
18	16.95	6.07	16·63	6.89	16·27	7·70	15·88	8·48	15.44	9·25	14·96	10·00	18
19	17.89	6.40	17·56	7·27	17·18	8·13	16·76	8·95	16.30	9 77	15·79	10·56	19
20	18·83	6·74	18·48	7.65	18·08	8·55	17·64	9·43	17·15	10.28	16.63	11·11	20
21	19.77	7.08	19.40	8·03	18·98	8 98	18·52	9·90	18.01	10.79	17·46	11.67	21
22	20.71	7.41	20·33	8.42	19·89	9·41	19·40	10·37	18·87	11.31	18·29	12·22	22
23	21.66	7.75	21·25	8 80	20·79	9·83	20.29	10 84	19·72	11.82	19·12	12·78	23
24	22.60	8·09	22.18	9 18	21·70	10·26	21·17	11·32	20·58	12·34	19·96	13·33	24
25	23·54	8·43	23·10	9·56	22·60	10.69	22·05	11.79	21·44	12 85	20·79	13·86	25
26	24.48	8.76	24·02	9·95	23·50	11·12	22.93	12·26	22·30	13·36	21·62	14 44	26
27	25.42	9.10	24·95	10·33	24·41	11·54	23.81	12 73	23·15	13·88	22·45	15·00	27
28	26.36	9.44	25·87	10·71	25·31	11·97	24·70	13·20	24 01	14·39	23·28	15·55	28
29	27 30	9·77	26.80	11·09	26·22	12·40	25·58	13·67	24·87	14.91	24·11	16·11	29
30	28·25	10·11	27·72	11·48	27·12	12.83	26·46	14·14	25 73	15·42	24 94	16·67	30
31	29.19	10·45	28.64	11.86	28·02	13·26	27·34	14·61	26·59	15·93	25·77	17·23	31
32	30.13	10·78	29·57	12·25	28·93	13·69	28.22	15·08	27·45	16·45	26·60	17 78	32
33	31.08	11·12	30·49	12·63	29·83	14.11	29 11	15·55	28·30	16.96	27·42	18·34	33
34	32.02	11.46	30.42	13·01	30·74	14 54	29.99	16.03	29·16	17·48	28.27	18·89	34
35	32·96	11·80	31·34	13·39	31·64	14·97	30·87	16·50	30·02	17·99	29·10	19·45	35
36	33·90	12·13	33·26	13·78	32·54	15·40	31·75	16 97	30·88	18.50	29 93	20·00	36
37	34·84	12·47	34·19	14.16	33·45	15·82	32·63	17·44	31·73	19·02	30·76	20.56	37
38	35·78	12.81	35·11	14·54	34·35	16·25	33·52	17·91	32·59	19.53	31·59	21 11	38
39	36.72	13·14	36 01	14.92	35·26	16.68	34.40	18·38	33·45	20.05	32·42	21·67	39
40	37·66	13·48	36·95	15·31	36 16	17.10	35·27	18 86	34·31	20.56	33·26	22·22	40
41	38.60	13·82	37.87	15.69	37·05	17·53	36·15	19·33	35 17	21·07	34·09	22·78	41
42	39.54	14·15	38·80	16·08	37·97	17·96	37·03	19·80	36·03	21·59	34·92	23 33	42
43	40.49	14·47	39·72	16.46	38·87	18.38	37 92	20 27	36·88	22.10	35·75	23 89	43
44	41.43	14·83	40.65	16·84	39.78	18·81	38·80	20.75	37·74	22.62	36 59	24·44	44
45	42·37	15·17	41·57	17·22	40.68	19·24	39.68	21·22	38·60	23·13	37·42	25·00	45
46	43.31	15·50	42·49	17·61	41·58	19 67	40·56	21.69	39·46	23·64	38·25	25·56	46
47	44.25	15·84	43·42	17·99	42·49	20 09	41·44	22.16	40·31	24·16	39·08	26.11	47
48	45.19	16·18	44·34	18·37	43 39	20 52	42·33	22.63	41·17	24·67	39·91	26·66	48
49	46.13	16·51	45·26	18·75	44 29	20.95	43·20	23·10	42·03	25·19	40·74	27.22	49
50	47·08	16·85	46·19	19·14	45·20	21·38	44·10	23·57	42·89	25·71	41·57	27·78	50
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	6 ¼ poin.		6 points.		5 ¾ point		5 ⅓ point		5 ¼ Point		5 Point.		

Distant.	1 ½ poin.		2 Points.		2 ¼ Point		2 ½ Point		2 ¾ poin.		3 Point.		Distant.
	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	
51	48·02	17·19	47·11	19·52	46·10	21·81	44·98	24·04	43·75	26·21	42·40	28 34	51
52	48·96	17·52	48·04	19·91	47·01	22·24	45·86	24·51	44 61	26·74	43·23	28·89	52
53	49·91	17·86	48·96	20·29	47·91	22·66	46·75	24·98	45·46	27·25	44·06	29·45	53
54	50·85	18·20	49·89	20·67	48·82	23·09	47·63	25·46	46·32	27·77	44·90	30·00	54
55	51·79	18·54	50·82	21·05	49·72	23·52	48·51	25·93	47 18	28·28	45·73	30·56	55
56	52·73	18·87	51·73	21·44	50·62	23·95	49·39	26·40	48·04	28·70	46·56	31·11	56
57	53·67	19·21	52·68	21 82	51·53	24·37	50·27	26·87	48·89	29·31	47·39	31·67	57
58	54·61	19·55	53·58	22·20	52·43	24·80	51·16	27·34	49·75	29·82	48·22	32·22	58
59	55·55	19·88	54·51	22·57	53 34	25·23	52·04	27·81	50·61	30·34	48·04	32·78	59
60	56·49	20·21	55·43	22·96	54·24	25·65	52·91	28 28	51 46	30·85	49·89	33·33	60
61	57·43	20·55	56·35	23·34	55·14	26·07	53·79	28·75	52·32	31·36	50 72	33·89	61
62	58·37	20·88	57·28	23·73	56·05	26·51	54 67	29·22	53 18	31·88	51·55	34·44	62
63	59·32	21·22	58·20	24·11	56·95	26·93	55·56	29·69	54 03	32 39	52·36	35·00	63
64	60·26	21·56	59·13	24·49	57·86	27·36	56·44	30·17	54·89	32·91	53·22	35·55	64
65	61·20	21·90	60·05	24 87	58·76	27·79	57·32	30·54	55·75	33·42	54·05	36·11	65
66	62 14	22·23	60·97	25·26	59·66	28·22	58·20	31·11	56·61	33·93	54·88	36·66	66
67	63·08	22·57	61·90	25·64	60 57	28·64	59·08	31·58	57·46	34·45	55 71	37·22	67
68	64·02	22·91	62·82	26·02	61·47	29·07	60·97	32·05	58·32	34·96	56·54	37·77	68
69	64·96	23·24	63·75	26·40	62·38	29·50	60·85	32·52	59·18	35·48	57·37	38·33	69
70	65·91	23·58	64 67	26·79	63·28	29·93	61·73	33·00	60·04	35 93	58·20	38·89	70
71	66 85	23·92	65·59	27·17	64·18	30·36	62·61	33·47	60·90	36·50	59·03	39·45	71
72	67 79	24·25	66 52	27·56	65·09	30·79	63·49	33·94	61·76	37·02	59·83	40·00	72
73	68 74	24·59	67·44	27·94	65·99	31·21	64·38	34·41	62·61	37·53	60 69	40·56	73
74	69·68	24·93	68·37	28·32	66·90	31·64	65·26	34·89	63·47	38·05	61·53	41·11	74
75	70·62	25·27	69·29	28·70	67·80	32·07	66·14	35·36	64·33	38·56	62·36	41·67	75
76	71·56	25·60	70·21	29·09	68·70	32·48	67·02	35·83	65·19	39 07	63·19	42·22	76
77	72·50	25·94	71·14	29 47	69·61	32·92	67·90	36·30	66 04	39·59	64 02	42·78	77
78	73·44	26·28	72·06	29·85	70·51	33·35	68·79	36·77	66·90	40·10	64·85	43·33	78
79	74·38	26·61	72·99	30·23	71·42	33·78	69·67	37·24	67·76	40·62	65·67	43·89	79
80	75·32	26·95	73·91	30·62	72·32	34 21	70·55	37·71	68 62	41·13	66·52	44·45	80
81	76·26	27·29	74·83	31·00	73 22	34 64	71·43	38·18	69·48	41·64	67·35	45·00	81
82	77·20	27·62	75·76	31·39	74·13	35·07	72·31	38·65	70·34	42·16	68·18	45·55	82
83	78·15	27 96	76·68	31·77	75·03	35·49	73 20	39·12	71·19	42·67	68 99	46·11	83
84	79 09	28·30	77·61	32·15	75·94	35·92	74·08	39·60	72·05	43·19	69·85	46 66	84
85	80 08	28·64	78 58	32·53	76·84	36·35	74·96	40·07	72·91	43·70	70·68	47·22	85
86	80·97	28·97	79·45	32·92	77 74	36·78	75·84	40·54	73 77	44·21	71·51	47·77	86
87	81·91	29 31	80·38	33·30	78·65	37·20	76·72	41·01	74·63	44·73	72·34	48·33	87
88	82·85	29·65	81·30	33·68	79 55	37 63	77·61	41·48	75·48	45·24	73·17	48·88	88
89	83·79	29·98	82 23	34·06	80·46	38·06	78·49	41·95	76 34	45 76	74·00	49·44	89
90	84·74	30·32	83·15	34·44	81 36	38·48	79·37	42·42	77·20	46·27	74·83	50·00	90
91	85·68	30·66	84·07	34·82	82 26	38·91	80 25	42·89	78·06	46·78	75 66	50·56	91
92	86·62	30 99	85 00	35·21	83 17	39 34	81·13	43·36	78 92	47 30	76 46	51·11	92
93	87·57	31·33	85·92	35·59	84·07	39·76	82 02	43 83	79·77	47·81	77·32	51·67	93
94	88 51	31·67	86 85	35·97	84·98	40·19	82·90	44·31	80·63	48·33	78·16	52·22	94
95	89 45	32·01	87 77	36·35	85 88	40·62	82·78	44·78	81·49	48·84	79·99	52 78	95
96	90 39	32·34	88·69	36·74	86·79	41·05	84 66	45·25	82 35	49·35	79·82	53·33	96
97	91·33	32·68	89·62	37·12	87·69	41·47	85·54	45·72	83·20	49·87	80·65	53·89	97
98	92·27	33·02	90 54	37·50	88·60	41 90	86 43	46·19	84·06	50·38	81·48	54·44	98
99	93·21	33·35	91·47	38·88	89 50	42·33	87·31	46·66	84 92	50·90	82·30	55·00	99
100	94 16	33·69	92·39	38·27	90·40	42·76	88·18	47·14	85·77	51·41	83 15	55·56	100
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	6 ¼ Point.		6 Point.		5 ¾ point.		5 ½ Point.		5 ¼ Point.		5 Point.		

Distant	3 ¼ Points. Lat.	Dep	3 ½ Points. Lat.	Dep	3 ¾ Points. Lat.	Dep	4 Points. Lat.	Dep	Distant
1	·80	·60	·77	·63	·74	·67	·71	·71	1
2	1.61	1·19	1·55	1·27	1·48	1·34	1·41	1·41	2
3	2.41	1·79	2·32	1·90	2·22	2·01	2·12	2·12	3
4	3.21	2·38	3·09	2·54	2·96	2·69	2·83	2·83	4
5	4·02	2·98	3·86	3·17	3·70	3·36	3·53	3·53	5
6	4.82	3·57	4.64	3·81	4·45	4·03	4·24	4·24	6
7	5 62	4·17	5·41	4·44	5·19	4·70	4·95	4·95	7
8	6·43	4·77	6.18	5·07	5·93	5·37	5·66	5·66	8
9	7·23	5·36	6.96	5·71	6.67	6 04	6 36	6.36	9
10	8·03	5·96	7·73	6.34	7·41	6.72	7.07	7.07	10
11	8.83	6·56	8·50	6 97	8·15	7·39	7·78	7·78	11
12	9·64	7·15	9 28	7·61	8.89	8.06	8.48	8·48	12
13	10·44	7·75	10·05	8.24	9·63	8·73	9·19	9 19	13
14	11·24	8 34	10·82	8.88	10·37	9·41	9·90	9 90	14
15	12·05	8·94	11·59	9·51	11·11	10·08	10.60	10·60	15
16	12.85	9·53	12.37	10.15	11 86	10·75	11·31	11·31	16
17	13 65	10·13	13·14	10·78	12.60	11 42	12·02	12.02	17
18	14.46	10·73	13·91	11·41	13·34	12.09	12 73	12.73	18
19	15·26	11·32	14·69	12·05	14·08	12 76	13·43	13·47	19
20	16·06	11·91	15.46	12.69	14 82	13·43	14·14	14·14	20
21	16 86	12·51	16.23	13·32	15·56	14·10	14·85	14 85	21
22	17.67	13.10	17.01	13·96	16·30	14·77	15·55	15 55	22
23	18.47	13·70	17·78	14·59	17·04	15·44	16.26	16.26	23
24	19·27	14·29	18 55	15·23	17·78	16·12	16.97	16.97	24
25	20·08	14·89	19.32	15 86	18 52	16.79	17.67	17.67	25
26	20·88	15·48	20·10	16·50	19·27	17·43	18.38	18·38	26
27	21·68	16.08	20 87	17.13	20·01	18·13	19·09	19·09	27
28	22·48	16 68	21·64	17.76	20·75	18·80	19·80	19·80	28
29	23·28	17 27	22.42	18·40	21·49	19·47	20·50	20·50	29
30	24·10	17·87	23·19	19·03	22.23	20·15	21.21	21.21	30
31	24·89	18.47	23 96	19.66	22.97	20.82	21·92	21·92	31
32	25·70	19.06	24·74	20.30	23·71	21.49	22·62	22·62	32
33	26.50	19·66	25·51	20·93	24·45	22.16	23·33	23·33	33
34	27·30	20.25	26·28	21·57	25.19	22·84	24·04	24·04	34
35	28·11	20·85	27.05	22 20	25·93	23·51	24 74	24·74	35
36	28·91	21·44	27·83	22.84	26.68	24·18	25·45	25·45	36
37	29·71	22.04	28.60	23·47	27·42	24 85	26.06	26 16	37
38	30·51	22.64	29·37	24·10	28 16	25·52	26.87	26·87	38
39	31·31	23·23	30·15	24·74	28.90	26.19	27 57	27·57	39
40	32·13	23·83	30·92	25·38	29 64	26 86	28.28	28.28	40
41	32 92	24.43	31·69	26.01	30 38	27·53	28.99	28·99	41
42	33·73	25·02	32·47	26.65	31·12	28.20	29 69	29.69	42
43	34·53	25·62	33·24	37 28	31·86	28·87	30·40	30·40	43
44	35·33	26·21	34·01	27·92	32.60	29·55	31·11	31.11	44
45	36.14	26.81	34·78	28·55	33·34	30.22	31 81	31·81	45
46	36·94	27.40	35·56	29·19	34·09	30.86	32·52	32·52	46
47	37·74	28·00	36·33	29 82	34·83	31·56	33·23	33·23	47
48	38·54	28·60	37·10	30·45	35·57	32·23	33·94	33·94	48
49	39·34	29·19	37·88	31·09	36·31	32·90	34·64	34·64	49
50	40·16	29 78	38·65	31·72	37·05	33·58	35·35	35·35	50
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	4 ¼ points.		4 ½ Points.		4 ¾ Points.		4 Points.		

Distant	3 ¾ Points. Lat.	Dep	3 ½ Points. Lat.	Dep	3 ¼ Points. Lat.	Dep	3 Points. Lat.	Dep	Distant
51	40.96	30.38	39.42	32 35	37.79	34.25	36.06	36.06	51
52	41.77	30.97	40.20	32.99	38.53	34 92	36.76	36.76	52
53	42.57	31.57	40.97	33.62	39.27	35.59	37.47	37 47	53
54	43.37	32.16	41.74	34.26	40 01	36.27	38.18	38.18	54
55	44.18	32.76	42 51	34.89	40.75	36.94	38.88	38.88	55
56	44.98	33.35	43 29	35.53	41.50	37.61	39.59	39.59	56
57	45.78	33.95	44.06	36.16	42.24	38.28	40.30	40.30	57
58	46 58	34.55	44.83	36.79	42.97	38.95	41.01	41.01	58
59	47.39	35 14	45.61	37.43	43.72	39.62	41.71	41.71	59
60	48.19	35.74	46.38	38.06	44.46	40.29	42.43	42.43	60
61	48 99	36 34	47.15	38 69	45.20	40 96	43.14	43.14	61
62	49.80	36.93	47.93	39.33	45.94	41.63	43.84	43.84	62
63	50.60	37.53	48.70	39.96	46.68	42.30	44.55	44.30	63
64	51.40	38.12	49.47	40.60	47.42	42 98	45.26	45.26	64
65	52.21	38.72	50.24	41.23	48.16	43.65	45 96	45 96	65
66	53.01	39.31	51.02	41.87	48.91	44 29	46.67	46.67	66
67	53.81	39.91	51.79	42.50	49.65	44.99	47.38	47.38	67
68	54.62	40.51	52.56	43.13	50 39	45.66	48.09	48.09	68
69	55.42	41.10	53.34	43 77	51.13	46.33	48.79	48.79	69
70	56.23	41 70	54.11	44.41	51.87	47.01	49.50	49 50	70
71	57.03	42.30	54.88	45 04	52.61	47.68	50.21	50.21	71
72	57.84	42.89	55.66	45.68	53.35	48.35	50.91	50 91	72
73	58.64	43.49	56.43	46 31	54.09	49.02	51.62	51.62	73
74	59.44	44.08	57 20	46.95	54.83	49.70	52.33	52.33	74
75	60.25	44.68	57 97	47.58	55.57	50.37	53 03	53.03	75
76	61.05	45 27	58.75	48 22	56.32	51.04	53.74	53.74	76
77	61.85	45 87	59.52	48.85	57.06	51.71	54.45	54.45	77
78	62.66	46.47	60.29	49.48	57.80	52.38	55.16	55.16	78
79	63.46	47.06	61.07	50.12	58.54	53.05	55.86	55.86	79
80	64.26	47 66	61.84	50.75	59.28	53.72	56.57	56.57	80
81	65.06	48.26	62.61	51.38	60.02	54.39	57.28	57.28	81
82	65 87	48.85	63 39	52.02	60.76	55.06	57.98	57.98	82
83	66.67	49 45	64.16	52.65	61.50	55.73	58.69	58.69	83
84	67.47	50 04	64.93	53.29	62.24	56.41	59.40	59.40	84
85	68.28	50.64	65.70	53 92	62.98	57.08	60 10	60.10	85
86	69.08	51.23	66.48	54.56	63.73	57.72	60.81	60 81	86
87	69 88	51.83	67.25	55.19	64.47	58.42	61.52	61.52	87
88	70.69	52.43	68.02	55.82	65.21	59.09	62.23	62.23	88
89	71.49	53.02	68.80	56.46	65.95	59.76	62.93	62.93	89
90	72.29	53.61	69 57	57.10	66.69	60 44	63.64	63.64	90
91	73.09	54.21	70.34	57.73	67.43	61.11	64.35	64.35	91
92	73.90	54.80	71.12	58.37	68.17	61.78	65.05	65.05	92
93	74.70	55 40	71.89	59 00	68.91	62 45	65.76	65 76	93
94	75.50	55 99	72.66	59.64	69.65	63.13	66.47	66.47	94
95	76.31	56.59	73.43	60.27	70.39	63.80	67.17	67.17	95
96	77.11	57.18	74.21	60 91	71.14	64.47	67.88	67.88	96
97	77.91	57.78	74.98	61 54	71.88	65.14	68.59	68.59	97
98	78.72	58.38	75.75	62.17	72.62	65.81	69.30	69.30	98
99	79.52	58.97	76.53	62.81	73.36	66.48	70.00	70.00	99
100	80.32	59.57	77.30	63.44	74.10	67.16	70.71	70.71	100
	Dep	Lat.	Dep	Lat.	Dep	Lat.	Dep	Lat.	
	4 ¼ Points.		4 ½ Points.		4 ¾ Points.		4 Points.		

The Use of the preceeding Table of Difference of Latitude and Departure.

THis is a large Table, giving the Difference of Latitude and Departure to any Distance not exceeding 10000; and to every quarter Point of the Compass.

The Course stands at the Head and Foot of the Table; at the Head it begins at ¼ Point, so ½ Point ¾ Point, increasing to 4 Points; at the Foot it begins at 4 Points, so 4 ¼ Points 4 ½ Points; increasing backwards to 7 ¾ Points. The Distance is placed in the two outermost Columns of each Page, under the word *Distant*, on the left hand Page, beginning at 1, and increasing to 50; on the right hand Page, beginning at 51, and increasing to 100. The Difference of Latitude and Departure, stand under the Course at the Head of the Table, and over the Course at the Foot thereof, distinguished by the words *Lat.* and *Dep.*

1. In this Table, if your Distance exceed not 100 miles, or leagues, the Difference of Latitude and Departure will be given in miles or leagues, and 100 parts of a mile or league: But it may suffice, if the Difference of Latitude and Departure be taken only to miles or leagues, and 10th parts of a mile or league, with this allowance, that if the parts be 16 or more, instead thereof set down two tenths, (which is 20 hundreth parts); if 26, or more, 3 Tenths; if 36, or more, 4 Tenths; if 46, or more, 5 Tenths; if 56, or more, 6 Tenths; if 66, or more, 7 Tenths; if 76, or more, 8 Tenths; if 86, or more, 9 Tenths; if 96, or more, then make the Miles or Leagues of Difference of Latitude or Departure, 1 more than they are in the Table: As for instance, instead of 19.16, set down 19.2 Tenths; for 27.27, place 27.3; for 49.59, place 49.6; for 52.78, place 52.8; for 76.96, place 77. for 78 96, place 79 miles or leagues.

2. If the Distance be above 100, and not exceeding 1000, this Table gives the Difference of Latitude and Departure in miles or leagues, and tenth parts, being taken out at twice.

3. If the Distance be more than 1000, and exceeds not 10000, the Difference of Latitude and Departure is given in miles or leagues, as shall be explained by what follows.

This

This Table is very uſeful in the reſolving theſe 6 *Problems* in Navigation following; provided, in the five laſt Problems, the Diſtance either given or required, exceeds not an hundred miles or leagues.

Problem 1.

The Courſe and Diſtance given; To find the Difference, Latitude, and Departure.

1 *Example.*

A Ship ſayls W. S. W. *half* Weſt, 50 *miles*; *To find the Difference of Latitude and Departure.*

On the right Page of the Table, over 6½ Points, and right againſt 50 miles diſtance, you will find over the word *Lat.* 14.57, and over *Dep.* 47.85; which being contracted, according to the 1 Rule aforegoing, ſhews your Difference of Latitude to be 14.6 Tenths, and your Departure 47.8 Tenths, as was required.

2 *Example.*

A Ship ſayls Eaſt by North, half Eaſt, 125 *miles*; *To find the Difference of Latitude and Departure.*

This muſt be taken out of the Table at twice, after this following manner.

To perform this, you muſt account 1 at the beginning of the Table to be 10; and 2 to be 20; 3, 30; 4, 40; 5, 50; and ſo 10 to be 100; 11, 110; 12, 120; and 20 to be 200; 30, 300; 40, 400; 50, 500; 60, 600; 70, 700; 80, 800; 90, 900; and 100 at the end to be 1000.

According to this Direction, againſt 12 (which ſtands for 120) on the left hand Page, over 7½ Points ſtands 1.18 over *Lat.* and 11.94 over *Dep.* which done, according to the ſecond Rule before given, your Difference of Latitude is 1.2, and your Departure 11.9; then take out the Difference of Latitude and Departure for the remainder, which is 5, according to the firſt Rule aforegoing, and after the manner of the *firſt Example of this Problem*; ſo you will find the Difference of Latitude to be 0.5, and your Departure 5.0: This done, ſet them down, and add them together after this manner.

Dist.	Lat.	Dep.
120	11.8	119.4
5	0.5	5.0
125	12.3	124.4

So that your Difference of Latitude for the whole Distance 125 miles, is 12.3 Tenths, and your Departure 124.4 Tenths.

3 *Example.*

A Ship Sayls North-West by North, ½ West, 976 miles; To find the Difference of Latitude, and the Departure.

Under 3 ½ Points, and against 97 (taken for 970) stands 77.91, and 57.78, that is the Difference of Latitude 779.1 Tenth, the Departure 577.8 Tenths; against 6 stands 4.82 and 3.57; that is, the Difference of Latitude 4.8 Tenths, the Departure 3.6 Tenths; which added together, makes the whole Difference of Latitude 783.9, and the Departure 581.4.

4 *Example.*

A Ship sayls North-East by North, half East, 7968 miles, to find the Difference of Latitude and Departure.

To perform this, you must account 1 at the beginning of the Table to be 100; 2 to be 200; 3, 300; 4, 400: And so 10 to be 1000; 11 to be 1100; 12, 1200; 13, 1300; 14, 1400; So 20 to be 2000; 30, 3000; 40, 4000; 50, 5000; 60, 6000; 70, 7000; 80, 8000; 90, 9000; and 100, 10000.

According to this Direction, against 79 (taken for 7900) and under 3 ⅓ Points, stands 6107 for the Difference of Latitude, and 5012 miles for the Departure, according to the third Rule. Then take out the Difference of Latitude and Departure for the Remainder 68, according to the first Rule, which you will find to be 52.6, and 43.1; so the whole Difference of Latitude is 6159.6 miles, and the Departure 5055.1 miles.

Problem 2.

The Course and Difference of Latitude being given; To find the Distance and Departure.

Example.

A Ship sayls W. N. W. *half* West, *until her Difference of Latitude be* 14.5 *leagues; To find the Distance and the Departure.*

Look over 6 ½ Points, the Course, in the Column of Latitude, until you find 14.5, and right against it you will find the Distance 50 leagues, and the Departure 47.8 leagues.

Problem 3.

The Course and Departure given, To find the Difference of Latitude and the Distance.

Example.

A Ship sayls South-West by South, ½ *West, until her Departure be* 47.7 *leagues; To find the Difference of Latitude and Distance.*

Look in the Column of Departure, under 3 ½ Points, until you find 47.7; and right against it you see 52.6 leagues, for the Difference of Latitude, and 71 leagues for the Distance.

Problem 4.

The Difference of Latitude and Distance given; To find the Course and Departure.

Example.

A Ship sayls 50 *leagues between the South and the West, until her Difference of Latitude be* 14.5 *leagues; To find the Course and Departure.*

Look over your several Columns in the Table, until right against 50 the Distance, you find 14.5 in the Column of Latitude, over the Course, which will be 6 ½ Points; and in the Column of Departure you will find your Departure to be 47.8.

Problem 5.

The Distance and Departure given; To find the Course and Difference of Latitude.

Example.

A Ship sayls 80 leagues North-Easterly, until her Departure be 53.7 leagues; To find the Course and Difference of Latitude?

Look over the several Columns in the Table, until right against 80 the Distance, you find 53.7 in the Column of Departure; over it you will see 3 ½ Points, or North-West by North ¼ West, and the Difference of Latitude (in the Column of Latitude, right against 80) to be 59.3 leagues.

Problem 6.

The Difference of Latitude and Departure being given; To find the Course and Distance.

Example.

A Ship sayls between the North and the East, until her Difference of Latitude be 56.3 leagues, and her Departure 51.0; To find the Course and Distance.

Look over your several Columns of Latitude and Departure, until you find 56.3 to stand against 51.0, or the neareſt thereto, which will be under 3 ½ Points, which makes the Course North-East by North, half East; and right against 67 leagues, which is the Distance required.

Problem 7.

How to Work a Traverse, by the Tables of Latitude and Departure.

These Tables, in the Working of a Traverse, are both readier, and far more exact, than any Instrument commonly used for that purpose. See *Problem 8. of the Sinical Quadrant*, pag. 236.

Example.

Example.

A Ship ſayls South-Weſt by South 37 min. then South by Eaſt 39 min. then South-Eaſt by South, half Eaſt, 47 min. then Weſt by North 59 min. then W. N. W. 62 min. then South-Weſt, half Weſt, 27 min. To find the Difference of Latitude and Departure, and the direct Courſe and Diſtance from the firſt Place.

Set down the ſeveral Courſes and Diſtances as in the following Table.

Courſe.	*Diſt.*	*Nor.*	*South.*	*Eaſt.*	*Weſt.*
South-Weſt by South.	37		30.8		20.6
South by Eaſt.	39		38.2	07.6	
S. E. by South, ½ Eaſt.	47		36.3	29.8	
Weſt by North.	59	11.5			57.9
W. N. W.	62	23.7			57.3
South-Weſt, ½ Weſt.	27		17.1		20.9
		35.2	122.4	37.4	156.7
			35.2		37.4
		Diff. Lat.	87.2	Dep.	119.3

Then by *Prob'em* 1. find the Difference of Latitude and Departure for thoſe Courſes and Diſtances ſeverally, which place in their proper Columns, *viz.* If the Courſe be North-Eaſterly, place the Difference of Latitude in the North Column, (under *Nor.*) the Departure in the Eaſt Column, (under *Eaſt*): If the Courſe be South-eaſterly, place the Difference of Latitude in the South Column, (under *South*) and the Departure in the Eaſt Column. If the Courſe be North-Weſterly, place the Difference of Latitude in the North Column, and the Departure in the Weſt Column. If the Courſe be South-Weſterly, place the Difference of Latitude in the South Column, and the Departure in the Weſt Column.

As for inſtance; In the foregoing Table, the firſt Courſe is South-Weſt by South, the Diſtance 37: Becauſe the Courſe is South-Weſterly, you muſt place the Difference of Latitude 30.8 in the South Column, and the Departure 20.6 in the Weſt Column, as you ſee in the Table.

The

The second Course is South by East, the Distance 39; Therefore because the Course is South-Easterly, you must place the Difference of Latitude in the South Column, and the Departure in the East Column: The like is to be understood of the rest.

Having found the Difference of Latitude and Departure for all your several Courses, and inserted them in their proper Columns, you must then add up your *North*, *South*, *East*, and *West* Columns, and substract the North and South Columns the one from the other, *viz.* the less from the greater; and likewise the East and West Columns. So in the Table, the sum of the North Column is 35.2, of the South Column 122.4, of the East Column 37.4, and of the West Column 156.7; substracting the North Column from the South, the Remainder is 87.2, the Difference of Latitude Southerly; and substract the East Column from the West, the Remainder is 119.3, the departure Westerly.

Having the Difference of Latitude and Departure, you may find the Course and Distance by *Problem* 6. But in this Example, because your Difference of Latitude 87.2, and your Departure 119.3. out-run the Table, that is to say, you can find no such numbers in the Table; therefore take the half of your Difference of Latitude, which is 43.6, and the half of your Departure, which is 59.6. According to the Direction in the sixth *Problem*, over 4 Points $\frac{1}{4}$, against 44.1 in the Column of Latitude, you will find 59.4 in the Column of Departure, (which are the two neareſt numbers in the Table) and in the Column of the Distance 74, which being doubled is the Distance sought: The Course is between the South and the West, because the Difference of Latitude is Southerly, and the Departure Westerly, therefore the Course is South-West, $\frac{1}{4}$ West, which was required.

This Table in particular is very useful for the easie forming of a *Sea-Reckoning*, or *Journal*; as shall be instanced in this following Table, being a Journal from the *Lizard* to the *Barbadoes*.

The Title of your *Journal* may be as follows.

A Journal of our Voyage intended, by God's permission, from the Lizard, *in the Latitude* 50° 00′, *North, Longitude (from the* Pico *of* Teneriff) 12° 37′; *and the Island of* Barbadoes, *in the Latitude* 13° 12′, *North, Longitude* 319° 40′. *The Difference of Longitude between the* Lizard *and the* Barbadoes *is* 52° 57′, *the Course South-West, half West, Distance* 2821 *min.* March 20. 1672. *the* Lizard *bears North, distant* 30 *min.*

How

Days	Month and Lat. by observation.	The Course Corrected.	Diſt. in min.	North	Southing. min.	Eaſting. min.	Weſting. min.	Lat. by reckon. d. m.	Eaſt Long. min.	Weſt Longit. min.
22	*March.*	*Lizard* South.	30		30.0			49.30		
23		South-Weſt.	112		79.2		79.2	48.11		120.0
24	47° 00′	S.W. by S. ½ W.	72		55.6		45.7	47.15		68.1
		Correction by Obſervat.			15.0		11.0	47.00		16.0
25		S.W. by South.	96		79.8		53.3	45.40		75.2
26		S.W. by South.	79		65.7		43.9	44.34		62.8
27	42 37	S.W. by South.	138		114.6		76.7	42.39		106.2
28		S.S.W. ¾ Weſt.	129		110.7		66.3	40.48		88.8
29		S. S. W.	72		66.5		27.6	39.41		36.4
30	37 44	S.S.W. ½ Weſt.	102		90.0		48.0	38.11		62.0
		Correction by Obſervat.			27.0		16.0	37.44		20.0
1	*April.*	South-Weſt.	85		60.1		60.1	36.44		75.0
2		W. S. W.	20		7.6		18.5	36.36		24.1
3		S. by W. ½ W.	32		30.6		9.3	36.05		11.9
4	34 10	South by Weſt.	120		117.7		23.4	34.07		27.9
		Correct. by Obſerv.	3.0			1.0		34.10	1.0	
5		S. by W. ⅓ W.	164		156.9		47.6	31.33		56.7
6	29 37	S. S. W.	125		115.5		47.9	29.37		55.9
7		S.W. by South.	110		91.4		61.2	28.06		69.5
8		S.W. by South.	122		101.4		67.8	26.25		76.2
9	24 43	South-Weſt.	116		82.0		82.0	25.03		91.0
		Correction by Obſervat.			20.0		11.0	24.43		12.0
10		South-Weſt.	97		68.6		68.6	23.34		75.0
11		South-Weſt.	96		67.9		67.9	22.26		74.0
12		South-Weſt.	114		80.6		80.6	21.05		88.0
13		South-Weſt.	118		83.5		83.5	19.41		89.0
14		S.W. by Weſt.	110		61.2		91.4	18.40		96.2
15		W. S. W.	91		34.8		84.1	18.05		89.4

Dayes	Month and Lat. by observation.	The Course Corrected.	Dist. in min.	Nort.	South ing. min.	East ing. min.	West ing. min.	Lat. by reckon. d. m.	East Long min.	West Long. min.
	1672.		*Brought from the other side*					18.05	1.0	1667.3
16	*April.*	W.S.W	91	—	34.8	—	84.1	17.30	—	87.0
17		W.S.W.	84	—	32.1	—	77.6	16.58	—	82.0
18		W.S.W.	107	—	41.0	—	98.9	16.17	—	103.7
19		W.S.W.	103	—	39.5	—	95.2	15.37	—	99.0
20	14 43	W.S.W.	116	—	44.4	—	107.2	14.53	—	111.0
		Correct. by Observ.			10.0	—	15.9	14.43	—	16.0
21		W. by S.	110	—	21.5	—	107.9	14.21	—	114.1
22		W. by S.	120	—	23.4	—	117.7	13.58	—	119.1
23		W. by S.	106	—	20.7	—	104.0	13.37	—	108.7
24		W. by S.	100	—	19.5	—	98.1	13.17	—	103.8
25		W. by S.	120	—	23.4	—	117.7	12.54	—	118.7
26	13° 12′	W. by N.	100	19.5	—	—	98.1	13.14	—	103.1
27		West.	130	—	—	—	130.0	13.12	—	133.5
28		West.	136	—	—	—	136.0	13.12	—	139.8
29	13° 12′	West.	69	—	—	—	69.0	13.12	—	70.8

The whole Difference of Longitude is 3177.6, or 3178 *min.* which is 52° 58′ Westerly.

The Explanation of this Journal.

In this *Journal* there are eleven Columns; The first contains the *dayes of the Month*; the second, the *Month of the Year*, and *Latitude by Observation*; the third, the *Course Corrected*, by the allowance for *Leeway*, or for the *Variation of the Compass*, if there be any; the fourth, the *Distance sayled*; the fifth, sixth, seventh, and eighth, the *Northing*, *Southing*, *Easting*, and *Westing*, being the Difference of Latitude and Departure of the several Courses and Distances; the ninth, the *Latitude* by *Dead-Reckoning*; the tenth, the *East Longitude*; the eleventh, the *West Longitude*.

Here

Here I would adviſe all that are deſirous to give a good account of their Reckoning, to any that have Reaſon or Authority to demand it, That they keep a particular Account of that which they take off the *Log-board* every day at Noon, either in the ſame Book where they keep their Reckoning, or elſe in a Book diſtinctly for that purpoſe, commonly called a *Log-Book*.

Now, the manner of proceeding in this *Journal*, by the help of the Table of *Latitude and Departure*, is very facile, as followes; the 22d of *March*, at noon, I find the *Lizard* to bear North, and to be diſtant about 10 leagues, or 30 miles, or minutes; therefore I am to the ſouthward of the *Lizard* 30 minutes; which 30 minutes I place in the *South Column*, and that makes my *Latitude* 49 *deg.* 30 *min.*

The 23d day, my Courſe is South-Weſt, and the Diſtance 112 minutes; to find the Difference of Latitude and Departure, by the Table of *Latitude and Departure*, according to *Problem* 1. The Difference of Latitude is 79.2, and the Departure 79.2, Becauſe the Courſe is South-Weſterly, I place the Difference of Latitude in the *South Column*, and my Departure in the *Weſt Column*; 79 *min.* or 1° 9′ ſubſtracted from 40° 30′, gives the Latitude 48° 11′.

How to find the Difference of Longitude.

To find the Difference of Longitude in the two laſt Columns, you have both Latitudes, 48 *deg.* 11 *min.* and 49 *deg.* 30 *min.* (the preſent Latitude, and the Lat. of the day before) and the Courſe S. W. by which you may find the Diff. Longitude, according to the proportion in *Chap.* 5. *Prob.* 3. of *Mercators Sayling*: Saying, *As Radius, to the Meridional Diff. Latitude*; *So is the Tang. of the Courſe, to the Diff. Longitude.* This Proportion being wrought by the *Logarithmes*, or the *Gunters Scale*, (which may ſerve in this caſe) you will find the Diff. Longitude 120 *min.* which place in the *Weſt Column*, becauſe your Courſe is Weſterly.

The 24th day is wrought after the manner of the 23d, having the Courſe and Diſtance given, to find the Diff. Latitude, Departure, and Diff. Longitude, as was ſhewed before.

How to Correct your Reckoning by Obſervation of the Latitude.

On the 24th of *March*, by a good Obſervation, I find my Latitude to be 47 *deg.* whereas by my Reckoning I ſhould be in the Lat. 47 *deg.*

15 *min.* ſo that the Difference is 15 *min.* more Southerly: Therefore to Correct my Latitude, I place 15 *min.* in the *South Column*; which ſubſtracted from 47 *deg.* 15 *min.* makes my Latitude by Reckoning, to agree with the Obſervation. To Correct your Departure, you muſt conſider, whether the fault may be imputed to your Courſe, or to your Diſtance; if your Courſe be well ſteered, and you find no *Current*, nor any Variation of the Compaſs, then your Diſtance is faulty: But if you cannot truſt to the Courſe ſteered, then your beſt way is to Correct your Latitude only, not medling with your Departure. If there be a *Current*, and you know which way the *Current ſets*, and *how faſt*, then find the Diff. Latitude and Departure of the Current, and add or ſubſtract that Latitude and Departure, to or from the Ships Diff. Latitude and Departure, according as the *Current* doth farther or hinder your Ship in her Courſe. But if you only by ſome probable reaſon conjecture there is a *Current*, then give what allowance you think meet in Diff. Latitude and Departure, and ſee if that will reform your Reckoning in your Latitude; if ſo, you have gueſſed well; but if it will not, it's to be ſuppoſed that you are miſtaken in your Conjecture, or that there is ſome other cauſe of this Error in your Reckoning.

If the *Compaſs* varies, (as moſt commonly it doth) then finding what the Variation is, and which way it is, you muſt allow it in the Ships Courſe.

But if you cannot impute the Error to any of theſe, then (as I ſaid before) the Diſtance is faulty, and this is that which uſually makes the Difference between the Latitude Obſerved, and the Latitude by your Reckoning: and this I take to be the cauſe of the error this 24*th* day of *March*, and generally in this Reckoning.

Now to Correct your Departure and Diff. Longitude; you muſt add up the *North*, *South*, *Eaſt*, and *Weſt Columns*, from the day that you Correct, to the beginning of your *Journal-Tables*; if it be the firſt Correction you have made, or from the day of Correction to the laſt Correction; if it be the *ſecond*, *third*, *fourth*, &c. then ſubſtract the Sums of the *North* and *South Columns* from each other, and likewiſe of the *Eaſt* and *Weſt*; And ſay, by the Rule of Proportion, As the Difference of the *North* and *South Columns*, to the Diff. of the *Eaſt* and *Weſt Columns*; So is the Diff. between the Latitudes by Obſervation and Reckoning; to the Diff. in the Departure. And for the Diff. Longitude, As the Diff. between the Latitudes by Obſervation and Reckoning, to the Meridional Difference for thoſe two Latitudes; So is the Diff. in the Departure, to the Diff. in the Longitude.

Example.

Example.

The 24*th* day you will find the Sum of the *North* Column 00, the Sum of the *South* Column (leaving out 15 *min.* the Error) 164.8 *min.* and therefore their Diff. is 164.8: The Sum of the *East* Column is 00 *min.* of the *West* Column 124.9, and their Diff. 124.9. Then the Operation by the *Logarithms* will be,

		Co. Ar.
As the Diff. of the *North* and *South* Columns	164.8 ——	7.78304
To the Diff. of the *East* and *West* Columns	124.9 ——	2.09656
So is the Diff. between the two Latitudes	15.0 ——	1.17609
To the Difference in the Departure	11. ——	*x* 1.05569

Place this 11 *min.* in the *West* Column, because the Sum of the *West* Column exceeds the Sum of the *East* Column.

In this Operation we neglect the *Tenths of the Departure*, as not to be regarded.

The Operation for the Difference in the Longitude.

The two Latitudes are 47 *deg.* 15 *min.* & 47 *deg.* 00 *min.* by which, in the Table of *Meridional Parts*, you will find the Meridional Diff. Latitude 22 *min.* Therefore,

		Co. Ar.
As the *Diff. between the two Latitudes*	15 min. ——	8.82391
To the *Meridional Diff. of those Lat.*	22 min. ——	1.34242
So is the *Diff. in the Departure*	11 min. ——	1.04139
To the *Diff. in the Longitude*	16 min. ——	*x* 1.20772

This 16 *min.* is placed in the *West* Column, because the Departure is Westerly.

After the same manner are the Corrections made in this *Journal*, upon the 30*th* of *March*, the 4*th*, the 9*th*, and the 20*th* dayes of *April*; the Error being supposed to be in the computation of the Distance.

If your Ship saile several Courses in 24 hours, you must find your Diff. Latitude and Departure, by working a *Traverse*, according to *Problem* 7, in the Use of the Table of *Latitude and Departure*; your Diff. Latitude will give you what Latitude the Ship is in; then have you

two Latitudes, *viz.* the Latitude the Ship was in the day before, at Noon, and the Latitude the Ship is now in, by which you may find the Meridional Diff. Latitude, by the Table of *Meridional Parts*, according to *Chap. 5. Prob. 1.* of *Mercators Sayling.*

Then, for your Diff. Longitude, say,

As the Diff. Latitude found by the *Traverse,*
To the Diff. Latitude in Meridional Parts:
So is the Departure found by the Traverse,
To the Diff. Longitude for that Traverse.

To find the whole Diff. Longitude of the two Ports between which you make your Voyage.

Add up the Columns of *East* and *West* Longitude, and substract the one from the other, the Remainder reduced into *deg.* and *min.* is the Diff. Longitude sought.

In this *Journal*, the Diff. of the *East* and *West* Columns of Longitude, is 3177.6, or 3178 *min*; which reduced into *deg.* and *min.* makes 52 *deg.* 58 *min.* the Diff. Longitude between the *Lizard* and the *Barbadoes.*

The Use of the Table of ten Chiliads, or ten thousand Logarithmes.

1. *ANY Number given under* 10000; *To find the Logarithme thereof.*

The left hand Column of every Page, contains Numbers, increasing in their Natural Order, from 1 to 999. The other five Columns of each Page, contain the *Logarithmes* of all Numbers, from 1 to 9999: These Columns on the left hand Page, are distinguished with the figures 0. 1. 2. 3. 4. those on the right hand Page with 5. 6. 7. 8. 9.

The Numbers in the left hand Column, by the supply of those figures on the top of the other Columns, are extended to 9999, and are to be read cross both Pages.

If the Number propounded to find its Logarithm, consist of one place; as suppose you were to find the *Logarithme* of (7); look for (7) among the Figures on the top of the Columns, and right against (0) in the

the left hand Column, and under (7), you will find 0.8450980, which is the *Logarithme* of 7.

If the Number propounded conſiſt of two places, as (68); look the firſt Figure (6) in the left hand Column, and the laſt Figure (8) at the top of the Page; then right againſt (6) and under (8), you will find 1.8325089, which is the *Log.* of 68.

If the Number conſiſt of three places, as 574, look for the two firſt Figures (57) in the left hand Column, and the laſt Figure (4) at the top of the Page; then right againſt (57) and under (4), you will find 2.5789119, which is the *Logar.* of 574.

If the Number conſiſt of four places, as 9499, look the three firſt Figures (949) in the left hand Column, and the laſt Figure (9) at the top of the Page; ſo right againſt (949) and under (9), you will find 3.9776779, which is the *Logar.* of 9499.

2. *A Logarithme being given; To find the correſpondent Number.*

Note; If the firſt Figure of the given *Logarithme* be (0) the Number ſought conſiſts of one place; if it be (1), it conſiſts of two places; if it be (2), of three places; if it be (3) of four places.

Let the Log. be 0.9030900; this *Logar.* will be found in the firſt line of the Table againſt (0); for if you look in the firſt line, croſſing both Pages, under (8) upon the right hand Page, you will find the given Logar, which ſhews that (8) is the Number ſought.

Let the Log. be 1.9190781; look down the ſecond Column of the left hand Page, among thoſe Logarithmes, and you will find the neareſt, being leſs than the given Log. to be 1.9030900, and the Number againſt it, in the left hand Column, is (8), then look croſs the Pages in the ſame line againſt (8), and under (3) at the top of the Page, you will find the Logar. given; therefore the Number ſought is 83.

Let the Log. be 2.8318698; Look down the ſecond Column of the left hand Page, until you find a Logar. being the neareſt leſs than the given Logar. which will be 2.8260748, and the Number againſt it, in the left hand Column, is 67; then look croſs both Pages in the ſame line againſt 67, and under (9) (at the top of the Page) you will find the given Logar. therefore the Number ſought is 679.

Let 3.9802761 *be the Logar. given*; Look down the ſecond Column, as before, and you will find the neareſt leſs to be 3.9800034, and the Number againſt it 955; and croſſing the Pages, as before directed, under (6) you will have the given Logar. therefore the Number ſought is 9556.

Let

Let the Logar. *given be* 3.9664379; If you look in the Table, according to the former Directions, you cannot find any Logar. the same with this here given; and this is commonly the case in the use of these Tables; but then you must find the nearest, being less than the Logar. given; which is 3.9664233, and the number answering thereto is 9256, which is the Number sought.

The Use of the Table of Artificial, or Logarithmical, Sines, Tangents, and Secants.

THis Table contains the *Logarithmical Sines, Tangents, and Secants, of every Degree and Minute of the Quadrant.*

1. *To find the Sine, Tangent, or Secant, of any degree and minute.*

If the Degrees be less than 45, your *Sine, Tangent,* or *Secant,* is found in those Columns, which are distinguished by the words, *(Sine) (Tang) (Secant)* at the head of the Table.

But if the Degrees exceed 45, then your Sine, Tangent, or Secant, is found in those Columns, which are distinguished with the words *(Sine) (Tang) (Secant)* at the foot of the Table.

Suppose you were to find the Log. Sine, Tangent, or Secant of 32 deg. 12 min. Look for 32 *Degrees* at the head of the Table, and upon the left hand Page, in the Column of *Minutes*, under the Letter (M), you will find 12 *min* and against 12 *min.* and under *Sine* at the head of the Table, you shall find 9.7266274, which is the *Log. Sine* of 32 *deg.* 12 *min.* and against 12 *min.* and under (*Tang*) you have 9.7991569, the *Log. Tangent* of 32 *deg.* 12 *min.* And against 12 *min.* and under (*Secant*) you have 10.0725305, the *Log. Secant* of 32 *deg.* 12 *min.*

Suppose you were to find the Log. Sine, Tangent, or Secant of 37 deg. 47 min; Turn to 37 *Degrees* at the head of the Table, and upon the right hand Page (because the Minutes exceed 30) in the Column of Minutes under (M), you must look for 47 *min.* and against 47 *min.* and under (*Sine*) at the head of the Table, you will find 9.7872317, the *Sine* of 37 *deg.* 47 *min.* And against 47, and under (*Tang*), you will find 9.8894214, the *Tangent* of 37 *deg.* 47 *min.* And against 47, and under (*Secant*) you will find 10.1021897 the *Secant* of 37 *degrees* 47 *minutes.*

Suppose

Suppoſe you were to find the Log. Sine, Tangent, or Secant of 64 deg. 15 min. Turn to 64 *Degrees* at the foot of the Table, and upon the right hand Page, in the Column of *Minutes*, over the letter (M) look upwards for 15 *min.* againſt 15 *min.* and over (*Sine*) at the foot of the Table, you will find 9.9545793, the *Sine* of 64 *deg.* 15 *min.* and againſt 15 *min.* and over (*Tang*) you will find 10 3166443, the *Tangent* of 64 *deg.* 15 *min.* And againſt 15 *min.* and over (*Secant*) you will find 10.3620649 the *Secant* of 64 *deg.* 15 *min.*

Suppoſe you were to find the Log. Sine, Tangent, or Secant of 78 deg. 45 min. Turn to 78 *Degrees* at the foot of the Table, and upon the left hand Page (becauſe the Minutes exceede 30) in the Column of Minutes over (M) look for 45 *min.* againſt 45, and over (*Sine*), you find the *Sine* of 78° 45′, to be 9.9915739, and the *Tangent*, in the ſame Line over (*Tang*) to be 10.7013382; and the *Secant*, over (*Secant*) to be 10.7097643.

2. *A Log. Sine, Tangent, or Secant, being given, to find the Degrees and Minutes anſwering thereto.*

This is but the Converſe of the former, but that you may the more readily turn to the *degree* and *minute* required, take this brief Direction.

If it be a *Sine*, and the five firſt Figures leſs than 9.8494, or a *Tangent* leſs than *Radius*, or 10.0000000; or a *Secant*, and the ſix firſt Figures leſs than 10.1505; then it is a *Sine*, *Tangent*, or *Secant* of leſs than 45 *deg.* and is to be ſought, in thoſe Columns diſtinguiſhed with (*Sine*) (*Tang.*) (*Secant*) at the head of the Table; but if the *Sine*, *Tangent*, or *Secant*, exceed theſe reſpective Numbers, then the *Degrees* anſwering thereto are more than 45, and they are to be found in thoſe Columns diſtinguiſhed by (*Sine*) (*Tang*) (*Secant*) at the foot of the Table.

Suppoſe you were to find the Degrees and Minutes correſponding to this Sine 9.7035327: This being leſs than 45, I run over the Columns of *Sines*, diſtinguiſhed by (*Sine*) at the top; and under 30 *deg.* and againſt 21 *min.* I find the given *Sine*.

Suppoſe I were to find the Degree and Minute correſponding to this Tangent, 10.3862931: This being greater then 45 *deg.* I run over the Columns of *Tangents*, diſtinguiſhed by (*Tang*) at the foot of the Table; and over 67 *deg.* and againſt 39 *min.* I find the neareſt leſs, *viz.* 10.3860000, and therefore the neareſt *deg.* and *min.* correſponding, are 67 *deg.* 39 *min.*

1. *Note*,

1. *Note*, If you are to find the *Sine Complement*, *Tangent Complement*, or *Secant Complement*, of any *deg.* and *min.* As, ſuppoſe you were to find the *Sine Complement* of 39 *deg.* 17 *min.* Subſtract 39 *deg.* 17 *min.* from 90 *deg.* 00 *min.* and look the Sine of the Remainder, (or Complement to 90 *deg.*) *viz.* the Sine of 50 *deg.* 43 *min.*

2. *Note*, If you are to find the *Sine*, *Tangent*, or *Secant*, of any Number of *deg.* and *min.* exceeding 90. As, ſuppoſe you were to find the *Tangent* of 127 *deg.* 39 *min.* ſubſtract 127 *deg.* 39 *min.* from 180 *deg.* 00 *min.* and find the *Tangent* of the Remainder, *viz.* the *Tang.* 52 *deg.* 21 *min.* which is alſo the *Tangent* 127 *deg.* 39 *min.* as was required.

I have been the more prolix in explaining theſe Tables, becauſe I would have any Body readily to uſe them, without the help of a Tutor.

A

TABLE

Containing

Ten Chiliads

OF

LOGARITHMES:

For Numbers increasing in their Natural Order, from 1 to 10000.

LONDON,

Printed by *John Darby*, for *John Seller*, and *John Wingfield*, 1672.

Num	0	1	2	3	4
0	0.0000000	0.0000000	0.3010300	0.4771212	0.6020600
1	1.0000000	1.0413927	1.0791812	1.1139433	1.1461280
2	1.3010300	1.3222193	1.3424227	1.3617278	1.3802112
3	1.4771212	1.4913617	1.5051500	1.5185139	1.5314789
4	1.6000600	1.6127838	1.6232493	1.6334684	1.6434527
5	1.6989700	1.7075702	1.7160033	1.7242759	1.7323937
6	1.7781512	1.7853298	1.7923917	1.7993405	1.8061800
7	1.8450980	1.8512583	1.8573325	1.8633228	1.8692317
8	1.9030900	1.9084850	1.9138138	1.9190781	1.9242793
9	1.9542425	1.9590414	1.9637878	1.9684829	1.9731278
10	2.0000000	2.0043214	2.0086002	2.0128372	2.0170333
11	2.0413927	2.0453230	2.0492180	2.0530784	2.0569048
12	2.0791812	2.0827854	2.0863598	2.0899051	2.0934217
13	2.1139433	2.1172713	2.1205739	2.1238516	2.1271048
14	2.1461280	2.1492191	2.1522883	2.1553360	2.1583625
15	2.1760912	2.1789769	2.1818436	2.1846914	2.1875207
16	2.2041200	2.2068259	2.2095150	2.2121876	2.2148438
17	2.2304489	2.2329961	2.2355284	2.2380461	2.2405492
18	2.2552725	2.2576786	2.2600714	2.2624511	2.2648178
19	2.2787536	2.2810333	2.2833012	2.2855573	2.2878017
20	2.3010300	2.3031960	2.3053513	2.3074960	2.3096301
21	2.3222193	2.3242824	2.3263358	2.3283796	2.3304138
22	2.3424227	2.3443923	2.3463530	2.3483048	2.3502480
23	2.3617278	2.3636120	2.3654880	2.3673559	2.3692158
24	2.3802112	2.3820170	2.3838153	2.3856063	2.3873898
25	2.3979400	2.3996737	2.4014005	2.4031205	2.4048337
26	2.4149733	2.4166405	2.4183013	2.4199557	2.4216039
27	2.4313637	2.4329693	2.4345689	2.4361626	2.4377505
28	2.4471580	2.4487063	2.4502491	2.4517864	2.4533183
29	2.4623980	2.4638930	2.4653828	2.4668676	2.4683473
30	2.4771212	2.4785665	2.4800069	2.4814426	2.4828736
31	2.4913617	2.4927604	2.4941546	2.4955443	2.4969296
32	2.5051500	2.5065050	2.5078559	2.5092025	2.5105450
33	2.5185139	2.5198280	2.5211381	2.5224442	2.5237464
34	2.5314789	2.5327544	2.5340261	2.5352941	2.5365584
35	2.5440680	2.5453071	2.5465426	2.5477747	2.5490033
36	2.5563025	2.5575072	2.5587086	2.5599066	2.5611014

Num	5	6	7	8	9
0	0.6989700	0.7781512	0.8450980	0.9030900	0.9542425
1	1.1760912	1.2041200	1.2304489	1.2552725	1.2787536
2	1.3979400	1.4149733	1.4313637	1.4471580	1.4623980
3	1.5440680	1.5563025	1.5682017	1.5797836	1.5910646
4	1.6532125	1.6627578	1.6720978	1.6812412	1.6901961
5	1.7403627	1.7481880	1.7558748	1.6734280	1.7708520
6	1.8129133	1.8195439	1.8260748	1.8325089	1.8388491
7	1.8750612	1.8808136	1.8864907	1.8920946	1.8976271
8	1.9294189	1.9344984	1.9395192	1.9444827	1.9493900
9	1.9777236	1.9822712	1.9867717	1.9912261	1.9956352
10	2.0211893	2.0253058	2.0293838	2.0334237	2.0374265
11	2.0606978	2.0644580	2.0681858	2.0718820	2.0755469
12	2.0969100	2.1003705	2.1038037	2.1072099	2.1105897
13	2.1303337	2.1335389	2.1367205	2.1398791	2.1430148
14	2.1613680	2.1643528	2.1673173	2.1702617	2.1731862
15	2.1903317	2.1931246	2.1958996	2.1986571	2.2013971
16	2.2174839	2.2201081	2.2227165	2.2253093	2.2278867
17	2.2430380	2.2455127	2.2479732	2.2504200	2.2528530
18	2.2671717	2.2695129	2.2718416	2.2741578	2.2764618
19	2.2900346	2.2922561	2.2944662	2.2966652	2.2988531
20	2.3117538	2.3138672	2.3159703	2.3180633	2.3201463
21	2.3324384	2.3344537	2.3364597	2.3384565	2.3404441
22	2.3521825	2.3541084	2.3560258	2.3579348	2.3598355
23	2.3710678	2.3729120	2.3747483	2.3765770	2.3783979
24	2.3891661	2.3909351	2.3926969	2.3944517	2.3961993
25	2.4065402	2.4082399	2.4099331	2.4116197	2.4132997
26	2.4232459	2.4248816	2.4265112	2.4281348	2.4297523
27	2.4393327	2.4409091	2.4424797	2.4440448	2.4456042
28	2.4548448	2.4563660	2.4578819	2.4593925	2.4608978
29	2.4698220	2.4712917	2.4727564	2.4742162	2.4756712
30	2.4842998	2.4857214	2.4871384	2.4885507	2.4899585
31	2.4983105	2.4996871	2.5010593	2.5024271	2.5037907
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162	3.2095150	3.2097830	3.2100508	3.2103185	3.2105860
163	3.2121876	3.2124540	3.2127201	3.2129862	3.2132521
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165	3.2174839	3.2177471	3.2180100	3.2186728	3.2185355
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167	3.2227165	3.2229764	3.2232363	3.2234959	3.2237554
168	3.2253093	3.2255677	3.2258260	3.2260841	3.2263421
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174	3.2405492	3.2407988	3.2410481	3.2412974	3.2415465
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176	3.2455127	3.2457593	3.2460059	3.2462523	3.2464986
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195	.2900346	.2902573	.2904798	.2907022	.2909246
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189	.2776092	.2778383	.2780673	.2782962	.2785250
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195	.2911468	.2913688	.2915908	.2918127	.2920344
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239	.3783979	.3785796	.3787612	.3789427	.3791241
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264	.4224257	.4225898	.4227539	.4229180	.4230820
265	3.4240645	3.4242281	3.4243915	3.4245550	3.4247183
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282	.4510184	.4511721	.4513258	.4514794	.4516329
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284	.4540823	.4542349	.4543875	.4545400	.4546924
285	.4556061	.4557582	.4559102	.4560622	.4562142
286	.4571246	.4572762	.4574277	.4575791	.4577305
287	.4586378	.4587889	.4589399	.4590908	.4592417
288	.4601458	.4602963	.4604468	.4605972	.4607475
289	3.4616486	3.4617986	3.4619485	3.4620984	3.4622482
290	.4631461	.4632956	.4634450	.4635944	.4637437
291	.4646386	.4647875	.4649364	.4650853	.4652341
292	.4661259	.4662743	.4664227	.4665711	.4667194
293	.4676081	.4677560	.4679039	.4680518	.4681996
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295	.4705575	.4707044	.4708513	.4709982	.4711450

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298	.4742163	.4743620	.4745076	.4746533	.4747988
299	.4756712	.4758164	.4759616	.4761067	.4762518
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303	.4814426	.4815859	.4817292	.4818724	.4820156
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305	.4842998	.4844422	.4845845	.4847268	.4848690
306	.4857214	.4858633	.4860052	.4861470	.4862888
307	.4871384	.4872798	.4874212	.4875626	.4877039
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310	.4913617	.4915018	.4916418	.4917818	.4919217
311	.4927604	.4929000	.4930396	.4931791	.4933186
312	.4941546	.4942938	.4944329	.4945720	.4947110
313	.4955443	.4956831	.4958218	.4959604	.4960990
314	3.4969296	3.4970679	3.4972062	3.4973444	3.4974825
315	.4983106	.4984484	.4985862	.4987240	.4988617
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318	.5024271	.5025637	.5027002	.5028366	.5029731
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321	.5065050	.5066403	.5067755	.5069107	.5070459
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323	.5092025	.5093370	.5094713	.5096057	.5097400
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332	.5211381	.5212689	.5213996	.5215303	.5216610

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337	.5276299	.5277588	.5278876	.5280163	.5281451
338	.5289167	.5290452	.5291736	.5293020	.5294303
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341	.5327544	.5328817	.5330090	.5331363	.5332635
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344	.5365584	.5366847	.5368109	.5369370	.5370631
345	3.5378191	3.5379450	3.5380708	3.5381966	3.5383223
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348	.5415792	.5417040	.5418288	.5419535	.5420781
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351	3.5453071	3.5454308	3.5455545	3.5456781	3.5458017
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358	.5538830	.5540043	.5541256	.5542468	.5543680
359	.5550944	.5552154	.5553362	.5554572	.5555781
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361	.5575072	.5576275	.5577477	.5578680	.5579881
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338	.5295587	.5296869	.5298152	.5299434	.5300716
339	3.5308398	3.5309677	3.5310955	3.5312234	3.5313512
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373	.5717088	.5718252	.5719416	.5720580	.5721743
374	.5728716	.5729877	.5731038	.5732198	.5733358
375	.5740313	.5741471	.5742628	.5743786	.5744943
376	3.5751878	3.5753033	3.5754188	3.5755342	3.5756496
377	.5763413	.5764565	.5765717	.5766868	.5768019
378	.5774917	.5776067	.5777215	.5778363	.5779511
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384	.5843312	.5844443	.5845574	.5846704	.5847834
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386	.5865873	.5866998	.5868123	.5869247	.5870371
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389	.5899496	.5900612	.5901728	.5902844	.5903959
390	.5910646	.5911759	.5912873	.5913985	.5915098
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374	.5734518	.5735678	.5736837	.5737990	.5739154
375	.5746099	.5747256	.5748412	.5749568	.5850723
376	3.5757650	3.5758803	3.5759956	3.5761109	3.5762261
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381	.5814945	.5816084	.5817222	.5818359	.5819497
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390	.5916210	.5917322	.5918434	.5919546	.5920657
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411	.6138418	.6139475	.6140531	.6141587	.6142643
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413	3.6159501	3.6160552	3.6161603	3.6162654	3.6163705
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418	.6211763	.6212802	.6213840	.6214879	.6215917
419	3.6222140	3.6223177	3.6224213	3.6225249	3.6226284
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422	.6253124	.6254153	.6255182	.6256211	.6257239
423	.6263404	.6264430	.6265457	.6266483	.6267509
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426	.6294096	.6295115	.6296134	.6297153	.6298172
427	.6304279	.6305296	.6306312	.6307329	.6308354
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433	.6364879	.6365882	.6366884	.6367887	.6368889
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410	.6133132	.6134189	.6135147	.6136304	.6137361
411	.6143698	.6144754	.6145809	.6146863	.6147918
412	.6154240	.6155292	.6156345	.6157397	.6158449
413	3.6164755	3.6165805	3.6166855	3.6167905	3.6168954
414	.6175245	.6176293	.6177340	.6178387	.6179434
415	.6185710	.6186755	.6187800	.6188845	.6189889
416	.6196150	.6197193	.6198235	.6199277	.6200319
417	.6206565	.6207605	.6208645	.6209684	.6210724
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419	3.6227320	3.6228355	3.6229390	3.6230424	3.6231459
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424	.6178777	.6279800	.6280823	.6281845	.6282867
425	3.6288996	3.6290016	3.6291036	3.6292057	3.6293076
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427	.6309361	.6310377	.6311392	.6312408	.6313423
428	.6319508	.6320522	.6321535	.6322548	.6323560
429	.6329632	.6330643	.6331653	.6332664	.6333674
430	.6339732	.6340740	.6341749	.6342757	.6343765
431	3.6349808	3.6350814	3.6351800	3.6352826	3.6353832
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577	·7611758	·7612511	·7613263	·7614016	·7614768
578	·7619278	·7620030	·7620781	·7621532	·7622283
579	3·7626786	3·7627536	3·7628286	3·7629035	3·7629785
580	·7634280	·7635029	·7635777	·7636526	·7637274
581	·7641761	·7642509	·7643256	·7644003	·7644750
582	·7649230	·7649976	·7650722	·7651468	·7652214
583	·7656686	·7657430	·7658175	·7658920	·7659664
584	·7664128	·7664872	·7665616	·7666359	·7667102
585	3·7671559	3·7672301	3·7673043	3·7673785	3·7674527
586	·7678976	·7679717	·7680458	·7681199	·7681940
587	·7686381	·7687121	·7687860	·7688600	·7689339
588	·7693773	·7694512	·7695250	·7695988	·7696727
589	·7701153	·7701890	·7702627	·7703364	·7704101
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591	·7715875	·7716610	·7717344	·7718079	·7718813

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556	·7454652	·7455432	·7456212	·7456992	·7457772
557	·7462449	·7463228	7464006	·7464785	·7465564
558	·7470232	·7471009	·7471787	·7472564	·7473341
559	·7478001	·7478777	·7479553	·7480329	·7481105
560	·7485756	·7486531	·7487306	·7488080	·7488854
561	3·7493498	3·7494271	3·7495044	3·7495817	3·7496590
562	·7501225	·7501997	·7502769	·7503541	·7504312
563	·7508939	·7509710	·7510480	·7511251	·7512021
564	·7516639	·7517409	·7518178	·7518947	·7519716
565	·7524326	·7525094	·7525862	·7526629	·7527397
566	·7531999	·7532766	·7533532	·7534292	·7535065
567	3·7539659	3·7540424	3·7541189	3·7541954	3·7542719
568	·7547305	·7548069	·7548832	·7549596	·7550359
569	·7554937	·7555700	·7556462	·7557224	·7557987
570	·7562556	·7563318	·7564079	·7564840	·7565600
571	·7570162	·7570922	·7571682	·7572441	·7573201
572	·7577755	·7578513	·7579272	·7580030	·7580788
573	3·7585334	3·7586091	3·7586848	3·7587605	3·7588362
574	·7592900	·7593656	·7594412	·7595168	·7595923
575	·7600453	·7601208	·7601962	·7602717	·7603471
576	·7607993	·7608746	·7609500	·7610253	·7611005
577	·7615520	·7616272	·7617024	·7617775	·7618527
578	·7623034	·7623784	·7624535	·7625285	·7626035
579	3·7630534	3·7631284	3·7632033	3·7632782	3·7633531
580	·7638022	·7638770	·7639518	·7640266	·7641014
581	·7645497	·7646244	·7646991	·7647737	·7648484
582	·7652959	·7653705	·7654450	·7655195	·7655941
583	·7660409	·7661153	·7661897	·7662641	·7663385
584	·7667845	·7668588	·7669331	·7670074	·7670816
585	3·7675269	3·7676011	3·7676752	3·7677494	3·7678235
586	·7682680	·7683421	·7684161	·7684901	·7685641
587	·7690079	·7690818	·7691557	·7692296	·7693035
588	·7697465	·7698203	·7698940	·7699678	·7700416
589	·7704838	·7705575	·7706311	·7707048	·7707784
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591	·7719547	·7720282	·7721016	·7721750	·7722483

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595	.7745170	.7745899	.7746629	.7747359	.7748088
596	.7752463	.7753191	.7753920	.7754648	.7755376
597	.7759743	.7760471	.7761198	.7761925	.7762652
598	3.7767012	3.7767738	3.7768464	3.7769190	3.7769916
599	.7774268	.7774993	.7775718	.7776443	.7777167
600	.7781513	.7782236	.7782960	.7783683	.7784407
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603	.7803173	.7803893	.7804613	.7805333	.7806053
604	3.7810369	3.7811088	3.7811807	3.7812526	3.7813245
605	.7817554	.7818272	.7818989	.7819707	.7820424
606	.7824726	.7825443	.7826159	.7826876	.7827592
607	.7831887	.7832602	.7833318	.7834033	.7834748
608	.7839036	.7839750	.7840464	.7841178	.7841892
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610	3.7853298	3.7854010	3.7854722	3.7855434	3.7856145
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612	.7867514	.7868224	.7868933	.7869643	.7870352
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615	.7888751	.7889457	.7890163	.7890869	.7891575
616	3.7895807	3.7896512	3.7897217	3.7897922	3.7898626
617	.7902852	.7903555	.7904259	.7904663	.7905666
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624	.7951846	.7952542	.7953238	.7953933	.7954629
625	.7958800	.7959495	.7960190	.7960884	.7961578
626	.7965743	.7966437	.7967131	.7967824	.7968517
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596	.7756104	.7756832	.7757560	.7758288	.7759016
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601	.7792356	.7793078	.7793800	.7794522	.7795243
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603	.7806773	.7807492	.7808212	.7808931	.7809650
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605	.7821141	.7821859	.7822576	.7823293	.7824010
606	.7828308	.7829024	.7829740	.7830456	.7831171
607	.7835463	.7836178	.7836892	.7837607	.7838321
608	.7842606	.7843319	.7844033	.7844746	.7845460
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610	3.7856857	3.7857568	3.7858279	3.7858990	3.7859701
611	.7863965	.7864675	.7865385	.7866095	.7866805
612	.7871061	.7871770	.7872479	.7873188	.7873896
613	.7878146	.7878853	.7879561	.7880269	.7880976
614	.7885219	.7885926	.7886632	.7887339	.7888045
615	.7892281	.7892986	.7893691	.7894397	.7895102
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633	.8014037	.8014723	.8015409	.8016095	.8016781
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635	3.8027737	3.8028421	3.8029105	3.8029789	3.8030472
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637	.8041394	.8042076	.8042758	.8043439	.8044121
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633	.8017466	.8018152	.8018837	.8019522	.8020208
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674	.8286599	.8287243	.8287887	.8288532	.8289176
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676	.8299467	.8300109	.8300752	.8301394	.8302036
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690	3.8388491	3.8389120	3.8389750	3.8390379	3.8391008
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694	.8413595	.8414220	.8414846	.8415472	.8416097
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673	.8283376	.8284021	.8284665	.8285310	.8285955
674	.8289820	.8290463	.8291107	.8291751	.8292394
675	.8296254	.8296896	.8297539	.8298182	.8298824
676	.8302678	.8303320	.8303962	.8304603	.8305245
677	.8309093	.8309734	.8310375	.8311016	.8311656
678	3.8315499	3.8316139	3.8316778	3.8317418	3.8318058
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693	.8410465	.8411091	.8411717	.8412343	.8412969
694	.8416722	.8417348	.8417973	.8418598	.8419223
695	.8422971	.8423596	.8424220	.8424844	.8425468
696	3.8429211	3.8429835	3.8430458	3.8431081	3.8431705
697	.8435442	.8436065	.8436687	.8437310	.8434932
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699	.8447877	.8448498	.8449119	.8449739	.8450360
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705	.8481891	.8482507	.8483123	.8483739	.8484355
706	.8488047	.8488662	.8489277	.8489892	.8490507
707	.8494194	.8494808	.8495423	.8496037	.8496651
708	.8500333	.8500946	.8501559	.8502172	.8502786
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710	.8512583	.8513195	.8513807	.8514418	.8515030
711	.8518696	.8519307	.8519917	.8520528	.8521139
712	.8524800	.8525410	.8526020	.8526629	.8527239
713	.8530895	.8531504	.8532113	.8532722	.8533331
714	.8536982	.8537590	.8538198	.8538806	.8539414
715	3.8543060	3.8543668	3.8544275	3.8544882	3.8545489
716	.8549130	.8549737	.8550343	.8550949	.8551556
717	.8555192	.8555797	.8556403	.8557008	.8557614
718	.8561244	.8561849	.8562454	.8563059	.8563663
719	.8567289	.8567893	.8568497	.8569101	.8569704
720	.8573325	.8573928	.8574531	.8575134	.8575737
721	3.8579353	3.8579955	3.8580557	3.8581159	3.8581761
722	.8585372	.8585973	.8586575	.8587176	.8587777
723	.8591383	.8591984	.8592584	.8593185	.8593785
724	.8597386	.8597985	.8598585	.8599185	.8599784
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727	3.8615344	3.8615941	3.8616539	3.8617136	3.8617733
728	.8621314	.8621910	.8622507	.8623103	.8623699
729	.8627275	.8627871	.8628467	.8629062	.8629658
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731	.8639174	.8639768	.8640362	.8640956	.8641550
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735	.8662873	.8663464	.8664055	.8664646	.8665236
736	.8668778	.8669368	.8669958	.8670548	.8671138
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706	.8491122	.8491736	.8492351	.8492956	.8493580
707	.8497264	.8497878	.8498492	.8499106	.8499719
708	.8503399	.8504011	.8504624	.8505237	.8505850
709	3.8509524	3.8510136	3.8510748	3.8511360	3.8511972
710	.8515641	.8516252	.8516863	.8517474	.8518085
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712	.8527849	.8528458	.8529068	.8529677	.8530286
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714	.8540022	.8540630	.8541238	.8541845	.8542453
715	3.8546096	3.8546703	3.8547310	3.8547917	3.8548524
716	.8552162	.8552768	.8553374	.8553980	.8554586
717	.8558219	.8558824	.8559429	.8560035	.8560640
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726	.8612356	.8612954	.8613552	.8614149	.8614747
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742	.8704039	.8704624	.8705209	.8705795	.8706380
743	.8709888	.8710473	.8711057	.8711641	.8712226
744	.8715729	.8716313	.8716897	.8717480	.8718064
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746	3.8727388	3.8727970	3.8728552	3.8729134	3.8729716
747	.8733206	.8733788	.8734369	.8734950	.8735531
748	.8739016	.8739597	.8740177	.8740757	.8741338
749	.8744818	.8745398	.8745978	.8746557	.8747137
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754	.8773713	.8774289	.8774865	.8775441	.8776017
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757	.8790959	.8791532	.8792106	.8792680	.8793253
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764	3.8830934	3.8831502	3.8832070	3.8832639	3.8833207
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746	3.8730298	3.8730880	3.8731461	3.8732043	3.8732625
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780	.8920945	.8921503	.8922059	.8922616	.8923173
781	.8926510	.8927066	.8927622	.8928178	.8928734
782	.8932068	.8932623	.8933178	.8933733	.8934288
783	3.8937618	3.8938172	3.8938727	3.8939281	3.8939836
784	.8943161	.8943715	.8944268	.8944822	.8945376
785	.8948697	.8949250	.8949803	.8950356	.8950909
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787	.8959747	.8960299	.8960851	.8961403	.8961954
788	.8965262	.8965813	.8966364	.8966915	.8967466
789	3.8970770	3.8971320	3.8971871	3.8972421	3.8972971
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804	.9052560	.9053101	.9053641	.9054181	.9054721
805	.9057960	.9058498	.9059038	.9059577	.9060116
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779	.8918161	.8918718	.8919275	.8919832	.8920389
780	.8923729	.8924285	.8924842	.8925398	.8925954
781	.8929290	.8929846	.8930401	.8930957	.8931512
782	.8934843	.8935398	.8935953	.8936508	.8937063
783	3.8940390	3.8940944	3.8941498	3.8942053	3.8942607
784	.8945929	.8946483	.8947037	.8947590	.8948143
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786	.8956987	.8957539	.8958091	.8958643	.8959195
787	.8962506	.8963057	.8963608	.8964160	.8964711
788	.8968017	.8968568	.8969118	.8969669	.8970220
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791	.8984509	.8985058	.8985606	.8986155	.8986703
792	.8989993	.8990541	.8991089	.8991636	.8992184
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818	.9127533	.9128064	.9128595	.9129126	.9129656
819	.9132839	.9133369	.9133899	.9134430	.9134960
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821	.9143432	.9143961	.9144489	.9145018	.9145547
822	.9148718	.9149246	.9149775	.9150303	.9150831
823	.9153998	.9154526	.9155054	.9155581	.9156109
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826	3.9169800	3.9170326	3.9170852	3.9171378	3.9171903
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830	.9190781	.9191304	.9191827	.9192350	.9192873
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832	3.9201233	3.9201755	3.9202277	3.9202799	3.9203321
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834	.9211661	.9212181	.9212702	.9213222	.9213743
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836	.9222063	.9222582	.9223102	.9223621	.9224140
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839	.9237620	.9238137	.9238655	.9239172	.9239690
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843	.9258276	.9258791	.9259306	.9259821	.9260336
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847	.9278834	.9279347	.9279859	.9280372	.9280885
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815	.91142 40	.91147 72	.91153 05	.91158 37	.91163 69
816	.91195 62	.91200 94	.91206 26	.91211 57	.91216 89
817	.91248 78	.91254 09	.91259 40	.91264 71	.91270 02
818	.91301 87	.91307 17	.91312 48	.91317 78	.91323 09
819	.91354 90	.91360 19	.91365 49	.91370 79	.91376 09
820	3.91407 86	3.91413 15	3.91418 44	3.91423 73	3.91429 03
821	.91460 76	.91466 04	.91471 33	.91476 61	.91481 90
822	.91513 59	.91518 87	.91524 15	.91529 43	.91534 71
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829	.91881 64	.91886 87	.91892 11	.91897 34	.91902 58
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972	.9876668	9877109	.9877556	.9878003	.9878449
973	.9881128	.9881575	.9882021	.9882467	.9882913
974	3.9885590	3.9886035	3.9886481	3.9886927	3.9887373
975	.9890046	.9890492	.9890937	.9891382	.9891828
976	.9894498	.9894943	.9895388	.9895833	.9896278
977	.9898946	.9899390	.9899835	.9900279	.9900723
978	.9903389	.9903833	.9904277	.9904721	.9905164
979	.9907827	.9908270	.9908714	.9909158	.9909601
980	3.9912261	3.9912704	3.9913147	3.9913590	3.9914033
981	.9916690	.9917133	.9917575	.9918018	.9918461
982	.9921115	.9921557	.9921999	.9922441	.9922884
983	.9925535	.9925977	.9926419	.9926860	.9927302
984	.9929951	.9930392	.9930834	.9931275	.9931716
985	.9934362	.9934803	.9935244	.9935685	.9936126
986	3.9938769	3.9939210	3.9939650	3.9940090	3.9940531
987	.9943172	.9943612	.9944051	.9944491	.9944931
988	.9947569	.9948009	.9948448	.9948888	.9949327
989	.9951963	.9952402	.9952841	.9953280	.9953719
990	.9956352	.9956791	.9957229	.9957668	.9958106
991	.9960737	.9961175	.9961613	.9962051	.9962489
992	3.9965117	3.9965554	3.9965992	3.9966430	3.9966868
993	.9969492	.9969930	.9970367	.9970804	.9971242
994	.9973864	.9974301	.9974738	.9975174	.9975611
995	.9978231	.9978667	.9979104	.9979540	.9979976
996	.9982593	.9983029	.9983465	.9983901	.9984337
997	.9986952	.9987387	.9987823	.9988258	.9988694
998	.9991305	.9991740	.9992176	.9994611	.9993046
999	.9995655	.9996090	.9996524	.9992959	.9997393

Num	5	6	7	8	9
962	3.9834007	3.9834459	3.9834910	3.9835361	3.9835812
963	.9838517	.9838968	.9839419	.9839869	.9840320
964	.9843022	.9843473	.9843923	.9844373	.9844823
965	.9847523	.9847973	.9848422	.9848872	.9849322
966	.9852019	.9852468	.9852917	.9853366	.9853816
967	.9856510	.9856959	.9857407	.9857856	.9858305
968	3.9860996	3.9861445	3.9861893	3.9862341	3.9862790
969	.9865478	.9865926	.9866374	.9866822	.9867270
970	.9869955	.9870403	.9870850	.9871298	.9871745
971	.9874428	.9874875	.9875321	.9875769	.9876216
972	.9878896	.9879343	.9879789	.9880236	.9880682
973	.9883360	.9883806	.9884252	.9884698	.9885144
974	3.9887818	3.9888264	3.9888710	3.9889155	3.9889601
975	.9892273	.9892718	.9893163	.9893608	.9894053
976	.9896723	.9897167	.9897612	.9898056	.9898501
977	.9901168	.9901612	.9902056	.9902500	.9902944
978	.9905608	.9906052	.9906496	.9906940	.9907383
979	.9910044	.9910488	.9910931	.9911374	.9911818
980	3.9914476	3.9914919	3.9915362	3.9915805	3.9916247
981	.9918903	.9919345	.9919788	.9920230	.9920673
982	.9923326	.9923768	.9924210	.9924651	.9925093
983	.9927744	.9928185	.9928627	.9929068	.9929510
984	.9932157	.9932598	.9933039	.9933480	.9933921
985	.9936566	.9937007	.9937448	.9937888	.9938329
986	3.9940971	3.9941411	3.9941851	3.9942291	3.9942731
987	.9945371	.9945811	.9946251	.9946690	.9947130
988	.9949767	.9950206	.9950645	.9951085	.9951524
989	.9954158	.9954597	.9955036	.9955474	.9955913
990	.9958545	.9958983	.9959422	.9959860	.9960298
991	.9962927	.9963365	.9963803	.9964241	.9964679
992	3.9967303	3.9967743	2.9968180	3.9968618	3.9969055
993	.9971679	.9972116	.9972553	.9972990	.9973427
994	.9976048	.9976485	.9976921	.9977358	.9977794
995	.9980413	.9980849	.9981285	.9981721	.9982157
996	.9984773	.9985209	.9985645	.9986080	.9986516
997	.9989129	.9989564	.9990000	.9990435	.9990870
998	.9993481	.9993916	.9994350	.9994785	.9995220
999	.9997828	.9998262	.9998697	.9999131	.9999566

A

Triangular Canon Logarithmical:

OR,

A TABLE of Artificial SINES, TANGENTS, and SECANTS, the Radius 10.0000000; and to every Degree and Minute of the

QUADRANT.

LONDON, Printed by *John Darby*, for *John Seller*, and *John Wingfield*, 1673.

A Table of Artificial Sines,

0 Degrees.

M	Sine.		Tang		Secant		M
0	0.0000000	10.0000000	0.0000000	Infinite.	10.0000000	Infinite	60
1	6.4637261	9.9999999	6.4637261	13.5362739	10.0000000	13.5362739	59
2	6.7647561	9.9999999	6.7647562	13.2352438	10.0000001	13.2352439	58
3	6.9408473	9.9999998	6.9408475	13.0591525	10.0000002	13.0591527	57
4	7.0657860	9.9999997	7.0657863	12.9342137	10.0000003	12.9342140	56
5	7.1626960	9.9999995	7.1626964	12.8373036	10.0000005	12.8373040	55
6	7.2418771	9.9999993	7.2418778	12.7581222	10.0000007	12.7581229	54
7	7.3088239	9.9999991	7.3088247	12.6911752	10.0000009	12.6911761	53
8	7.3668157	9.9999988	7.3668169	12.6331831	10.0000012	12.6331843	52
9	7.4179681	9.9999985	7.4179696	12.5820304	10.0000015	12.5820319	51
10	7.4637255	9.9999982	7.4637273	12.5362727	10.0000018	12.5362745	50
11	7.5051181	9.9999978	7.5051203	12.4948797	10.0000022	12.4948819	49
12	7.5429065	9.9999974	7.5429091	12.4570909	10.0000026	12.4570935	48
13	7.5776684	9.9999969	7.5776715	12.4223285	10.0000031	12.4223316	47
14	7.6093550	9.9999964	7.6098566	12.3901434	10.0000036	12.3901470	46
15	7.6398160	9.9999959	7.6398201	12.3601799	10.0000041	12.3601840	45
16	7.6678445	9.9999953	7.6678492	12.3321508	10.0000047	12.3321555	44
17	7.6941733	9.9999947	7.6941786	12.3058214	10.0000053	12.3058267	43
18	7.7189966	9.9999940	7.7190026	12.2809974	10.0000060	12.2810034	42
19	7.7424775	9.9999934	7.7424841	12.2575159	10.0000066	12.2575225	41
20	7.7647537	9.9999927	7.7647610	12.2352390	10.0000073	12.2352463	40
21	7.7859427	9.9999919	7.7859508	12.2140492	10.0000081	12.2140573	39
22	7.8061458	9.9999911	7.8061547	12.1938453	10.0000089	12.1938542	38
23	7.8254507	9.9999903	7.8254604	12.1745396	10.0000097	12.1745493	37
24	7.8439338	9.9999894	7.8439444	12.1560556	10.0000106	12.1560662	36
25	7.8616623	9.9999885	7.8616738	12.1383262	10.0000115	12.1383377	35
26	7.8786953	9.9999876	7.8787077	12.1213923	10.0000124	12.1213047	34
27	7.8950854	9.9999866	7.8950988	12.1049012	10.0000134	12.1049146	33
28	7.9108793	9.9999856	7.9108938	12.0891062	10.0000144	12.0891207	32
29	7.9261190	9.9999845	7.9261344	12.0738656	10.0000155	12.0738810	31
30	7.9408419	9.9999835	7.9408584	12.0591416	10.0000165	12.0591581	30
M	Sine.		Tang			Secant	M

89 Degrees.

0 Degrees.

M	Sine.		Tang		Secant		
30	7·9408419	9·9999535	7·9408584	12·0591416	10·0000165	12·0591581	30
31	7·9550819	9·9999423	7·9550996	12·0449004	10·0000177	12·0449181	29
32	7·9688698	9·9999312	7·9688886	12·0311114	10·0000188	12·0311302	28
33	7·9822334	9·9999200	7·9822534	12·0177466	10·0000200	12·0177666	27
34	7·9951980	9·9999788	7·9952192	12·0047808	10·0000212	12·0048020	26
35	8·0077867	9·9999775	8·0078092	11·9921908	10·0000225	11·9922133	25
36	8·0200207	9·9999762	8·0200445	11·9799555	10·0000238	11·9799793	24
37	8·0319195	9·9999748	8·0319446	11·9680554	10·0000252	11·9680805	23
38	8·0435009	9·9999735	8·0435274	11·9564726	10·0000265	11·9564991	22
39	8·0547814	9·9999721	8·0548094	11·9451906	10·0000279	11·9452186	21
40	8·0657763	9·9999706	8·0658057	11·9341943	10·0000294	11·9342237	20
41	8·0764997	9·9999691	8·0765306	11·9234694	10·0000309	11·9235003	19
42	8·0869646	9·9999676	8·0869970	11·9130030	10·0000324	11·9130354	18
43	8·0971832	9·9999660	8·0972172	11·9027828	10·0000340	11·9028168	17
44	8·1071669	9·9999644	8·1072025	11·8927975	10·0000356	11·8928331	16
45	8·1169262	9·9999628	8·1169634	11·8830366	10·0000372	11·8830738	15
46	8·1264710	9·9999611	8·1265099	11·8734901	10·0000389	11·8735290	14
47	8·1358104	9·9999594	8·1358510	11·8641490	10·0000406	11·8641896	13
48	8·1449532	9·9999577	8·1449956	11·8550044	10·0000423	11·8550468	12
49	8·1539075	9·9999559	8·1539516	11·8460484	10·0000441	11·8460925	11
50	8·1626808	9·9999541	8·1627267	11·8372733	10·0000459	11·8373192	10
51	8·1712804	9·9999522	8·1713282	11·8286718	10·0000478	11·8287196	9
52	8·1797129	9·9999503	8·1797626	11·8202374	10·0000497	11·8202871	8
53	8·1879848	9·9999484	8·1880364	11·8119636	10·0000516	11·8120152	7
54	8·1961020	9·9999464	8·1961556	11·8038444	10·0000536	11·8038980	6
55	8·2040703	9·9999444	8·2041259	11·7958741	10·0000556	11·7959297	5
56	8·2118949	9·9999424	8·2119526	11·7880474	10·0000576	11·7881051	4
57	8·2195811	9·9999403	8·2196408	11·7803592	10·00·0597	11·7804189	3
58	8·2271335	9·9999382	8·2271953	11·7728047	10·0000618	11·7728665	2
59	8·2345568	9·9999360	8·2346208	11·7653792	10·0000640	11·7654432	1
60	8·2418553	9·9999338	8·2419215	11·7580785	10·0000662	11·7581447	0
		Sine.		Tang.		Secant	M

89 Degrees.

A Table of Artificial Sines,

1 Degree.

M	Sine.		Tang		Secant		M
0	8.2418553	9 9999338	8.2419215	11.7580785	10.0000661	11 7581447	60
1	8.2490332	9 9999316	8.2491015	11.7508985	10 0000684	11.7509668	59
2	8.2560743	9 9999294	8.2561649	11.7438351	10.0000706	11.7439057	58
3	8.2630424	9.9999271	8 2631153	11.7368847	10.0000729	11.7369576	57
4	8.2698812	9.9999247	8.2699563	11.7300437	10 0000753	11.7301890	56
5	8 2766136	9 9999224	8.2766912	11.7233088	10.0000776	10 7233864	55
6	8.2832434	9 9999200	8.2833234	11.7166766	10 0000800	11.7167566	54
7	8 2897734	6.9999175	8.2898559	11.7101441	10 0000825	11.7102266	53
8	8.2962057	9.9999150	8.2962917	11.7037083	10 0000850	11.7037933	52
9	8.3025460	9.9999125	8.3026335	11 6973665	10.0000875	11.6974540	51
10	8.3087941	9.9999100	8.3088842	11 6911158	10 0000900	11.6912059	50
11	8.3149536	9.9999074	8.3150462	11.6849538	10.0000926	11.6850464	49
12	8.3210269	9.9999047	8.3211221	11.6788779	10.0000953	11.6789731	48
13	8 3270163	9.9999021	8.3271143	11.6728857	10.0000979	11.6729837	47
14	8.3329243	9.9998994	8.3330249	11.6669751	10 0001006	11 6670757	46
15	8.3387529	9.9998966	8.3388563	11.6611437	10.0001034	11 6612471	45
16	8.3445043	9.9998939	8.3446105	11.6553895	10.0001061	11 6554957	44
17	8.3501805	9.9998911	8 3502895	11.6497105	10.0001089	11.6498195	43
18	8 3557835	9.9998882	8 3558953	11 6441047	10.0001118	11.6442165	42
19	8.3613150	9.9998853	8.3614297	11.6385703	10 0001147	11.6386850	41
20	8.3667769	9.9998824	8.3668945	11.6331055	10 0001176	11 6332231	40
21	8.3721710	9.9998794	8.3722915	11.6277085	10.0001206	11.6278190	39
22	8.3774983	9 9998764	8.3776223	11 6223777	10.0001236	11.6225012	38
23	8 3827620	9.9998734	8 3828886	11. 6171114	10.0001266	11.6172380	37
24	8.3879622	9.9998703	8 3880918	11.6119082	10 0001297	11.6120378	36
25	8.3931008	9 9998672	8.3932336	11.6067664	10 0001328	11 6068992	35
26	8.3981793	9 9998641	8.3983152	11.6016848	10.0001359	11 6018207	34
27	8.4031990	9.9998609	8.4033381	11.5966619	10 0001391	11.5968010	33
28	8.4081614	9.9998577	8.4083037	11.5916963	10.0001423	11.5918386	32
29	8.4130676	9.9998544	8.4132132	11.5867868	10.0001456	11.5869324	31
30	8.4179190	9.9998512	8.4180679	11.5819321	10.0001488	11.5820810	30
M		Sine.		Tang.		Secant	M

88 Degrees.

1 Degree.

M	Sine.		Tang		Secant		M
30	8.4179190	9.9998512	8.4182679	11.5819321	10.0001488	11.5820810	30
31	8.4227168	9.9998478	8.4228690	11.5771310	10.0001522	11.5772832	29
32	8.4274621	9.9998445	8.4276176	11.5723824	10.0001555	11.5725379	28
33	8.4321561	9.9998411	8.4323150	11.5676850	10.0001589	11.5678439	27
34	8.4367999	9.9998376	8.4369622	11.5630378	10.0001624	11.5632001	26
35	8.4413949	9.9998342	8.4415603	11.5584397	10.0001658	11.5586056	25
36	8.4459409	9.9998306	8.4461103	11.5538897	10.0001694	11.5540591	24
37	8.4504402	9.9998271	8.4506131	11.5493869	10.0001729	11.5495598	23
38	8.4548934	9.9998235	8.4550693	11.5449201	10.0001765	11.5451066	22
39	8.4593013	9.9998199	8.4594814	11.5405186	10.0001801	11.5406987	21
40	8.4636649	9.9998162	8.4638486	11.5361514	10.0001838	11.5363351	20
41	8.4679850	9.9998125	8.4681725	11.5318275	10.0001875	11.5320150	19
42	8.4722626	9.9998088	8.4724538	11.5275462	10.0001912	11.5277374	18
43	8.4764984	9.9998050	8.4766933	11.5233067	10.0001950	11.5235016	17
44	8.4806932	9.9998012	8.4808920	11.5191080	10.0001988	11.5193068	16
45	8.4848479	9.9997974	8.4850505	11.5149495	10.0002026	11.5151521	15
46	8.4889632	9.9997935	8.4891696	11.5108304	10.0002065	11.5110368	14
47	8.4930398	9.9997896	8.4932502	11.5067498	10.0002104	11.5069602	13
48	8.4970784	9.9997856	8.4972928	11.5027072	10.0002144	11.5029216	12
49	8.5010798	9.9997817	8.5012982	11.4987018	10.0002183	11.4989202	11
50	8.5050447	9.9997776	8.5052672	11.4947329	10.0002224	11.4949553	10
51	8.5089736	9.9997736	8.5092001	11.4907999	10.0002264	11.4910264	9
52	8.5128673	9.9997695	8.5130978	11.4869022	10.0002305	11.4871327	8
53	8.5167264	9.9997653	8.5169610	11.4830387	10.0002347	11.4832736	7
54	8.5205514	9.9997612	8.5207902	11.4792098	10.0002388	11.4794486	6
55	8.5243430	9.9997570	8.5245860	11.4754140	10.0002430	11.4756570	5
56	8.5281017	9.9997527	8.5283490	11.4716510	10.0002473	11.4718983	4
57	8.5318281	9.9997484	8.5320797	11.4679203	10.0002516	11.4681719	3
58	8.5355228	9.9997441	8.5357787	11.4642213	10.0002559	11.4644772	2
59	8.5391863	9.9997398	8.5394466	11.4605534	10.0002602	11.4608137	1
60	8.5428192	9.9997354	8.5432838	11.4569162	10.0002646	11.4571808	0
		Sine.		Tang.		Secant	M

A Table of Artificial Sines,

2 Degrees.

M	Sine.		Tang		Secant		M
0	8 5428192	9·9997354	8 5430838	11·4569162	10 0002646	11 4571808	60
1	8·5464218	9·9997309	8·5466909	11·4533091	10 0002691	11 4535782	59
2	8·5499948	9 9997265	8 5502683	11·4497317	10·0002735	11 4500052	58
3	8·5535386	9·9997220	8 5538166	11·4461834	10 0002780	11 4464614	57
4	8·5570536	9 9997174	8·5573362	11·4426638	10 0002826	11·4429464	56
5	8·5605404	9·9997128	8·5608276	11·4391724	10·0002872	11·4394596	55
6	8·5639994	9·9997082	8·5642912	11·4357088	10·0002918	11·4360006	54
7	8 5674310	9·9997036	8·5677275	11·4322725	10 0002964	11·4325690	53
8	8 5708357	9·9996989	8 5711368	11·4288632	10 0003011	11·4291643	52
9	8·5742139	9 9996942	8·5745197	11 4254803	10 0003058	11·4257861	51
10	8·5775660	9·9996894	8 5778766	11·4221234	10 0003106	11·4224340	50
11	8·5808923	9·9996846	8·5812077	11·4187923	10·0003154	11·4191077	49
12	8 5841933	9·9996798	8·5845136	11·4154864	10·0003202	11·4158067	48
13	8·5874694	9·9996749	8·5877945	11·4122055	10 0003251	11·4125306	47
14	8·5907203	9 9996700	8·5910509	11·4089491	10·0003300	11·4092791	46
15	8·5939483	9·9996650	8·5942832	11·4057168	10 0003350	11·4060517	45
16	8·5971517	9·9996601	8·5974917	11·4025083	10·0003399	11·4028483	44
17	8·6003317	9·9996550	8·6006767	11·3993233	10 0003450	11 3996683	43
18	8·6034886	9·9996500	8·6038386	12·3961614	10·0003500	11·3965114	42
19	8·6066226	9·9996449	8·6069777	11·3930223	10·0003551	11·3933774	41
20	8·6097341	9·9996398	8·6100943	11·3899057	10·0003602	11·3902659	40
21	8·6128235	9·9996346	8·6131889	11·3868111	10·0003654	11·3871765	39
22	8·6158910	9·9996264	8·6162616	11·3837384	10·0003706	11·3841090	38
23	8·6189369	9 9996242	8 6193127	11·3806873	10 0003758	11·3810631	37
24	8·6219616	9·9996189	8·6223427	11·3776573	10·0003811	11·3780384	36
25	8·6249653	9·9996136	8·6253518	11·3746482	10 0003864	11·3750347	35
26	8 6279484	9·9996082	8 6283402	11 3716598	10 0003918	11·3720516	34
27	8·6309111	9 9996028	8·6313083	11·3686917	10·0003972	11·3690889	33
28	8·6338537	9·9995974	8 6342563	11·3657437	10·0004026	11·3661463	32
29	8·6367764	9·9995919	8·6371845	11·3628155	10 0004081	11·3632236	31
30	8·6396795	9·9995865	8·6400931	11·3599059	10·0004135	11·3603204	30
		Sine.		Tang.		Secant	M

87 Degrees.

2 Degrees.

M	Sine.		Tang		Secant		M
30	8.6396796	9 9995865	8.6400931	11.3599069	10.0004135	11.3603204	30
31	8.6425634	9.9995809	8.6429825	11.3570175	10.0004191	11.3574366	29
32	8.6454282	9.9995753	8.6458528	11.3541472	10.0004247	11.3545718	28
33	8.6482742	9.9995697	8.6487044	11.3512956	10.0004303	11.3517258	27
34	8.6511016	9.9995641	8.6515375	11.3484625	10.0004359	11.3488984	26
35	8.6539107	9.9995584	8.6543525	11.3456478	10.0004416	11.3460893	25
36	8.6567017	9.9995527	8.6571490	11.3428510	10.0004473	11.3432983	24
37	8.6594748	9.9995469	8.6599279	11.3400721	10.0004530	11.3405252	23
38	8.6622303	9.9995411	8.6626891	11.3373109	10.0004589	21.3377697	22
39	8.6649684	9.9995353	8.6654331	11.3345669	10.0004647	11.3350316	21
40	8.6676893	9.9995294	8.6681598	11.3318402	10.0004705	11.3323107	20
41	8.6703933	9.9995236	8.6708697	11.3291303	10.0004764	11.3296068	19
42	8.6730804	9.9995176	8.6735628	11.3264372	10.0004824	11.3269196	18
43	8.6757510	9.9995116	8.6762393	11.3237607	10.0004884	11.3242490	17
44	8.6784052	9.9995056	8.6788996	11.3211004	10.0004944	11.3215948	16
45	8.6810433	9.9994996	8.6815437	11.3184563	10.0005004	11.3189567	15
46	8.6836654	9.9994935	8.6841719	11.3158281	10.0005065	11.3163346	14
47	8.6862718	9.9994874	8.6867844	11.3132156	10.0005126	1173137282	13
48	8.6888625	9.9994812	8.6893813	11.3106187	10.0005188	11.3111375	12
49	8.6914379	9.9994750	8.6919629	11.3080371	10.0005250	11.3085621	11
50	8.6939980	9.9994688	8.6945292	11.3054708	10.0005312	11.3060019	10
51	8.6965431	9.9994625	8.6970806	11.3029194	10.0005375	11.3034569	9
52	8.6990734	9.9994562	8.6996172	11.3003828	10.0005438	11.3009266	8
53	8.7015889	9.9994498	8.7021390	11.2978610	10.0005502	11.2984111	7
54	8.7040899	9.9994435	8.7046465	11.2953535	10.0005565	11.2959101	6
55	8.7065766	9.9994370	8.7071395	11.2928605	10.0005630	11.2934234	5
56	8.7090490	9.9994306	8.7096185	11.2903815	10.0005694	11.2909510	4
57	8.7115075	9.9994241	8.7120834	11.2879166	10.0005759	11.2884925	3
58	8.7139520	9.9994176	8.7145345	11.2854655	10.0005824	11.2860480	2
59	8.7163829	9.9994110	8.7169719	11.2830281	10.0005890	11.2836171	1
60	8.7188002	9.9994044	8.7193958	11.2806042	10.0005956	11.2811908	0
		Sine.		Tang.		Secant	M

87 Degrees.

A Table of Artificial Sines,

3 Degrees.

M	Sine.		Tang		Secant		M
0	8·7188022	9·9944344	8·7193956	11·2806042	10 0005956	11·2811938	60
1	8·7212040	9·9993978	8·7218063	11·2781937	10·0026022	11·2787960	59
2	8·7235946	9·9993911	8·7242035	11·2757965	10·0026089	11·2764054	58
3	8·7259721	9·9993844	8·7265877	11·2734123	10·0026156	11·2740279	57
4	8·7283366	9·9993776	8 7289589	11·2710411	10 0026224	11·2716634	56
5	8·7306882	9·99937 8	8·7313174	11·2686826	10 0026292	11·2693118	55
6	8·7330272	9·9993640	8·7336631	11·2663369	10 0026360	11·2669728	54
7	8·7353535	9·9993572	8·7359964	11·2640036	10·0026428	11 2646465	53
8	8·7376675	9·9993503	8·7383172	11. 2616828	10·0026497	11·2623325	52
9	8·7399691	9·9993433	8·7406258	11·2593742	10·0026567	11 2600309	51
10	8·7422586	9 9993364	8·7429222	11 2570778	10·0026636	11·2577414	50
11	8·7445360	9·9993293	8·7452067	11·2547933	10 0026707	11·2554640	49
12	8·7468015	9·9993223	8 7474792	11·2525208	10·0026777	11·2531985	48
13	8 7490553	9·9993152	8 7497400	11 2502600	10·0026848	11·2509447	47
14	8·7512973	9·9993081	8·7519892	11·2480108	10·0026919	11 2487027	46
15	8·7535278	9·9993009	8·7542269	11·2457731	10·0026991	11·2464722	45
16	8·7557469	9·9992938	8·7564531	11·2435469	10·0027060	11·2442531	44
17	8·7579546	9·9992865	8 7586681	11·2413319	10·0027135	11·2420454	43
18	8·7601512	9 9992793	8·7608719	11·2391281	10·0027207	11·2398488	42
19	8 7623366	9 9992720	8·7630647	11·2369353	10 0027280	11·2376634	41
20	8·7645111	9·9992646	8·7652465	11·2347535	10·0027354	11·2354889	40
21	8·7666747	9·9992572	8·7674175	11·2325825	10·0027428	11·2333253	39
22	8·7688275	9·9992498	8·7695777	11·2304223	10·0027502	11·2311723	38
23	8·7709697	9·9992424	8 7717274	11·2282726	10·0027576	11·2290303	37
24	8 7731014	9 9992349	8·7738665	11·2261335	10·0027651	11·2268986	36
25	8·7752226	9 9992274	8·7759952	11 2240048	10·0027726	11·2247774	35
26	8 7773334	9·9992198	8·7781136	11·2218864	10·0027802	11·2226666	34
27	8·7794340	9·9992122	8 7802218	11 2197782	10·0027878	11·2205660	33
28	8·7815244	9 9992046	8·7823199	11·2176801	10·0027954	11·2184756	32
29	8·7836048	9·9991969	8·7844079	11·2155921	10·0028031	11·2163952	31
30	8·7856753	9·9991892	8·7864861	11·2135139	10 0028108	11·2143247	30
		Sine.		Tang.		Secant	M

36 Degrees.

3 Degrees.

M	Sine.		Tang		Secant		M
30	8 7856753	9 9991892	8.7864861	11.2135139	10.0008108	11.2143247	30
31	8.7877359	9.9991815	8.7885544	11.2114456	10.0008185	11.2122641	29
32	8.7897867	9.9991737	8.7906130	11.2093870	10.0008263	11.2102133	28
33	8.7918278	9 9991659	8.7926620	11.2073380	10.0008341	11.2081722	27
34	8.7938594	9 9991580	8.7947014	11.2052986	10.0008420	11.2061406	26
35	8 7958814	9.9991501	8.7967313	11.2032687	10.0008499	11.2041186	25
36	8.7978941	9 9991422	8.7987519	11.2012481	10.0008578	11.2021059	24
37	8.7998974	9.9991342	8 8007632	11.1992368	10 0008658	11.2001026	23
38	8 8018915	9.9991262	8.8027653	11.1972347	10 0008738	11.1981085	22
39	8.8038764	9.9991182	8.8047583	11.1952417	10 0008818	11.1961236	21
40	8.8058523	9.9991101	8.8067422	11.1932578	10 0008899	11.1941477	20
41	8.8078192	9.9991020	8.8087172	11.1912828	10.0008980	11.1921808	19
42	8.8097772	9.9990938	8.8106834	11.1893166	10 0009062	11.1902228	18
43	8.8117264	9.9990856	8.8126407	11.1873593	10.0009144	11.1882736	17
44	8 8136668	9.9990774	8 8145894	11.1854106	10 0009226	11.1863332	16
45	8.8155985	9.9990691	8.8165294	11.1834706	10 0009309	11.1844015	15
46	8 8175217	9.9990608	8.8184608	11.1815392	10.0009392	11.1824783	14
47	8.8194363	9 9990525	8.8203838	11 1796162	10.0009475	11.1805637	13
48	8.8213425	9.9990441	8.8222984	11.1777016	10 0009559	11.1786575	12
49	8.8232404	9.9990357	8 8242046	11.1757954	10.0009643	11.1767596	11
50	8.8251299	9 9990273	8.8261026	11.1738974	10 0009727	11.1748701	10
51	8.8270112	9.9990188	8.8279924	11.1720076	10.0009812	11.1729888	9
52	8.8288844	9.9990103	8.8298741	11.1701259	10 0009897	11.1711156	8
53	8.8307495	9 9990017	8.8317478	11.1682522	10 0009983	11.1692505	7
54	8.8326066	9.9989931	8.8336134	11.1663866	10.0010069	11.1673934	6
55	8.8344557	9 9989845	8.8354712	11 1645288	10.0010155	11.1655443	5
56	8.8362969	9.9989758	8.8373211	11.1626789	10.0010242	11.1637031	4
57	8.8381304	9.9989671	8.8391633	11.1608367	10.0010329	11.1618696	3
58	8.8399561	9.9989584	8.8409977	11.1590023	10.0010416	11.1600439	2
59	8.8417741	9.9989496	8.8428245	11.1571755	10.0010504	11.1582259	1
60	8.8435845	9.9989408	8.8446437	11.1553563	10.0010592	11.1564155	0
M		Sine.		Tang.		Secant	M

86 Degrees.

A Table of Artificial Sines,

4 Degrees.

M	Sine.		Tang		Secant		M
0	8.8435845	9.9989428	8.8446437	11.1553563	10.0010572	11.1564155	60
1	8.8453874	9.9989319	8.8464554	11.1535446	10.0010681	11.1546126	59
2	8.8471827	9.9989230	8.8482597	11.1517403	10.0010770	11.1528173	58
3	8.8489707	9.9989141	8.8500566	11.1499434	10.0010859	11.1510293	57
4	8.8507512	9.9989052	8.8518461	11.1481539	10.0010948	11.1492488	56
5	8.8525245	9.9988962	8.8536283	11.1463717	10.0011038	11.1474755	55
6	8.8542905	9.9988871	8.8554034	11.1445966	10.0011129	11.1457095	54
7	8.8560493	9.9988780	8.8571713	11.1428287	10.0011220	11.1439507	53
8	8.8578010	9.9988689	8.8589321	11.1410679	10.0011311	11.1421990	52
9	8.8595457	9.9988598	8.8606859	11.1393141	10.0011402	11.1404543	51
10	8.8612833	9.9988506	8.8624327	11.1375673	10.0011494	11.1387167	50
11	8.8630139	9.9988414	8.8641725	11.1358275	10.0011586	11.1369861	49
12	8.8647376	9.9988321	8.8659055	11.1340945	10.0011679	11.1352624	48
13	8.8664545	9.9988228	8.8676317	11.1323683	10.0011772	11.1335455	47
14	8.8681646	9.9988135	8.8693511	11.1306489	10.0011865	11.1318354	46
15	8.8698680	9.9988041	8.8710638	11.1289362	10.0011959	11.1301320	45
16	8.8715646	9.9987947	8.8727699	11.1272301	10.0012053	11.1284354	44
17	8.8732546	9.9987853	8.8744694	11.1255306	10.0012147	11.1267454	43
18	8.8749381	9.9987758	8.8761623	11.1238377	10.0012242	11.1250619	42
19	8.8766150	9.9987663	8.8778487	11.1221513	10.0012337	11.1233850	41
20	8.8782854	9.9987567	8.8795286	11.1204714	10.0012433	11.1217146	40
21	8.8799493	9.9987471	8.8812022	11.1187978	10.0012529	11.1200507	39
22	8.8816069	9.9987375	8.8828694	11.1171306	10.0012625	11.1183931	38
23	8.8832581	9.9987278	8.8845303	11.1154697	10.0012722	11.1167419	37
24	8.8849031	9.9987181	8.8861850	11.1138150	10.0012819	11.1150969	36
25	8.8865418	9.9987084	8.8878334	11.1121666	10.0012916	11.1134582	35
26	8.8881743	9.9986986	8.8894757	11.1105243	10.0013014	11.1118257	34
27	8.8898007	9.9986888	8.8911119	11.1088881	10.0013112	11.1101993	33
28	8.8914209	9.9986790	8.8927420	11.1072580	10.0013210	11.1085791	32
29	8.8930351	9.9986691	8.8943660	11.1056340	10.0013309	11.1069649	31
30	8.8946433	9.9986591	8.8959842	11.1040158	10.0013409	11.1053567	30
		Sine.		Tang		Secant	

85 Degrees.

4 Degrees.

M	Sine.		Tang		Secant		
30	8.8946433	9.9986591	8.8959843	11.1040158	10.0013409	11.1053567	30
31	8.8962455	9.9986492	8.8975962	11.1024 37	10.0013508	11.1037545	29
32	8.8978418	9 9986392	8.8992026	11.1007974	10.0013608	11.1021582	28
33	8.8994322	9.9986292	8.9008030	11.0991970	10 0013708	11.1005678	27
34	8.9010168	9.9986191	8 9023977	11.0976023	10.0013809	11.0989332	26
35	8.9025955	9.9986090	8 9039866	11.0960134	10.0013910	11 0974245	25
36	8.9041685	9.9985988	8.9055697	11.0944303	10.0014012	11.0958315	24
37	8.9057358	9.9985886	8.9071472	11.0928528	10 0014014	11.0942642	23
38	8.9072975	9.9985784	8.9087190	11 0912810	10.0014216	10.0927025	22
39	8.9088535	9.9985682	8.9102853	11.0897147	10.0014318	11.0911465	21
40	8.9104039	9.9985579	8.9118460	11.0881540	10 0014421	11.0895961	20
41	8 9119487	9.9985475	8.9134012	11.0865988	10.0014525	11.0880513	19
42	8.9134881	9.9985372	8.9149509	11.0850491	10 0014628	11.0865119	18
43	8.9150219	9 9985268	8.9164952	11.0835048	10 0014732	11.0849781	17
44	8.9165504	9.9985163	8.9180340	11.0819660	10.0014837	11.0834496	16
45	8.9180734	9.9985058	8.9195675	11.0804325	10.0014942	11.0819266	15
46	8.9195911	9.9984953	8.9210957	11.0789043	10.0025047	11 0804089	14
47	8.9211034	9.9984848	8.9226186	11.0773814	10.0015152	11.0788966	13
48	8.9226105	9.9984742	8.9241363	11.0758637	10.0015258	11.0773895	12
49	8.9241123	9.9984636	8.9256487	11.0743513	10 0015364	11 0758877	11
50	8 9256089	9.9984529	8.9271560	11.0728440	10.0015471	11.0743911	10
51	8.9271003	9.9984422	8.9286581	11.0713419	10.0015578	11.0728997	9
52	8.9285866	9 9984315	8.9301552	11.0698448	10.0015685	11.0714134	8
53	8.9300678	9.9984207	8.9316471	11.0683529	10.0015793	11.0699322	7
54	8.9315439	9.9984099	8.9331340	11.0668660	10.0015901	11.0684561	6
55	8.9330150	9.9983990	8.9346160	11.0653840	10.0016010	11.0669850	5
56	8 9344811	9.9983881	8.9360929	11.0639071	10 0016119	11.0655189	4
57	8.9359422	9.9983772	8 9375650	11.0624350	10 0016228	11.0640578	3
58	8.9373983	9.9983663	8.9390321	11.0609679	10.0016337	11.0626017	2
59	8.9388496	9 9983553	8 9404944	11.0595056	10.0016447	11.0611504	1
60	8.9402960	9.9983442	8.9419518	11.0580482	10.0016558	11.0597040	0
		Sine.		Tang.		Secant	M

85 Degrees.

A Table of Artificial Sines,

5 Degrees.

M	Sine.		Tang		Secant		M
0	8 9420960	9 9983442	8·9419518	11·0580482	10 0016558	11·0597040	60
1	8·9417376	9·9983332	8·9434044	11·0565956	10·0016668	11·0582624	59
2	8·9413743	9 9983220	8·9448523	11 0551477	10·0016780	11·0568257	58
3	8·9410063	9 9983109	8·9462954	11·0537046	10·0016891	11·0553937	57
4	8·9406335	9·9982997	8·9477338	11·0522662	10·0017003	11·0539665	56
5	8·9474561	9·9982885	8·9491676	11·0508324	10·0017115	11·0525439	55
6	8·9488739	9·9982772	8·9505967	11·0494033	10·0017228	11·0511261	54
7	8·9502871	9 9982660	8·9520211	11·0479789	10·0017340	11·0497129	53
8	8·9516957	9·9982546	8 9534410	11 0465590	10 0017454	11·0483043	52
9	8·9530996	9·9982433	8 9548564	11·0451436	10·0017567	11 0469004	51
10	8 9544991	9·9982318	8·9562672	11.0437328	10·0017682	11·0455009	50
11	8 9558940	9·9982204	8 9576735	11·0423265	10·0017796	11·0441060	49
12	8·9572843	9 9982089	8·9590754	11·0409246	10·0017911	11·0427157	48
13	8·9586705	9·9981974	8·9604728	11·0395272	10·0018026	11·0413297	47
14	8·9600517	9 9981859	8·9618659	11·0381341	10.0018141	11·0399483	46
15	8·9614288	9·9981742	8·9632545	11·0367455	10·0018257	11·0385712	45
16	8·9628014	9·9981626	8·9646386	11.0353612	10.0018371	11·0371986	44
17	8·9641697	9·9981510	8·9660188	11·0339812	10·0018490	11·0358303	43
18	8 9655337	8·9981393	8·9673944	11·0326056	10·0018607	11·0344663	42
19	8·9668934	9·9981275	8·9687658	11 0312342	10·0018725	11·0331066	41
20	8 9682487	9·9981158	8·9701330	11·0298670	10·0018842	11·0317513	40
21	8·9695993	9 9981040	8·9714959	11.0285041	10 0018960	11·0304001	39
22	8·9709468	9 9980921	8·9728547	11·0271453	10·0019079	11·0290532	38
23	8·9722895	9·9980802	8 9742092	11·0257908	10·0019198	11·0277105	37
24	8·9736280	9 9980683	8·9755597	11·0244403	10·0019317	11·0263720	36
25	8 9749624	9·9980563	8·9769060	11 0230940	10·0019437	11·0250376	35
26	8 9762926	9 9980443	8·9782483	11 0217517	10 0019557	11·0237074	34
27	8·9776188	9·9980323	8·9795865	11·0104135	10·0019677	11·0223812	33
28	8·9789408	9·9980202	8·9809206	11·0190794	10·0019798	11·0210592	32
29	8 9802589	9 9980081	8·9822507	11·0177493	10·0019919	11·0197411	31
30	8 9815729	9 9979960	8·9835769	11·0164231	10·0020040	11·0184271	30
M		Sine.		Tang.		Secant	M

84 Degrees.

5 Degrees.

M	Sine.		Tang		Secant		M
30	8·9815729	9·9979960	8·9835769	11·0164231	10·0020040	11·0184271	30
31	8·9828819	9 9979838	8·9848991	11·0151009	10.0020162	11·0171171	29
32	8·9841889	9·9979716	8·9862173	11·0137827	10.0020284	11 0158111	28
33	8·9854910	9·9979594	8·9875317	11·0124683	10.0020407	11·0145090	27
34	8·9867891	9 9979470	8·9888421	11 0111579	10.0020530	11·0132109	26
35	8·9880834	9·9979347	8·9901487	11·0098513	10.0020653	11·0119165	25
36	8·9893737	9·9979223	8·9914514	11·0085489	10·0020777	11·0106263	24
37	8·9906602	9·9979099	8·9927503	11·0072497	10 0020901	11·0093398	23
38	8·9919429	9·9978975	8 9940454	11·0059546	10·0021025	11·0080572	22
39	8·9932217	9·9978850	8·9953367	11·0046633	10·0021150	11 0067783	21
40	8·9944968	9·9978725	8·9966243	11·0033757	10·0021275	11·0055032	20
41	8·9957681	9·9978599	8·9979081	11·0020919	10·0021410	11 0042319	19
42	8·9970356	9 9978473	8 9991883	11·0008117	10 0021527	11 0029644	18
43	8·9982994	9·9978347	9·0004647	10 9995353	10 0021653	11·0017006	17
44	8·9995595	9·9978220	9·0017375	10·9982625	10·0021780	11·0004405	16
45	9·0008160	9 9978093	9·0030066	10·9969934	10·0021907	10 9991840	15
46	9·0020687	9·9977966	9·0042721	10·9957279	10 0022034	10·9979313	14
47	9 0033179	9 9977838	9 0055340	10·9944660	10·0022162	10·9966821	13
48	9·0045634	9·9977710	9·0067924	10·9932076	10 0022290	10·9954366	12
49	9·0058053	9 9977582	9·0080471	10·9919529	10·0022418	10·9941947	11
50	9 0070436	9·9977453	9 0092984	10·9907016	10 0022547	10·9929564	10
51	9·0082784	9·9977323	9·0105461	10·9894539	10·0022677	10·9917216	9
52	9 0095096	9·9977194	9 0117903	10 9882097	10·0022806	10·9904904	8
53	9·0107374	9 9977064	9·0130310	10·9869690	10 0022936	10·9892626	7
54	9·0119616	9·9976933	9·0142682	10 9857318	10 0023067	10 9880384	6
55	9·0131823	9 9976803	9·0155021	10·9844979	10·0023197	10·9868177	5
56	9 0143996	9·9976672	9·0167325	10·9832675	10 0023328	10·9856004	4
57	9 0156135	9·9976540	9·0179594	10·9820406	10·0023460	10·9843865	3
58	9·0168238	9·9976408	9·0191831	10 9808169	10·0023592	10·9831761	2
59	9·0180309	9·9976276	9·0204033	10 9795967	10 0023724	10·9819691	1
60	9·0192346	9·9976143	9 0216202	10 97837·8	10·0023857	10·9807654	0
		Sine.		Tang.		Secant	M

84 Degrees.

A Table of Artificial Sines,

6 Degrees.

M	Sine.		Tang		Secant		M
0	9.0192346	9.9976143	9.0216202	10 9783798	10.0023857	10 9807654	60
1	9.0204348	9.9976011	9 0228338	10.9771662	10.0023989	10 9795652	59
2	9.0216318	9.9975877	9 0240441	10.9759559	10 0024123	10 9783682	58
3	9.0228254	9.9975743	9 0252510	10.9747490	10.0024257	10 9771746	57
4	9.0240157	9.9975609	9.0264548	10.9735452	10.0024391	10 9759843	56
5	9.0252027	9.9975475	9 0276552	10.9723448	10.0024525	10.9747973	55
6	9.0263865	9.9975340	9.0288524	10.9711476	10 0024660	10.9736135	54
7	9.0275669	9.9975205	9.0300464	10.9699536	10.0024795	10.9724331	53
8	9.0287442	9.9975069	9 0312373	10.9687627	10 0024931	10.9712558	52
9	9 0299182	9.9974933	9.0324249	10.9675751	10.0025067	10.9700818	51
10	9.0310890	9.9974797	9.0336093	10.9663907	10 0025203	10.9689110	50
11	9.0322567	9.9974660	9 0347906	10.9652094	10.0025340	10.9677433	49
12	9.0334212	9.9974523	9.0359688	10.9640312	10.0025477	10.9665788	48
13	9.0345825	9.9974386	9.0371439	10 9628561	10.0025614	10 9654175	47
14	9 0357407	9.9974248	9 0383159	10.9616841	10.0025752	10.964 593	46
15	9.0368958	9.9974110	9.0394848	10.9605152	10.0025890	10 9631042	45
16	9.0380477	9.9973971	9.0406506	10.9593494	10.0026029	10.9619523	44
17	9.0391966	9 9973833	9.0418134	10.9581866	10.0026167	10 9608034	43
18	9.0403424	9.9973693	9.0429731	10 9570269	10 0026307	10 9596576	42
19	9.0414852	9.9973554	9 0441299	10.9558701	10.0026446	10 9585148	41
20	9.0426249	9.9973414	9.0452836	10.9547164	10 0026586	10.9573751	40
21	9.0437617	9.9973273	9.0464643	10.9535657	10.0026727	10.9562383	39
22	9 0448954	9.9973132	9 0475821	10.9524179	10.0026868	10.9551046	38
23	9.0460261	9 9972991	9.0487270	10.9512730	10.0027009	10.9539739	37
24	9.0471538	9.9972850	9 0498689	10.9501311	10.0027150	10.9528462	36
25	9 0482786	9.9972708	9.0510078	10.9489922	10.0027292	10.9517214	35
26	9 0491005	9 9972566	9.0521439	10.9478561	10.0027434	10.9505995	34
27	9 0505194	9.9972423	9.0532771	10.9467229	10.0027577	10.9494806	33
28	9.0516354	9.9972280	9.0544074	10.9455926	10.0027720	10.9483646	32
29	9.0527485	9.9972137	9.0555349	10.9444651	10.0027863	10.9472515	31
30	9 0538588	9.9971993	9.0566595	10.9433405	10.0028007	10.9461412	30
		Sine.		Tang.		Secant	M

83 Degrees.

6 Degrees.

M	Sine.		Tang		S. ca		M
30	8·0538588	9·9971993	9 0566595	10·0433405	10·0028007	10·0461412	30
31	9·0549661	9 9971849	9·0577813	10 0422187	10·0028151	10·0450339	29
32	9 0560706	9·9971704	9·0589002	10·0410998	10·0028296	10·0439294	28
33	9·0571723	9·9971559	9·0600164	10 0399836	10·0028441	10 0428277	27
34	9·0582711	9 9971414	9 0611297	10·0388703	10·0028586	10·0417289	26
35	9·0593672	9·9971268	9 0622403	10 0377597	10·0028732	10·0406328	25
36	9 0604604	9 9971122	9·0633482	10·0366518	10·0028878	10 0395496	24
37	9·0615509	9 9970976	9·0644533	10·0355467	10·0029024	10·0384491	23
38	9·0626386	9·9970829	9·0655556	10·0344444	10·0029171	10·0373614	22
39	9 0637235	9·9970682	9 0666553	10 0333447	10 0029318	10·0362765	21
40	9·0648057	9 9970535	9·0677522	10·0322478	10 0029465	10·0351943	20
41	9 0658852	9·9970387	9 0688465	10·0311535	10·0029613	10·0341148	19
42	9·0669619	9·9970239	9·0699381	10·0300619	10·0029761	10·0330381	18
43	9 0680360	9·9970090	9·0710270	10·0289730	10·0029910	10 0319640	17
44	9·0691074	9·9969941	9·0721133	10·0278867	10·0030059	10 0308926	16
45	9 0701761	9·9969792	9·0731969	10 0268031	10 0030208	10·0298239	15
46	9·0712421	9·9969642	9·0742779	10·0257221	10·0030358	10·0287579	14
47	9·0723055	9 9969482	9·0753563	10 0246437	10·0030508	10 0276945	13
48	9·0733663	9·9969342	9 0764321	10·0235679	10·0030658	10 0266337	12
49	9·0744244	9·9969191	9·0775053	10·0224947	10·0030809	10·0255756	11
50	9·0754799	9·9969040	6 0785760	10 0214240	10·0030960	10·0245201	10
51	9 0765329	9·9968888	9·0796441	10·0203559	10·0031112	10·0234671	9
52	9·0775832	9·9968736	9·0807096	10·0192904	10·0031264	10·0224168	8
53	9·0786310	9·9968584	9 0817726	10·0182274	10 0031416	10·0213690	7
54	9·0796762	9·9968431	9 0828341	10·0171659	10·0031569	10 0203238	6
55	9·0807189	9·9968278	9 0838911	10·0161089	10·0031722	10 0192811	5
56	9·0817590	9·9968125	9·0849466	10·0150534	10 0031875	10·0182410	4
57	9 0827966	9·9967971	9·0859996	10·0140004	10·0032029	10·0172034	3
58	9·0838317	9·9967817	9 0870501	10·0129499	10·0032183	10·0161683	2
59	9·0848643	9·9967662	9·0880981	10·0119019	10·0032338	10·0151357	1
60	9·0858945	9·9967507	9·0891438	10·0108562	10·0032493	10 0141055	0
		Sine.		Tang.		Secant	M

83 Degrees.

A Table of Artificial Sines,

7 Degrees.

M	Sine		Tang		Secant		
0	9.0358945	9.9967507	9.0891438	10.9108562	10.0032493	10.9141055	60
1	9.0369221	9.9967352	9.0901869	10.9098131	10.0032648	10.9137779	59
2	9.0379473	9.9967196	9.0912277	10.9087723	10.0032804	10.9120527	58
3	9.0389700	9.9967040	9.0922660	10.9077340	10.0032960	10.9110300	57
4	9.0399903	9.9966884	9.0933020	10.9066980	10.0033116	10.9100097	56
5	9.0410082	9.9966727	9.0943355	10.9056645	10.0033273	10.9089918	55
6	9.0420237	9.9966570	9.0953667	10.9046333	10.0033430	10.9079763	54
7	9.0430367	9.9966412	9.0963955	10.9036045	10.0033588	10.9069633	53
8	9.0440474	9.9966254	9.0974219	10.9025781	10.0033746	10.9059526	52
9	9.0450556	9.9966096	9.0984460	10.9015540	10.0033904	10.9049444	51
10	9.0460615	9.9965937	9.0994678	10.9005322	10.0034063	10.9039385	50
11	9.0470651	9.9965778	9.1004872	10.8995128	10.0034222	10.9029349	49
12	9.0480662	9.9965619	9.1015044	10.8984956	10.0034381	10.9019338	48
13	9.0490651	9.9965459	9.1025192	10.8974808	10.0034541	10.9009349	47
14	9.0500616	9.9965299	9.1035317	10.8964683	10.0034701	10.8999384	46
15	9.0510558	9.9965138	9.1045420	10.8954580	10.0034862	10.8989442	45
16	9.0520477	9.9964977	9.1055500	10.8944500	10.0035023	10.8979523	44
17	9.0530373	9.9964816	9.1065557	10.8934443	10.0035184	10.8969627	43
18	9.0540246	9.9964655	9.1075591	10.8924409	10.0035345	10.8959754	42
19	9.0550096	9.9964493	9.1085604	10.8914396	10.0035507	10.8949904	41
20	9.0559924	9.9964330	9.1095594	10.8904406	10.0035670	10.8940076	40
21	9.0569729	9.9964167	9.1105562	10.8894438	10.0035833	10.8930271	39
22	9.0579512	9.9964004	9.1115508	10.8884492	10.0035996	10.8920488	38
23	9.0589272	9.9963841	9.1125431	10.8874569	10.0036159	10.8910728	37
24	9.0599010	9.9963677	9.1135333	10.8864667	10.0036323	10.8900990	36
25	9.0608726	9.9963513	9.1145213	10.8854787	10.0036487	10.8891274	35
26	9.0618420	9.9963348	9.1155072	10.8844298	10.0036652	10.8881580	34
27	9.0628092	9.9963183	9.1164909	10.8835091	10.0036817	10.8871908	33
28	9.0637742	9.9963018	9.1174724	10.8825176	10.0036982	10.8862258	32
29	9.0647370	9.9962852	9.1184518	10.8815482	10.0037148	10.8852630	31
30	9.0656977	9.9962686	9.1194291	10.8805709	10.0037314	10.8843023	30
M		Sine.		Tang		Secant	M

82 Degrees.

7 Degrees.

M	Sine.		Tang		Secant		
30	9 1156977	9 9362686	9 1194291	10 8805709	10 0237314	10 8843023	30
31	9 1165562	9 9362519	9 1204043	10 8795957	10 0237431	10 8833428	29
32	9 1176125	9 9362352	9 1213773	10 8786227	10 0237548	10 8823875	28
33	9 1185667	9 9362185	9 1223482	10 8776518	10 0237815	10 8814333	27
34	9 1195188	9 9362017	9 1223371	10 8766629	10 0237983	10 8804812	26
35	9 1204683	9 9361849	9 1242839	10 8757161	10 0238151	10 8795312	25
36	9 1214167	9 9361681	9 1252486	10 8747514	10 0238319	10 8785833	24
37	9 1223624	9 9361512	9 1262212	10 8737888	10 0238488	10 8776376	23
38	9 1233061	9 9361343	9 1271718	10 8728282	10 0238657	10 8766939	22
39	9 1242477	9 9361174	9 1281303	10 8718697	10 0238826	10 8757523	21
40	9 1251872	9 9361004	9 1290868	10 8709132	10 0238996	10 8748128	20
41	9 1261246	9 9360834	9 1300413	10 8699587	10 0239166	10 8738754	19
42	9 1270600	9 9360663	9 1309917	10 8690063	10 0239337	10 8729400	18
43	9 1279934	9 9360492	9 1319442	10 8680558	10 0239508	10 8720066	17
44	9 1289247	9 9360321	9 1328926	10 8671074	10 0239697	10 8710753	16
45	9 1298539	9 9360149	9 1338390	10 8661609	10 0239851	10 8701451	15
46	9 1307812	9 9359977	9 1347835	10 8652165	10 0240023	10 8692188	14
47	9 1317064	9 9359804	9 1357260	10 8642740	10 0240196	10 8682936	13
48	9 1326297	9 9359631	9 1366665	10 8633335	10 0240369	10 8673703	12
49	9 1335509	9 9359458	9 1376051	10 8623949	10 0240542	10 8664491	11
50	9 1344702	9 9359284	9 1385417	10 8614583	10 0240716	10 8655278	10
51	9 1353875	9 9359111	9 1394764	10 8605236	10 0240889	10 8646125	9
52	9 1363028	9 9358936	9 1404092	10 8595908	10 0241064	10 8636972	8
53	9 1372161	9 9358761	9 1413400	10 8586600	10 0241239	10 8627839	7
54	9 1381275	9 9358586	9 1422689	10 8577311	10 0241414	10 8618725	6
55	9 1390370	9 9358411	9 1431959	10 8568041	10 0241589	10 8609630	5
56	9 1399445	9 9358235	9 1441210	10 8558790	10 0241765	10 8600555	4
57	9 1408501	9 9358059	9 1450442	10 8549558	10 0241941	10 8591499	3
58	9 1417537	9 9357882	9 1459655	10 8540345	10 0242118	10 8582463	2
59	9 1426555	9 9357705	9 1468850	10 8531150	10 0242295	10 8573445	1
60	9 1435553	9 9357528	9 1478025	10 8521975	10 0242472	10 8564447	0
M		Sine.		Tang.		Secant	M

82 Degrees.

A Table of Artificial Sines,

8 Degrees.

M	Sine.		Tang		Secant		M
0	9·1435553	9·9957528	9·1478025	10 8521975	10·0042472	10·8564447	60
1	9·1444532	9·9957350	9·1487182	10·8512818	10·0042650	10·8555468	59
2	9·1453493	9 9957172	9·1496321	10·8503679	10·0042828	10·8546507	58
3	9·1462435	9·9956993	9·1505441	10·8494559	10·0043007	10·8537565	57
4	9 1471358	9·9956815	9 1514543	10·8485457	10·0043185	10·8528642	56
5	9 1480262	9·9956635	9·1523627	10·8476373	10·0043365	10 8519738	55
6	9·1489148	9·9956456	9·1532692	10·8467308	10 0043544	10·8510852	54
7	9·1498015	9·9956276	9·1541739	10·8458261	10·0043724	10 8501985	53
8	9·1506864	9·9956095	9 1550769	10 8449231	10·0043905	10·8493136	52
9	9·1515694	9·9955915	9·1559780	10 8440220	10·0044085	10·8484306	51
10	9·1524507	9·9955734	9 1568873	10 8431227	10 0044266	10·8475493	50
11	9·1533301	9 9955552	9 1577748	10·8422252	10·0044448	10·8466699	49
12	9·1542076	9·9955370	9·1586706	10 8413294	10·0044630	10·8457924	48
13	9·1550834	9·9955188	9·1595646	10·8404354	10·0044812	10·8449166	47
14	9·1559574	9·9955005	9·1604569	10·8395431	10 0044995	10·8440426	46
15	9·1568296	9·9954822	9·1613473	10·8386527	10·0045178	10·8431704	45
16	9·1577000	9·9954639	9·1622361	10·8377639	10.0045361	10·8423000	44
17	9 1585686	9·9954455	9·1631231	10·8368769	10·0045545	10·8414314	43
18	9·1594354	9·9954271	9·1640083	10·8359917	10·0045729	10·8405646	42
19	9·1603005	9·9954087	9 1648919	10·8351081	10·0045913	10·8396995	41
20	9·1611639	9 9953902	9·1657737	10·8342263	10.0046098	10·8388361	40
21	9·1620254	9 9953717	9·1666538	10 8333462	10·0046283	10·8379745	39
22	9·1628853	9·9953531	9·1675322	10·8324678	10·0046469	10 8371147	38
23	9·1637434	9 9953345	9·1684089	10·8315911	10 0046655	10·8362566	37
24	9·1645998	9·9953159	9·1692839	10·8307161	10·0046841	10·8354002	36
25	9·1654544	9·9952972	9·1701572	10·8298428	10.0047028	10 8345456	35
26	9·1663074	9·9952785	9·1710289	10·8289711	10 0047215	10·8336926	34
27	9·1671586	9·9952597	9·1718989	10·8281011	10·0047403	10·8328414	33
28	9·1680082	9·9952409	9·1727672	10·8272328	10·0047591	10·8319919	32
29	9·1688559	9·9952221	9·1736338	10·8263662	10.0047779	10·8311441	31
30	9·1697021	9·9952033	9·1744988	10·8255012	10·0047967	10·8302979	30
M		Sine.		Tang		Secant	M

81 Degrees.

8 Degrees.

M	Sine.		Tang		Secant		
30	9.1697021	9.9952033	9.1744985	10.8255012	10.0047967	10.8302979	30
31	9.1705465	9.9951844	9.1753622	10.8246378	10.0048156	10.8294534	29
32	9.1713803	9.9951654	9.1762239	10.8237761	10.0048346	10.8286107	28
33	9.1722035	9.9951464	9.1770840	10.8229160	10.0048536	10.8277695	27
34	9.1730099	9.9951274	9.1779425	10.8220575	10.0048726	10.8269301	26
35	9.1739077	9.9951084	9.1787993	10.8212007	10.0048916	10.8260923	25
36	9.1747439	9.9950893	9.1796546	10.8203454	10.0049107	10.8252561	24
37	9.1755784	9.9950702	9.1805082	10.8194918	10.0049298	10.8244216	23
38	9.1764112	9.9950510	9.1813602	10.8186398	10.0049490	10.8235888	22
39	9.1772425	9.9950318	9.1822106	10.8177894	10.0049682	10.8227575	21
40	9.1780721	9.9950126	9.1830595	10.8169405	10.0049874	10.8219279	20
41	9.1789001	9.9949933	9.1839068	10.8160932	10.0050067	10.8210999	19
42	9.1797265	9.9949742	9.1847525	10.8152475	10.0050260	10.8202735	18
43	9.1805512	9.9949546	9.1855966	10.8144034	10.0050454	10.8194488	17
44	9.1813744	9.9949352	9.1864392	10.8135608	10.0050648	10.8186256	16
45	9.1821960	9.9949158	9.1872802	10.8127198	10.0050842	10.8178040	15
46	9.1830160	9.9948964	9.1881196	10.8118804	10.0051036	10.8169838	14
47	9.1838344	9.9948769	9.1889575	10.8110425	10.0051231	10.8161656	13
48	9.1846512	9.9948573	9.1897939	10.8102061	10.0051427	10.8153488	12
49	9.1854665	9.9948377	9.1906287	10.8093713	10.0051623	10.8145335	11
50	9.1862802	9.9948181	9.1914621	10.8085379	10.0051819	10.8137199	10
51	9.1870923	9.9947985	9.1922939	10.8077061	10.0052015	10.8129077	9
52	9.1879029	9.9947788	9.1931241	10.8068759	10.0052212	10.8120971	8
53	9.1887120	9.9947591	9.1939529	10.8060471	10.0052409	10.8112880	7
54	9.1895195	9.9947393	9.1947802	10.8052198	10.0052607	10.8104805	6
55	9.1903254	9.9947193	9.1956059	10.8043941	10.0052805	10.8096746	5
56	9.1911299	9.9946997	9.1964302	10.8035698	10.0053003	10.8088701	4
57	9.1919328	9.9946798	9.1972530	10.8027470	10.0053202	10.8080672	3
58	9.1927342	9.9946599	9.1980743	10.8019257	10.0053401	10.8072658	2
59	9.1935341	9.9946399	9.1988942	10.8011059	10.0053601	10.8064659	1
60	9.1943324	9.9946199	9.1997125	10.8002875	10.0053801	10.8056676	0
M		Sine.		Tang.		Secant	M

81 Degrees.

A Table of Artificial Sines,

9 Degrees.

M	Sine		Tang		Secant		M
0	9.1943324	9.9346193	9.1997125	10.0001875	10.0053801	10.0056676	60
1	9.1961238	9.9345999	9.2005294	10.7934706	10.0054001	10.8043707	59
2	9.1979147	9.9345796	9.2013449	10.7986551	10.0054202	10.8043763	58
3	9.1997050	9.9345597	9.2021598	10.7978411	10.0054403	10.8043814	57
4	9.2014948	9.9345396	9.2029714	10.7970286	10.0054604	10.8043870	56
5	9.2032839	9.9345194	9.2037825	10.7962175	10.0054806	10.8043931	55
6	9.2050725	9.9344992	9.2045922	10.7954079	10.0055008	10.8043987	54
7	9.2068605	9.9344789	9.2054024	10.7945976	10.0055211	10.8044207	53
8	9.2086480	9.9344587	9.2062072	10.7937928	10.0055413	10.7993342	52
9	9.2104349	9.9344383	9.2070126	10.7929874	10.0055617	10.7985491	51
10	9.2122213	9.9344180	9.2078165	10.7921835	10.0055820	10.7977655	50
11	9.2140071	9.9343975	9.2086191	10.7913809	10.0056025	10.7969833	49
12	9.2157924	9.9343771	9.2094205	10.7905797	10.0056227	10.7962026	48
13	9.2175766	9.9343566	9.2102202	10.7897800	10.0056434	10.7954234	47
14	9.2193605	9.9343361	9.2110184	10.7889816	10.0056639	10.7946455	46
15	9.2211439	9.9343156	9.2118163	10.7881847	10.0056844	10.7938691	45
16	9.2229269	9.9342950	9.2126129	10.7873871	10.0057050	10.7930941	44
17	9.2247094	9.9342743	9.2134081	10.7865919	10.0057257	10.7923205	43
18	9.2264916	9.9342537	9.2141980	10.7858020	10.0057463	10.7915484	42
19	9.2282734	9.9342330	9.2149894	10.7850106	10.0057670	10.7907776	41
20	9.2300547	9.9342122	9.2157795	10.7842205	10.0057878	10.7900083	40
21	9.2318357	9.9341914	9.2165683	10.7834317	10.0058086	10.7892403	39
22	9.2336163	9.9341706	9.2173556	10.7826444	10.0058294	10.7884737	38
23	9.2353964	9.9341498	9.2181417	10.7818583	10.0058502	10.7877086	37
24	9.2371762	9.9341289	9.2189264	10.7810736	10.0058711	10.7869448	36
25	9.2389555	9.9341079	9.2197097	10.7802903	10.0058921	10.7861824	35
26	9.2407344	9.9340870	9.2204917	10.7795083	10.0059130	10.7854213	34
27	9.2425129	9.9340659	9.2212724	10.7787276	10.0059341	10.7846616	33
28	9.2442909	9.9340449	9.2220518	10.7779482	10.0059551	10.7839033	32
29	9.2460685	9.9340238	9.2228298	10.7771702	10.0059762	10.7831464	31
30	9.2478456	9.9340027	9.2236065	10.7763935	10.0059973	10.7823908	30
M		Sine.		Tang		Secant	M

80 Degrees.

9 Degrees.

M	Sine.		Tang		Secant		M
30	9.2176092	9.9930017	9.2236065	10.7763935	10.0050973	10.7823908	30
31	9.2183635	9.9929815	9.2243819	10.7756181	10.0060185	10.7816365	29
32	9.2191164	9.9929602	9.2251561	10.7748439	10.0069397	10.7808836	28
33	9.2198680	9.9929391	9.2259289	10.7740711	10.0078607	10.7801320	27
34	9.2206182	9.9929175	9.2267004	10.7732996	10.0087822	10.7793818	26
35	9.2213671	9.9928965	9.2274706	10.7725294	10.0097035	10.7786329	25
36	9.2221147	9.9928752	9.2282395	10.7717605	10.0106245	10.7778853	24
37	9.2228609	9.9928538	9.2290071	10.7709929	10.0115452	10.7771391	23
38	9.2236059	9.9928324	9.2297735	10.7702265	10.0124656	10.7763941	22
39	9.2243495	9.9928109	9.2305386	10.7694614	10.0133858	10.7756505	21
40	9.2250918	9.9927894	9.2313024	10.7686976	10.0143056	10.7749082	20
41	9.2258328	9.9927679	9.2320650	10.7679350	10.0152252	10.7741672	19
42	9.2265725	9.9927463	9.2328262	10.7671738	10.0161445	10.7734275	18
43	9.2273110	9.9927247	9.2335863	10.7664137	10.0170635	10.7726890	17
44	9.2280481	9.9927032	9.2343451	10.7656549	10.0179822	10.7719519	16
45	9.2287839	9.9926813	9.2351026	10.7648974	10.0189007	10.7712161	15
46	9.2295185	9.9926596	9.2358589	10.7641411	10.0198189	10.7704815	14
47	9.2302518	9.9926378	9.2366139	10.7633861	10.0207368	10.7697482	13
48	9.2309838	9.9926160	9.2373678	10.7626322	10.0216545	10.7690162	12
49	9.2317145	9.9925942	9.2381203	10.7618797	10.0225718	10.7682855	11
50	9.2324440	9.9925723	9.2388717	10.7611283	10.0234889	10.7675560	10
51	9.2331722	9.9925504	9.2396218	10.7603782	10.0244056	10.7668278	9
52	9.2338992	9.9925285	9.2403708	10.7596292	10.0253220	10.7661008	8
53	9.2346249	9.9925065	9.2411185	10.7588815	10.0262381	10.7653751	7
54	9.2353494	9.9924844	9.2418650	10.7581350	10.0271539	10.7646506	6
55	9.2360726	9.9924624	9.2426103	10.7573897	10.0280695	10.7639274	5
56	9.2367946	9.9924403	9.2433543	10.7566457	10.0289847	10.7632054	4
57	9.2375153	9.9924181	9.2440972	10.7559028	10.0298996	10.7624847	3
58	9.2382349	9.9923959	9.2448389	10.7551611	10.0308142	10.7617651	2
59	9.2389532	9.9923737	9.2455794	10.7544206	10.0317285	10.7610468	1
60	9.2396702	9.9923515	9.2463189	10.7536812	10.0326426	10.7603298	0
		Sine.		Tang.		Secant	M

80 Degrees.

A Table of Artificial Sines,

10 Degrees.

M	Sine.		Tang.		Secant		M
0	9·2396702	9·9933515	9·2463188	10·7536812	10·0066485	10·7603298	60
1	9·2403861	9·9933292	9·2470569	10·7529431	10·0066708	10·7596139	59
2	9·2411007	9·9933068	9·2477939	10·7522061	10·0066932	10·7588993	58
3	9·2418141	9·9932845	9·2485297	10·7514703	10·0067155	10·7581859	57
4	9·2425264	9·9932621	9·2492643	10·7507357	10·0067379	10·7574736	56
5	9·2432374	9·9932396	9·2499978	10·7500022	10·0067604	10·7567626	55
6	9·2439472	9·9932171	9·2507301	10·7492699	10·0067829	10·7560528	54
7	9·2446558	9·9931946	9·2514612	10·7485388	10·0068054	10·7553442	53
8	9·2453632	9·9931720	9·2521912	10·7478088	10·0068280	10·7546368	52
9	9·2460695	9·9931494	9·2529200	10·7470800	10·0068506	10·7539305	51
10	9·2467746	9·9931268	9·2536477	10·7463523	10·0068732	10·7532254	50
11	9·2474784	9·9931041	9·2543743	10·7456257	10·0068959	10·7525216	49
12	9·2481811	9·9930814	9·2550997	10·7449003	10·0069186	10·7518189	48
13	9·2488827	9·9930587	9·2558240	10·7441760	10·0069413	10·7511173	47
14	9·2495830	9·9930359	9·2565472	10·7434528	10·0069641	10·7504170	46
15	9·2502822	9·9930131	9·2572692	10·7427308	10·0069869	10·7497178	45
16	9·2509803	9·9929902	9·2579901	10·7420099	10·0070098	10·7490197	44
17	9·2516772	9·9929673	9·2587099	10·7412901	10·0070327	10·7483228	43
18	9·2523729	9·9929444	9·2594285	10·7405715	10·0070556	10·7476271	42
19	9·2530675	9·9929214	9·2601461	10·7398539	10·0070786	10·7469325	41
20	9·2537609	9·9928984	9·2608625	10·7391375	10·0071016	10·7462391	40
21	9·2544532	9·9928753	9·2615779	10·7384221	10·0071247	10·7455468	39
22	9·2551444	9·9928522	9·2622921	10·7377079	10·0071478	10·7448556	38
23	9·2558344	9·9928291	9·2630053	10·7369947	10·0071709	10·7441656	37
24	9·2565233	9·9928059	9·2637173	10·7362827	10·0071941	10·7434767	36
25	9·2572110	9·9927827	9·2644283	10·7355717	10·0072173	10·7427890	35
26	9·2578977	9·9927595	9·2651382	10·7348618	10·0072405	10·7421022	34
27	9·2585832	9·9927362	9·2658470	10·7341530	10·0072638	10·7414168	33
28	9·2592676	9·9927129	9·2665547	10·7334453	10·0072871	10·7407324	32
29	9·2599509	9·9926895	9·2672613	10·7327387	10·0073105	10·7400491	31
30	9·2606330	9·9926661	9·2679669	10·7320331	10·0073339	10·7393670	30
		Sine.		Tang.		Secant	M

79 Degrees.

Tangents, and Secants.

10 Degrees.

M	Sine.		Tang		Secant		
30	9.2606330	9.9926661	9.2679669	10.7320331	10.0073339	10.7393670	30
31	9.2613141	9.9926427	9.2686714	10.7313286	10.0073573	10.7386559	29
32	9.2619941	9.9926192	9.2693749	10.7306251	10.0073808	10.7380559	28
33	9.2626729	9.9925957	9.2700772	10.7299228	10.0074043	10.7373271	27
34	9.2633507	9.9925722	9.2707786	10.7292214	10.0074278	10.7366493	26
35	9.2640274	9.9925486	9.2714788	10.7285212	10.0074514	10.7359729	25
36	9.2647030	9.9925252	9.2721780	10.7278220	10.0074750	10.7352970	24
37	9.2653775	9.9925013	9.2728762	10.7271238	10.0074987	10.7346225	23
38	9.2660509	9.9924776	9.2735733	10.7264267	10.0075224	10.7339491	22
39	9.2667232	9.9924339	9.2742694	10.7257306	10.0075461	10.7332768	21
40	9.2673945	9.9924301	9.2749644	10.7250356	10.0075699	10.7326055	20
41	9.2680647	9.9924063	9.2756584	10.7243416	10.0075937	10.7319353	19
42	9.2687338	9.9923824	9.2763514	10.7236485	10.0076176	10.7312662	18
43	9.2694019	9.9923585	9.2770434	10.7229566	10.0076415	10.7305981	17
44	9.2700689	9.9923346	9.2777343	10.7222657	10.0076654	10.7299311	16
45	9.2707348	9.9923106	9.2784242	10.7215758	10.0076894	10.7292652	15
46	9.2713997	9.9922866	9.2791130	10.7208869	10.0077134	10.7286003	14
47	9.2720635	9.9922626	9.2798009	10.7201991	10.0077374	10.7279365	13
48	9.2727263	9.9922385	9.2804878	10.7195122	10.0077615	10.7272737	12
49	9.2733880	9.9922144	9.2811736	10.7188264	10.0077856	10.7266120	11
50	9.2740487	9.9921902	9.2818585	10.7181415	10.0078098	10.7259513	10
51	9.2747083	9.9921660	9.2825423	10.7174577	10.0078340	10.7252917	9
52	9.2753669	9.9921418	9.2832251	10.7167749	10.0078582	10.7246331	8
53	9.2760245	9.9921175	9.2839069	10.7160930	10.0078825	10.7239755	7
54	9.2766811	9.9920932	9.2845878	10.7154122	10.0079068	10.7233189	6
55	9.2773366	9.9920689	9.2852677	10.7147323	10.0079311	10.7226634	5
56	9.2779911	9.9920445	9.2859466	10.7140534	10.0079555	10.7220089	4
57	9.2786445	9.9920201	9.2866245	10.7133755	10.0079799	10.7213555	3
58	9.2792970	9.9919956	9.2873014	10.7126986	10.0080044	10.7207030	2
59	9.2799484	9.9919711	9.2879773	10.7120227	10.0080289	10.7200516	1
60	9.2805988	9.9919466	9.2886523	10.7113477	10.0080534	10.7194012	0
		Sine.		Tang.		Secant	M

79 Degrees.

A Table of Artificial Sines,

11 Degrees.

M	Sine.		Tang.		Secant		M
0	9.2805988	9.9919406	9.2886523	10.7113477	10.0080534	10.7194012	60
1	9.2812483	9.9919220	9.2892363	10.7107637	10.0080730	10.7187517	59
2	9.2818967	9.9918974	9.2899193	10.7100807	10.0081026	10.7181033	58
3	9.2825441	9.9918727	9.2906713	10.7093287	10.0081273	10.7174559	57
4	9.2831905	9.9918480	9.2913424	10.7086576	10.0081520	10.7168095	56
5	9.2838359	9.9918233	9.2920126	10.7079874	10.0081767	10.7161641	55
6	9.2844803	9.9917986	9.2926817	10.7073183	10.0082014	10.7155197	54
7	9.2851237	9.9917737	9.2933500	10.7066500	10.0082263	10.7148763	53
8	9.2857661	9.9917489	9.2940172	10.7059828	10.0082511	10.7142339	52
9	9.2864076	9.9917240	9.2946836	10.7053164	10.0082760	10.7135924	51
10	9.2870480	9.9916991	9.2953489	10.7046511	10.0083009	10.7129520	50
11	9.2876875	9.9916741	9.2960134	10.7039866	10.0083259	10.7123125	49
12	9.2883260	9.9916492	9.2966769	10.7033231	10.0083508	10.7116840	48
13	9.2889636	9.9916241	9.2973395	10.7026605	10.0083759	10.7110364	47
14	9.2896001	9.9915990	9.2980011	10.7019989	10.0084010	10.7103999	46
15	9.2902357	9.9915739	9.2986618	10.7013382	10.0084261	10.7097643	45
16	9.2908704	9.9915488	9.2993216	10.7006784	10.0084512	10.7091296	44
17	9.2915042	9.9915236	9.2999804	10.7000196	10.0084764	10.7084960	43
18	9.2921367	9.9914984	9.3006383	10.6993617	10.0085016	10.7078633	42
19	9.2927685	9.9914731	9.3012954	10.6987046	10.0085269	10.7072315	41
20	9.2933993	9.9914478	9.3019514	10.6980486	10.0085522	10.7066007	40
21	9.2940291	9.9914225	9.3026066	10.6973934	10.0085775	10.7059709	39
22	9.2946580	9.9913717	9.3032609	10.6967391	10.0086029	10.7053420	38
23	9.2952859	9.9913717	9.3039143	10.6960857	10.0086283	10.7047141	37
24	9.2959129	9.9913462	9.3045667	10.6954333	10.0086538	10.7040871	36
25	9.2965390	9.9913207	9.3052183	10.6947817	10.0086793	10.7034610	35
26	9.2971641	9.9912952	9.3058689	10.6941311	10.0087048	10.7028359	34
27	9.2977883	9.9912696	9.3065187	10.6934813	10.0087304	10.7022117	33
28	9.2984116	9.9912440	9.3071675	10.6928325	10.0087560	10.7015884	32
29	9.2990339	9.9912184	9.3078155	10.6921845	10.0087816	10.7009661	31
30	9.2996553	9.9911927	9.3084626	10.6915374	10.0088073	10.7003447	30
		Sine.		Tang.		Secant	M

78 Degrees.

11 Degrees.

M	Sine.		Tang		Secant		
30	9 2996553	9.9311927	9 3084626	10 6915374	10.0088073	10.7003447	30
31	9 3002758	9.9311670	9.3091088	10.6908912	10.0088330	10.6997242	29
32	9.3008953	9.9311412	9.3097541	10 6902459	10.0088588	10.6991047	28
33	9.3015140	9 9311154	9 3103985	10.6896015	10 0088846	10.6984860	27
34	9.3021317	9.9310896	9.3110421	10.6889579	10.0089104	10.6978683	26
35	9.3027485	9.9310637	9.3116848	10.6883152	10 0089363	10.6972515	25
36	9.3033644	9.9310378	9.3123266	10.6876734	10.0089622	10.6966356	24
37	9 3039794	9.9310119	9.3129675	10.6870325	10 0089881	10.6960206	23
38	9.3045934	9 9309859	9.3136076	10.6863924	10.0090141	10.6954066	22
39	9.3052066	9.9309598	9 3142468	10 6857532	10.0090402	10 6947934	21
40	9.3058189	9 9309338	9.3148851	10.6851149	10 0090662	10.6941811	20
41	9 3064303	9 9309077	9.3155226	10.6844774	10.0090923	10.6935697	19
42	9.3070407	9 9308815	9.3161592	10.6838408	10.0091185	10.6929593	18
43	9.3076503	9.9308553	9.3167950	10.6832050	10.0091447	10 6923497	17
44	9.3082590	9.9308291	9.3174299	10.6825701	10.0091709	10.6917410	16
45	9.3088668	9.9308029	9.3180640	10.6819360	10.0091971	10.6911332	15
46	9.3094737	9.9307766	9.3186972	10 6813028	10.0092234	10 6905263	14
47	9.3100798	9.9307502	9.3193295	10 6806705	10 0092498	10.6899202	13
48	9.3106849	9.9307239	9.3199611	10.6800389	10.0092761	10 6893151	12
49	9.3112892	9.9306974	9.3205918	10 6794082	10.0093026	10.6887108	11
50	9 3118926	9.9306710	9.3212216	10.6787784	10.0093290	10.6881074	10
51	9 3124951	9 9306445	9.3218506	10.6781494	10 0093555	10.6875049	9
52	9.3130968	9.9306180	9.3224788	10.6775212	10.0093820	10.6869032	8
53	9.3136976	9.9305914	9.3231061	10.6768939	10 0094086	10 6863024	7
54	9.3142975	9 9305648	9.3237327	10 6762673	10.0094352	10 6857025	6
55	9.3148965	9.9305382	9.3243584	10.6756416	10 0094618	10.6851035	5
56	9.3154947	9 9305115	9 3249832	10 6750168	10.0094885	10 6845053	4
57	9.3160921	9 9304848	9.3256073	10 6743927	10 0095152	10 6839079	3
58	9.3166885	9.9304580	9.3262305	10 6737695	10 0095420	10.6833115	2
59	9.3172841	9.9304312	9 3268529	10 6731471	10.0095688	10 6827159	1
60	9.3178789	9 9304044	9.3274745	10.6725255	10 0095956	10.6821211	0
M		Sine		Tang		Secant	M

78 Degrees.

A Table of Artificial Sines,

12 Degrees.

M	Sine.		Tang		Secant		M
0	9 3178789	9·9304044	9·3274745	10 6725255	10·0030966	10·6821211	60
1	9·3181728	9·9303775	9·3280033	10·6719947	10 0030225	10·6815272	59
2	9·3184669	9 9303506	9·3287153	10·6712847	10·0036494	10 6809341	58
3	9·3196581	9 9303237	9·3293345	10·6706655	10 0036763	10 6803419	57
4	9·3202495	9·9302967	9·3299528	10 6700472	10 0037032	10 6797505	56
5	9·3208400	9·9302697	9 3305704	10·6693426	10 0037303	10·6791600	55
6	9·3214297	9·9302426	9·3311872	10·6688128	10·0037574	10 6785703	54
7	9·3220186	9·9302155	9 3318031	10·6681969	10·0037845	10·6779814	53
8	9·3226066	9·9301883	9·3324183	10·6675817	10 0038117	10·6773934	52
9	9·3231938	9 9301612	9 3330327	10·6669673	10·0038388	10·6768062	51
10	9·3237802	9·9301339	9 3336463	10·6663537	10·0038661	10 6762198	50
11	9 3243657	9 9301067	9·3342591	10·6657409	10·0038933	10·6756343	49
12	9·3249505	9 9300794	9·3348711	10 6651289	10 0039206	10 6750495	48
13	9 3255344	9·9300521	9·3354823	10·6645177	10 0039479	10 6744656	47
14	9 3261174	9·9300247	9·3360927	10 6639073	10·0039753	10 6738826	46
15	9·3266997	9·9299973	9 3367024	10·6632967	20·0100027	10·6733003	45
16	9 3272811	9 9299698	9 3373113	10·6626887	10 0100302	10·6727189	44
17	9·3278617	9·9299423	9·3379194	10·6620806	10·0100577	10·6721383	43
18	9·3284416	9 9299148	9·3385267	10 6614733	10 0100852	10·6715584	42
19	9·3290206	9·9298873	9·3391333	10·6608667	10·0101127	10 6709794	41
20	9·3295988	9·9298597	9·3397391	10·6602609	10·0101403	10 6704012	40
21	9 3301761	9·9298320	9·3403441	10·6596559	10·0101679	10·6698239	39
22	9·3307527	9 9298043	9·3409484	10·6590516	10·0101957	10 6692473	38
23	9·3313285	9·9297766	9·3415519	10·6584481	10·0102234	10·6686715	37
24	9·3319035	9·9297489	9·3421546	10·6578454	10·0102511	10·6680965	36
25	9·3324777	9 9297211	9 3427566	10·6572434	10 0102789	10·6675223	35
26	9·3330511	9·9296932	9·3433578	10 6566422	10·0103068	10·6669489	34
27	9·3336237	9·9296654	9·3439583	10·6560417	10·0103346	10·6663763	33
28	9·3341955	9 9296374	9·3445580	10 6554420	10 0103626	10·6658045	32
29	9·3347665	9·9296095	9·3451570	10·6548430	10 0103905	10·6652335	31
30	9·3353368	9·9295815	9·3457552	10·6542448	10 0104185	10·6646632	30
M		Sine.		Tang		Secant	M

77 Degrees.

12 Degrees.

M	Sine.		Tang		Secant		
30	9.3353398	9.9895816	9.3457552	10.0542448	10.0104185	10.0046632	30
31	9.3359362	9.9895535	9.3463527	10.0536473	10.0104465	10.0040938	29
32	9.3365343	9.9895254	9.3469494	10.0530506	10.0104746	10.0035251	28
33	9.3371338	9.9894973	9.3475454	10.0524546	10.0105027	10.0029572	27
34	9.3377349	9.9894692	9.3481407	10.0518593	10.0105308	10.0023901	26
35	9.3383376	9.9894410	9.3487352	10.0512648	10.0105590	10.0018274	25
36	9.3387418	9.9894128	9.3493290	10.0506710	10.0105872	10.0012582	24
37	9.3393475	9.9893845	9.3499220	10.0500780	10.0106155	10.0006935	23
38	9.3398706	9.9893562	9.3505143	10.0494857	10.0106438	10.0001294	22
39	9.3404338	9.9893279	9.3511059	10.0488941	10.0106721	10.0595662	21
40	9.3409963	9.9892995	9.3516968	10.0483032	10.0107005	10.0590037	20
41	9.3415580	9.9892711	9.3521869	10.0477131	10.0107289	10.0584420	19
42	9.3421190	9.9892427	9.3528763	10.0471237	10.0107573	10.0578810	18
43	9.3426792	9.9892142	9.3534650	10.0465350	10.0107858	10.0573208	17
44	9.3432386	9.9891856	9.3540530	10.0459470	10.0108144	10.0567614	16
45	9.3437973	9.9891571	9.3546402	10.0453598	10.0108429	10.0562027	15
46	9.3443552	9.9891285	9.3552267	10.0447733	10.0108716	10.0556448	14
47	9.3449124	9.9890998	9.3558126	10.0441874	10.0109002	10.0550876	13
48	9.3454688	9.9890711	9.3563977	10.0436023	10.0109289	10.0545312	12
49	9.3460245	9.9890424	9.3569821	10.0430179	10.0109576	10.0539755	11
50	9.3465794	9.9890137	9.3575658	10.0424342	10.0109863	10.0534206	10
51	9.3471336	9.9889849	9.3581487	10.0418513	10.0110151	10.0528664	9
52	9.3476870	9.9889560	9.3587310	10.0412690	10.0110440	10.0523130	8
53	9.3482397	9.9889271	9.3593126	10.0406874	10.0110729	10.0517603	7
54	9.3487917	9.9888982	9.3598935	10.0401065	10.0111018	10.0512083	6
55	9.3493429	9.9888693	9.3601736	10.0395264	10.0111307	10.0506571	5
56	9.3498934	9.9888403	9.3610531	10.0389469	10.0111597	10.0501066	4
57	9.3504432	9.9888113	9.3616319	10.0383681	10.0111887	10.0495568	3
58	9.3509922	9.9887822	9.3622100	10.0377900	10.0112178	10.0490078	2
59	9.3515405	9.9887531	9.3627874	10.0372126	10.0112469	10.0484595	1
60	9.3520880	9.9887239	9.3633641	10.0366359	10.0112761	10.0479120	0
		Sine.		Tang.		Secant	M

77 Degrees.

A Table of Artificial Sines,

13 Degrees.

M	Sine.		Tang		Secant		M
0	9·3520880	9·9887239	9·3633641	10 6366359	10·0112761	10 6479120	60
1	9 3526349	9 9886847	9·3639401	10 6360599	10·0113053	10 6473651	59
2	9·3531810	9·9886655	9 3645155	10·6354845	10·0113345	10·6468190	58
3	9·3537264	9·9886363	9·3650901	10 6349099	10·0113637	10 6462736	57
4	9 3542710	9·9886070	9 3656641	10·6343359	10·0113930	10·6457290	56
5	9·3548150	9·9885776	9·3662374	10·6337626	10·0114222	10 6451850	55
6	9·3553582	9 9885482	9·3668100	10 6331900	10·0114518	10 6446418	54
7	9·3559008	9·9885188	9·3673819	10·6326181	10·0114812	10·6440993	53
8	9 3564426	9·9884894	9·3679532	10·6320468	10·0115106	10 6435574	52
9	9·3569836	9 9884599	9·3685238	10·6314762	10 0115401	10·6430164	51
10	9·3575240	9 9884303	9·3690937	10·6309063	10 0115697	10·6424760	50
11	9·3580637	9·9884008	9·3696629	10·6303371	10 0115992	10·6419363	49
12	9·3586027	9·9883712	9·3702315	10·6297685	10·0116288	10·6413973	48
13	9·3591409	9·9883415	9·3707994	10 6292006	10·0116585	10 6408591	47
14	9 3596785	9·9883118	9 3713667	10 6286333	10·0116882	10·6403215	46
15	9·3602154	9·9882821	9·3719333	10 6280667	10·0117179	10 6397846	45
16	9·3607515	9·9882523	9·3724992	10 6275008	10 0117477	10·6392485	44
17	9·3612870	9·9882225	9·3730645	10·6269355	10·0117775	10·6387130	43
18	9·3618217	9·9881927	9·3736291	10·6263709	10 0118073	10·6381783	42
19	9·3623558	9·9881628	9 3741930	10·6258070	10·0118372	10·6376442	41
20	9 3628892	9·9881329	9·3747565	10 6252437	10 0118671	10 6371108	40
21	9·3634219	9 9881029	9 3753190	10·6246810	10·0118971	10·6365781	39
22	9·3639539	9·9880729	9·3758810	10·6241190	10·0119271	10·6360461	38
23	9 3644852	9·9880429	9·3764423	10 6235577	10·0119571	10·6355148	37
24	9·3650158	9·9880128	9·3770030	10·6229970	10·0119872	10·6349842	36
25	9·3655458	9·9879827	9 3775631	10 6224369	10·0120173	10·6344542	35
26	9·3660750	9 9879525	9·3781225	10·6218775	10·0120475	10·6339250	34
27	9·3666036	9·9879223	9·3786813	10·6213187	10·0120777	10·6333964	33
28	9·3671315	9·9878921	9·3792394	10·6207606	10 0121079	10·6328685	32
29	9·3676587	9·9878618	9·3797969	10·6202031	10·0121382	10·6323413	31
30	9 3681853	9·9878315	9 3803537	10·6196463	10 0121685	10·6318147	30
M		Sine.		Tang.		Secant	M

76 Degrees.

13 Degrees.

M	Sine.		Tang		Secant		
30	9·3681853	9·9878315	9·380353	10·6196493	10·0121685	10 6318147	30
31	9·3687141	9·9878012	9 3829100	10 6192900	10·0121988	10·6312859	29
32	9·3692363	9 9877703	9·3854055	10·6185345	10·0122292	10 6307657	28
33	9 3697603	9 9877104	9·382 205	10·6179795	10·0122596	10·6302392	27
34	9 3702847	9 9877093	9 3825748	10·6174252	10·0122901	10·6297153	26
35	9·3708079	9 9876794	9·3831285	10,6168715	10·0123206	10·6291921	25
36	9·3713304	9·9876483	9 3836816	10·6163184	10·0123512	10·6286696	24
37	9·3718523	9·9876185	9·3842340	10·6157660	10 0123817	10·6281477	23
38	9·3723735	9·9875876	9·3847858	10·6152142	10·0124124	10·6276265	22
39	9·3728	9 9875570	9·3853370	10·6146630	10·0124430	10·6271060	21
40	9·373	9 9875263	9 3858876	10·6141124	10·0124737	10 6265861	20
41	9·37	9·9874955	9 3864376	10·6135624	10 0125045	10·6260669	19
42	9 37 4617	9 9874648	9 3869869	10·6130131	10 0125352	10 6255483	18
43	9·3749696	9·9874339	9·3875356	10·6124644	10·0125661	10·6250304	17
44	9 3754868	9·9874031	9·3880837	10·6119163	10 0125969	10·6245132	16
45	9·3760034	9 9873722	9 3886312	10 6113688	10 0126278	10·6239966	15
46	9·3765194	9·9873413	9 3891781	10 6108219	10·0126587	10·6234806	14
47	9·3770347	9 9873103	9·3897244	10 6102756	10·0126897	10·6229653	13
48	9 3775493	9 9872793	9·3902700	10 6097300	10 0127207	10·6224507	12
49	9·3780633	9 9872482	9·3908155	10·6091849	10·0127518	10·6219367	11
50	9·3785767	9·9872171	9·3913595	10 6086405	10·0127829	10·6214233	10
51	9·3790894	9·9871860	9·3919034	10·6080966	10 0128140	10·6209106	9
52	9·3796015	9·9871549	9·3924466	10 6075534	10·0128451	10 6203985	8
53	9·3801129	9 9871236	9 3929893	10·6070107	10·0128764	10 6198871	7
54	9·3806237	9·9870924	9 3935313	10·6064487	10·0129076	10·6193763	6
55	9·3811339	9·9870611	9 3940727	10·6059272	10·0129389	10 6188661	5
56	9·3816434	9 9870298	9 3946136	10·6053864	10 0129702	10·6183566	4
57	9·3821523	9·9869984	9·3951538	10·6048462	10·0130016	10·6178477	3
58	9·3826605	9 9869670	9·3956935	10·6043065	10 0130330	10·6173395	2
59	9·3831682	9 9869356	9·3962326	10·6037674	10·0130644	10·6168318	1
60	9·3836752	9·9869041	9·3967711	10·6032289	10·0130959	10 6163248	0
		Sine.		Tang		Secant	M

76 Degrees.

A Table of Artificial Sines,

14 Degrees.

M	Sine.		Tang		Secan		M
0	9.3836752	9.9869041	9.3967711	10.6032289	10.0130959	10.6163248	60
1	9.3841815	9.9868726	9.3973089	10.6026911	10.0131274	10.6158185	59
2	9.3846873	9.9868410	9.3978463	10.6021537	10.0131590	10.6153127	58
3	9.3851924	9.9868094	9.3983830	10.6016170	10.0131906	10.6148076	57
4	9.3856969	9.9867778	9.3989191	10.6010809	10.0132222	10.6143031	56
5	9.3862008	9.9867461	9.3994547	10.6005453	10.0132539	10.6137992	55
6	9.3867040	9.9867144	9.3999896	10.6000104	10.0132856	10.6132960	54
7	9.3872067	9.9866827	9.4005240	10.5994760	10.0133173	10.6127933	53
8	9.3877087	9.9866509	9.4010578	10.5989422	10.0133491	10.6122913	52
9	9.3882101	9.9866191	9.4015910	10.5984090	10.0133809	10.6117899	51
10	9.3887109	9.9865872	9.4021237	10.5978763	10.0134128	10.6112891	50
11	9.3892111	9.9865553	9.4026558	10.5973442	10.0134447	10.6107889	49
12	9.3897106	9.9865233	9.4031873	10.5968127	10.0134767	10.6102894	48
13	9.3902096	9.9864913	9.4037182	10.5962818	10.0135087	10.6097904	47
14	9.3907079	9.9864593	9.4042486	10.5957514	10.0135407	10.6092921	46
15	9.3912057	9.9864273	9.4047784	10.5952216	10.0135727	10.6087943	45
16	9.3917028	9.9863952	9.4053076	10.5946924	10.0136048	10.6082972	44
17	9.3921993	9.9863630	9.4058363	10.5941637	10.0136370	10.6078007	43
18	9.3926952	9.9863308	9.4063644	10.5936356	10.0136692	10.6073048	42
19	9.3931905	9.9862986	9.4068919	10.5931081	10.0137014	10.6068095	41
20	9.3936852	9.9862663	9.4074189	10.5925811	10.0137337	10.6063148	40
21	9.3941794	9.9862340	9.4079453	10.5920547	10.0137660	10.6058206	39
22	9.3946729	9.9862017	9.4084712	10.5915288	10.0137983	10.6053271	38
23	9.3951658	9.9861693	9.4089965	10.5910035	10.0138307	10.6048342	37
24	9.3956581	9.9861369	9.4095212	10.5904788	10.0138631	10.6043419	36
25	9.3961499	9.9861045	9.4100454	10.5899546	10.0138955	10.6038501	35
26	9.3966410	9.9860720	9.4105690	10.5894310	10.0139280	10.6033590	34
27	9.3971315	9.9860394	9.4110921	10.5889079	10.0139606	10.6028685	33
28	9.3976215	9.9860069	9.4116146	10.5883854	10.0139931	10.6023785	32
29	9.3981109	9.9859742	9.4121366	10.5878634	10.0140258	10.6018891	31
30	9.3985996	9.9859416	9.4126581	10.5873419	10.0140584	10.6014004	30
		Sine.		Tang.		Secant	M

75 Degrees.

14 Degrees.

M	Sine.		Tang		Secant		M
30	9·3985396	9·9869416	9·4120581	10 5873419	10·0140584	10 0014004	30
31	9·3970878	9 9854889	9·4131780	10·5868211	10.0140911	10·0009122	29
32	9 3956364	9·9858762	9 4136993	10·5863027	10.0141238	10 0004246	28
33	9 4000625	9 9838434	9 4142191	10·5857803	10·0141566	10 9993375	27
34	9·4005489	9·9838126	9·4147383	10·5852617	10 0 41894	10·9988511	26
35	9·4010338	9·9837777	9 4152570	10·5847430	10 0142223	10·9983652	25
36	9·4015201	9·9857443	9·4157752	10·5842248	10·0142551	10 9984799	24
37	9·4020048	9 9857119	9 4162928	10 5837072	10.0142881	10·9979952	23
38	9·4024889	9 9856792	9·4168099	10·5831901	10·0143210	10·9975111	22
39	9·4029734	9·9856470	9·4173265	10 5826735	10.0143540	10 9970276	21
40	9·4034554	9 9856129	9 4178425	10 5821575	10.0143871	10 9965446	20
41	9·4039378	9 9855798	9·4183580	10·5816420	10·0144202	10·9960622	19
42	9·4044195	9·9855467	9·4188729	10·5811271	10 0144533	10 9955804	18
43	9·4049003	9 9855135	9·4193874	10 5806126	10 0144865	10·9950991	17
44	9·4053816	9·9854803	9·4199013	10·5800987	10·0145197	10·9946184	16
45	9 4058617	9·9854471	9·4204146	10·5795854	10 0145529	10 9941383	15
46	9 4063413	9·9854138	9·4209275	10 5790725	10.0145862	10·9936587	14
47	9·4068203	9·9853805	9·4214398	10·5785602	10.0146195	10·9931797	13
48	9 4072987	9·9853471	9 4219515	10·5780485	10·0146529	10·9927013	12
49	9·4077766	9·9853138	9·4224628	10·5775372	10·0146862	10·9922234	11
50	9·4082539	9·9852805	9 4229735	10·5770265	10.0147197	10·9917461	10
51	9·4087306	9·9852468	9·4234838	10·5765162	10 0147532	10·9912694	9
52	9·4092068	9·9852133	9·4239935	10 5760065	10.0147867	10·9907932	8
53	9·4096824	9·9851798	9·4245026	10·5754974	10·0148202	10 9903176	7
54	9·4101575	9·9851462	9·4250113	10·5749887	10 0148538	10 9898425	6
55	9·4106320	9·9851125	9·4255194	10 5744806	10.0148875	10 9893680	5
56	9 4111059	9·9850789	9·4260271	10·5739729	10 0149211	10·9888941	4
57	9·4115793	9·9850452	9 4265342	10·5734658	10·0149548	10·9884207	3
58	9·4120522	9·9850114	9·4270408	10 5729592	10 0149886	10 9879478	2
59	9 4125245	9·9849776	9·4275469	10·5724531	10 0150221	10 9874755	1
60	9·4129962	9·9849438	9 4280525	10·5719475	10 0150562	10·9870038	0
		Sine.		Tang.		Secant	M

75 Degrees.

A Table of Artificial Sines,

15 *Degrees.*

M	Sine		Tang		Secant		
0	9·4129352	9 9849438	9 4280525	10·5719475	10·0150562	10·5870038	60
1	9·4134674	9 9849299	9·4285575	10·5714425	10·0150301	10·5865326	59
2	9·4139361	9·9848760	9·4290621	10·5709379	10 0151242	10 5860819	58
3	9·4144082	9 9848420	9 4295661	10·5704339	10 0151580	10 5855918	57
4	9·4148778	9 9848081	9 4300697	10 5699303	10·0151919	10·5851222	56
5	9·4153478	9·9847743	9·4305727	10·5694273	10·0152260	10 5846532	55
6	9·4158152	9·9847400	9 4310753	10·5689247	10 0152600	10·5841848	54
7	9·4162832	9 9847059	9 4315773	10·5684227	10·0152941	10·5837168	53
8	9·4167506	9 9846717	9 4320789	10·5679211	10·0153283	10·5832494	52
9	9 4172174	9·9846375	9 4325799	10·5674201	10 0153625	10 5827826	51
10	9 4176837	9·9846033	9·4330804	10 5669196	10 0153967	10 5823163	50
11	9 4181495	9·9845690	9 4335805	10·5664195	10·0154310	10 5818505	49
12	9·4186148	9·9845347	9 4340800	10·5659200	10·0154653	10 5813852	48
13	9·4190795	9·9845004	9·4345711	10·5654289	10·0154996	10·5809205	47
14	9·4195436	9·9844660	9 4350776	10 5649224	10 0155340	10 5804564	46
15	9 4200073	9·9844316	9 4355757	10·5644243	10·0155684	10·5799927	45
16	9·4204704	9 9843971	9·4360733	10·5639267	10·0156029	10·5795296	44
17	9·4209330	9·9843626	9·4365704	10·5634296	10·0156374	10·5790670	43
18	9·4213950	9 9843281	9·4370670	10 5629330	10 0156719	10 5786050	42
19	9·4218566	9 9842935	9 4375631	10 5624369	10·0157065	10·5781434	41
20	9 4223176	9·9842589	9·4380587	10 5619413	10·0157411	10·5776824	40
21	9·4227780	9·9842242	9·4385538	10 5614462	10·0157758	10·5772220	39
22	9·4232380	9·9841895	9·4390485	10 5609515	10·0158105	10·5767620	38
23	9 4236974	9·9841548	9 4395426	10·5604574	10·0158452	10 5763026	37
24	9·4241563	9·9841200	9·4400363	10·5599637	10·0158800	10 5758437	36
25	9 4246147	9·9840852	9 4405295	10 5594705	10·0159148	10·5753853	35
26	9·4250726	9 9840503	9 4410222	10 5589778	10·0159497	10 5749274	34
27	9·4255299	9 9840154	9·4415145	10·5584855	10·0159846	10·5744701	33
28	9·4259867	9 9839805	9·4420062	10·5579938	10 0160195	10·5740133	32
29	9 4264430	9·9839455	9·4424975	10 5575025	10 0160545	10·5735570	31
30	9 4268988	9·9839105	9·4429883	10 5570117	10 0160895	10·5731012	30
		Sine.		Tang		Secant	M

74 *Degrees.*

15 Degrees.

M	Sine.		Tang		Secant		M
30	9·4268988	9·9839105	9·4429883	10·5570117	10·0160895	10 5731012	30
31	9·4273541	9·9838755	9·4434786	10·5565214	10·0161245	10·5726459	29
32	9·4278089	9·9838404	9·4439685	10·5560315	10 0161590	10 5721911	28
33	9·4282631	9 9838052	9·4444579	10·5555421	10 0161948	10 5717369	27
34	9·4287169	9·9837701	9·4449468	10·5550532	10 0162299	10 5712831	26
35	9·4291701	9 9837348	9·4454352	10·5545648	10 0162652	10·5708299	25
36	9·4296228	9·9836996	9·4459232	10·5540768	10·0163004	10 5703772	24
37	9 4300750	9·9836643	9 4464107	10·5535893	10·0163357	10·5699250	23
38	9·4305267	9·9836290	9·4468978	10·5531022	10 0163710	10 5694733	22
39	9·4309779	9·9835936	9·4473843	10·5526157	10·0164064	10·5690221	21
40	9·4314286	9·9835582	9·4478704	10 5521296	10·0164418	10 5685714	20
41	9·4318788	9·9835227	9·4483561	10·5516439	10·0164773	10·5681212	19
42	9·4323285	9·9834872	9 4488413	10·5511587	10·0165128	10·5676715	18
43	9·4327777	9 9834517	9 4493260	10·5506740	10·0165483	10·5672223	17
44	9·4332264	9·9834161	9·4498102	10·5501898	10·0165839	10 5667736	16
45	9·4336746	9·9833805	9·4502940	10·5497060	10·0166195	10·5663254	15
46	9 4341223	9 9833449	9 4507774	10·5492226	10 0166551	10·5658777	14
47	9·4345694	9·9833092	9 4512602	10·5487398	10·0166908	10 5654306	13
48	9·4350161	9·9832735	9 4517427	10·5482573	10·0167265	10·5649839	12
49	9 4354623	9·9832377	9·4522246	10 5477754	10·0167623	10 5645377	11
50	9·4359080	9·9832019	9·4527061	10·5472939	10 0167981	10·5640920	10
51	9·4363532	9·9831661	9 4531872	10·5468128	10 0168339	10·5636468	9
52	9·4367980	9·9831302	9·4536678	10·5463322	10·0168698	10·5632020	8
53	9·4372422	9·9830942	9·4541479	10·5458521	10·0169058	10 5627578	7
54	9·4376859	9·9830583	9·4546276	10·5453724	10·0169417	10·5623141	6
55	9·4381292	9·9830223	9·4551069	10·5448931	10·0169777	10·5618708	5
56	9·4385719	9·9829862	9·4555857	10 5444143	10·0170138	10·5614281	4
57	9·4390142	9·9829501	9·4560641	10·5439359	10 0170499	10·5609858	3
58	9·4394560	9 9829140	9·4565420	10·5434580	10·0170860	10·5605440	2
59	9·4398973	9 9828778	9·4570194	10 5429806	10·0171222	10·5601027	1
60	9·4403381	9·9828416	9·4574964	10·5425036	10·0171586	10·5596619	0
		Sine.		Tang		Secant	M

74 Degrees.

A Table of Artificial Sines,

16 Degrees.

M	Sine.		Tang		Secant		M
0	9·4423381	9·9821416	9·4574764	10·5425036	10·0171584	10·5596619	60
1	9·4427784	9·9821054	9·4577730	10·5422270	10·0171946	10·5592216	59
2	9·4432182	9·9820691	9·4580691	10·5419309	10·0172309	10·5587818	58
3	9·4436576	9·9820328	9·4583648	10·5416352	10·0172672	10·5583424	57
4	9·4440965	9·9819964	9·4586601	10·5413399	10·0173036	10·5579035	56
5	9·4445349	9·9819600	9·4589549	10·5410451	10·0173400	10·5574651	55
6	9·4449728	9·9819236	9·4592492	10·5407508	10·0173764	10·5570272	54
7	9·4454103	9·9818871	9·4595432	10·5404568	10·0174129	10·5565897	53
8	9·4458472	9·9818506	9·4598367	10·5401633	10·0174494	10·5561528	52
9	9·4462837	9·9818140	9·4601297	10·5398703	10·0174860	10·5557163	51
10	9·4467197	9·9817774	9·4604223	10·5395777	10·0175226	10·5552803	50
11	9·4471553	9·9817408	9·4607145	10·5392855	10·0175592	10·5548447	49
12	9·4475904	9·9817041	9·4610063	10·5389937	10·0175959	10·5544096	48
13	9·4480250	9·9816674	9·4612976	10·5387024	10·0176326	10·5539750	47
14	9·4484591	9·9816306	9·4615885	10·5384115	10·0176694	10·5535409	46
15	9·4488927	9·9815938	9·4618790	10·5381210	10·0177062	10·5531073	45
16	9·4493259	9·9815569	9·4621690	10·5378310	10·0177431	10·5526741	44
17	9·4497586	9·9815201	9·4624586	10·5375414	10·0177799	10·5522414	43
18	9·4501909	9·9814831	9·4627478	10·5372522	10·0178169	10·5518091	42
19	9·4506227	9·9814462	9·4630365	10·5369635	10·0178538	10·5513773	41
20	9·4510540	9·9814092	9·4633248	10·5366752	10·0178908	10·5509460	40
21	9·4514849	9·9813721	9·4636127	10·5363873	10·0179279	10·5505151	39
22	9·4519153	9·9813351	9·4639002	10·5360998	10·0179649	10·5500847	38
23	9·4523452	9·9812979	9·4641873	10·5358127	10·0180021	10·5496548	37
24	9·4527747	9·9812608	9·4644739	10·5355261	10·0180392	10·5492253	36
25	9·4532037	9·9812236	9·4647601	10·5352399	10·0180764	10·5487963	35
26	9·4536322	9·9811863	9·4650459	10·5349541	10·0181137	10·5483678	34
27	9·4540603	9·9811490	9·4653312	10·5346688	10·0181510	10·5479397	33
28	9·4544879	9·9811117	9·4656162	10·5343838	10·0181883	10·5475121	32
29	9·4549151	9·9810741	9·4659007	10·5340993	10·0182256	10·5470849	31
30	9·4553418	9·9810370	9·4661848	10·5338152	10·0182630	10·5466582	30
M	Sine.		Tang.		Secant		M

73 Degrees.

16 Degrees.

M	Sine.		Tang		Secant		M
30	9·4533418	9·9817370	9·4716048	10·5283952	10·0 82630	10·5466582	30
31	9·4537681	9·9816995	9·4720885	10·5279115	10·0183005	10·5462319	29
32	9·4541939	9·9816620	9·4725318	10·5274682	10·0183380	10·5458061	28
33	9·4546192	9·9816245	9·4729747	10·5270253	10·0183755	10·5453808	27
34	9·4550441	9·9815870	9·4734171	10·5265829	10·0184130	10·5449559	26
35	9·4554686	9·9815494	9·4738592	10·5261408	10·0184506	10·5445314	25
36	9·4558926	9·9815117	9·4743008	10·5256992	10·0184883	10·5441074	24
37	9·4563161	9·9814740	9·4748421	10·5251579	10·0185260	10·5436839	23
38	9·4567392	9·9814363	9·4753029	10·5246971	10·0185637	10·5432608	22
39	9·4571618	9·9813986	9·4757633	10·5242367	10·0186014	10·5428382	21
40	9·4575840	9·9813608	9·4762233	10·5237767	10·0186392	10·5424160	20
41	9·4580058	9·9813229	9·4766829	10·5233171	10·0186771	10·5419942	19
42	9·4584271	9·9812850	9·4771421	10·5228579	10·0187150	10·5415729	18
43	9·4588480	9·9812471	9·4776009	10·5223991	10·0187529	10·5411520	17
44	9·4592684	9·9812091	9·4780592	10·5219408	10·0187909	10·5407316	16
45	9·4596884	9·9811711	9·4785172	10·5214828	10·0188289	10·5403116	15
46	9·4601079	9·9811331	9·4789748	10·5210252	10·0188669	10·5398921	14
47	9·4605270	9·9810950	9·4794319	10·5205681	10·0189050	10·5394730	13
48	9·4609456	9·9810569	9·4798887	10·5201113	10·0189431	10·5390544	12
49	9·4613638	9·9810187	9·4803451	10·5196549	10·0189813	10·5386362	11
50	9·4617816	9·9809805	9·4808011	10·5191989	10·0190195	10·5382184	10
51	9·4621989	9·9809423	9·4812566	10·5187434	10·0190577	10·5378011	9
52	9·4626158	9·9809040	9·4817118	10·5182882	10·0190960	10·5373842	8
53	9·4630323	9·9808657	9·4821666	10·5178334	10·0191343	10·5369677	7
54	9·4634483	9·9808273	9·4826210	10·5173790	10·0191727	10·5365517	6
55	9·4638639	9·9807889	9·4830750	10·5169250	10·0192111	10·5361361	5
56	9·4642790	9·9807505	9·4835286	10·5164714	10·0192495	10·5357210	4
57	9·4646938	9·9807120	9·4839818	10·5160182	10·0192880	10·5353062	3
58	9·4651081	9·9806735	9·4844346	10·5155654	10·0193265	10·5348919	2
59	9·4655219	9·9806349	9·4848870	10·5151130	10·0193651	10·5344781	1
60	9·4659353	9·9805963	9·4853390	10·5146610	10·0194037	10·5340647	0
M		Sine.		Tang		Secant	M

73 Degrees.

A Table of Artificial Sines,

17 Degrees.

M	Sine.		Tang		Secant		
0	9·4659353	9·9805963	9·4853390	10·5146610	10·0194037	10·5340647	60
1	9·4663483	9·9805577	9·4857907	10·5142093	10·0194423	10·5336517	59
2	9·4667609	9·9805190	9·4862419	10·5137581	10·0194810	10·5332391	58
3	9·4671730	9·9804803	9·4866926	10·5133072	10·0195197	10·5328270	57
4	9·4675848	9·9804415	9·4871433	10·5128567	10·0195585	10·5324152	56
5	9·4679960	9·9804027	9·4875933	10·5124067	10·0195973	10·5320040	55
6	9·4684069	9·9803639	9·4880432	10·5119570	10·0196361	10·5315931	54
7	9·4688173	9·9803250	9·4884924	10·5115076	10·0196750	10·5311827	53
8	9·4692273	9·9802860	9·4889413	10·5110587	10·0197140	10·5307727	52
9	9·4696369	9·9802471	9·4893898	10·5106102	10·0197529	10·5303631	51
10	9·4702461	9·9802081	9·4898380	10·5101620	10·0197919	10·5299539	50
11	9·4704548	9·9801690	9·4902858	10·5097142	10·0198310	10·5295452	49
12	9·4708631	9·9801299	9·4907332	10·5092668	10·0·98701	10·5291369	48
13	9·4712710	9·9800908	9·4911802	10·5088198	10·0199092	10·5287290	47
14	9·4716785	9·9800516	9·4916269	10·5083731	10·0199484	10·5283215	46
15	9·4720856	9·9800124	9·4920731	10·5079269	10·0199876	10·5279144	45
16	9·4724922	9·9799732	9·4925190	10·5074810	10·0200268	10·5275078	44
17	9·4728985	9·9799339	9·4929646	10·5070354	10·0200661	10·5271015	43
18	9·4733043	9·9798946	9·4934097	10·5065903	10·0201054	10·5266957	42
19	9·4737097	9·9798552	9·4938545	10·5061455	10·0201448	10·5262903	41
20	9·4741146	9·9798158	9·4942988	10·5057012	10·0201842	10·5258854	40
21	9·4745192	9·9797764	9·4947429	10·5052571	10·0202236	10·5254808	39
22	9·4749234	9·9797369	9·4951865	10·5048135	10·0202631	10·5250766	38
23	9·4753271	9·9796973	9·4956298	10·5043702	10·0203027	10·5246729	37
24	9·4757304	9·9796578	9·4960727	10·5039273	10·0203422	10·5242696	36
25	9·4761334	9·9796182	9·4965152	10·5034848	10·0203818	10·5238666	35
26	9·4765359	9·9795785	9·4969574	10·5030426	10·0204215	10·5234641	34
27	9·4769380	9·9795388	9·4973991	10·5026009	10·0204612	10·5230620	33
28	9·4773396	9·9794991	9·4978406	10·5021594	10·0205009	10·5226604	32
29	9·4777409	9·9794593	9·4982816	10·5017184	10·0205407	10·5222591	31
30	9·4781418	9·9794195	9·4987223	10·5012777	10·0205805	10·5218582	30
M		Sine.		Tang.		Secant	M

72 Degrees.

17 Degrees.

M	Sine.		Tang		Secant		M
30	9 4781418	9 9734195	9·4987223	10·5012777	10·0265805	10·5218582	30
31	9·4785423	9·9733796	9·4991626	10·5008374	10·0266204	10 5214577	29
32	9·4789423	9·9733398	9·4996026	10·5003974	10·0266602	10 5210577	28
33	9·4793420	9·9732999	9 5000422	10·4999578	10 0267002	10·5206580	27
34	9 4797412	9·9732593	9·5004814	10 4995186	10·0267402	10·5201588	26
35	9·4801401	9·9732198	9·5009203	10 4990797	10·0267802	10 5198599	25
36	9·4805385	9·9731798	9·5013588	10 4986412	10 0268202	10·5194615	24
37	9 4809366	9·9731397	9 5017969	10·4982031	10·0268603	10·5190634	23
38	9 4813342	9 9730996	9·5022347	10·4977653	10 0269004	10·5186658	22
39	9·4817315	9 9730594	9·5026721	10·4973279	10·0269406	10·5182685	21
40	9·4821283	9 9730192	9·5031092	10·4968908	10 0269808	10·5178717	20
41	9·4825248	9·9789789	9·5035459	10·4964541	10 0210211	10·5174752	19
42	9·4829208	9·9789386	9·5039822	10·4960178	10·0210614	10·5170792	18
43	9 4833165	9 9788983	9·5044182	10·4955818	10·0211017	10·5166835	17
44	9·4837117	9·9788579	9·5048538	10·4951462	10 0211421	10 5162883	16
45	9·4841066	9·9788175	9·5052891	10 4947109	10·0211825	10 5158934	15
46	9 4845010	9·9787770	9·5057240	10 4942760	10·0212230	10·5154990	14
47	9 4848951	9·9787365	9·5061586	10 4938414	10·0212635	10·5151049	13
48	9·4852888	9·9786960	9·5065928	10·4934072	10·0213040	10·5147112	12
49	9·4856820	9 9786554	9·5070267	10·4 29733	10·0213446	10·5143180	11
50	9·4860749	9 9786148	9·5074602	10·4925398	10 0213852	10·5139251	10
51	9·4864674	9·9785741	9·5078933	10·4921067	10·0214259	10 5135326	9
52	9·4868594	9·9785334	9 5083261	10·4916739	10·0214666	10 5131405	8
53	9 4872512	9·9784927	9·50 7586	10·4912414	10 0215073	10·5127488	7
54	9·4876426	9 9784519	9·5091927	10·4908093	10 0215481	10·5123574	6
55	9·4880335	9·9784111	9·5096224	10 4903776	10 0215889	10 5119665	5
56	9·4884240	9 9783702	9·5100519	10 4899161	10 0216298	10·5115760	4
57	9 4888142	9·9783293	9·5104849	10·4895151	10·0216707	10·5111858	3
58	9·4892040	9·9782883	9 5109156	10·48 90844	10·0217117	10·5107960	2
59	9·4895934	9·9782474	9 5113460	10·4886540	10 0217526	10 5104066	1
60	9·4899824	9·9782063	9 5117760	10·4882240	10 0217937	10·5100176	0
M		Sine.		Tang		Secant	M

72 Degrees.

A Table of Artificial Sines,

18 Degrees.

M	Sine.		Tang		Secant		M
0	9·4899824	9·9782562	9·5117760	10·4882240	10 0117937	10 5100176	60
1	9·4903710	9·9781653	9·5126057	10 4877943	10·0118347	10·5096290	59
2	9·4907592	9·9781241	9·5126351	10·4873649	10·0118759	10·5092408	58
3	9·4911471	9·9780830	9·5130641	10·4869359	10·0119170	10 5088529	57
4	9·4915345	9·9780418	9·5134927	10·4865073	10 0119582	10 5084655	56
5	9·4919216	9·9780006	9·5139210	10·4860790	10·0119994	10·5080784	55
6	9·4923083	9·9779593	9·5143490	10·4856510	10 0120407	10 5076917	54
7	9·4926946	9·9779180	9·5147766	10 4852234	10 0120820	10·5073054	53
8	9·4930806	9 9778766	9·5152039	10 4847961	10·0121233	10·5069194	52
9	9 4934661	9 9778353	9 5156309	10·4843691	10·0121647	10 5065339	51
10	9·4938513	9·9777938	9 5160575	10 4839425	10·0122062	10·5061487	50
11	9·4942361	9·9777523	9·5164838	10·4835162	10 0122477	10·5057639	49
12	9 4946205	9·9777108	9 5169097	10·4830903	10·0122892	10 5053795	48
13	9·4950046	9 9776693	9·5173353	10·4826647	10·0123307	10·5049954	47
14	9·4953883	9·9776277	9 5177606	10·4822394	10·0123723	10 5046117	46
15	9·4957716	9·9775860	9·5181855	10·4818145	10·0124140	10 5042284	45
16	9 4961545	9·9775444	9·5186101	10 4813899	10·0124556	10·5038455	44
17	9·4965370	9·9775026	9·5190344	10·4809656	10 0124974	10 5034630	43
18	9·4969192	9·9774609	9 5194583	10·4805417	10 0125391	10 5030808	42
19	9·4973010	9·9774191	9·5198819	10·4801181	10 0125809	10 5026990	41
20	9 4976824	9 9773772	9·5203052	10 4796948	10 0126226	10·5023176	40
21	9 4980635	9·9773354	9·5207282	10·4792718	10·0126646	10·5019365	39
22	9 4984442	9 9772934	9·5211508	10·4788492	10·0127066	10 5015558	38
23	9·4988245	9·9772515	9 5215730	10 4784270	10 0127485	10·5011755	37
24	9 4992045	9 9772095	9·5219950	10 4780050	10·0127905	10·5007955	36
25	9·4995840	9·9771674	9 5224166	10·4775834	10 0128326	10·5004160	35
26	9·4999632	9·9771253	9·5228379	10·4771621	10 0128747	10·5000367	34
27	9 5003421	9·9770832	9·5232589	10·4767411	10·0129168	10·4996579	33
28	9·5007206	9·9770410	9 5236795	10·4763205	10·0129590	10·4992794	32
29	9·5010987	9·9769988	9 5240999	10·4759001	10·0130012	10 4989013	31
30	9·5014764	9·9769566	9·5245199	10·4754801	10·0130434	10·4985236	30
		Sine.		Tang.		Secant	M

71 Degrees.

18 *Degrees.*

M	Sine.		Tang		Secant		
30	9.5014764	9.9769566	9.5245199	10.4754801	10.0230434	10.4985236	30
31	9.5018538	9.8769143	9.5249395	10.4750605	10.0230857	10.4981462	29
32	9.5022308	9.9768720	9.5253589	10.4746411	10.0231280	10.4977692	28
33	9.5026075	9.9768296	9.5257779	10.4742221	10.0231704	10.4973925	27
34	9.5029838	9.9767872	9.5261966	10.4738034	10.0232128	10.4970162	26
35	9.5033598	9.9767447	9.5266150	10.4733850	10.0232553	10.4966403	25
36	9.5037353	9.9767022	9.5270331	10.4729669	10.0232978	10.4962647	24
37	9.5041105	9.9766597	9.5274508	10.4725492	10.0233403	10.4958895	23
38	9.5044853	9.9766171	9.5278682	10.4721318	10.0233829	10.4955147	22
39	9.5048598	9.9765745	9.5282853	10.4717142	10.0234255	10.4951402	21
40	9.5052339	9.9765318	9.5287021	10.4712979	10.0234682	10.4947661	20
41	9.5056077	9.9764891	9.5291186	10.4708814	10.0235109	10.4943923	19
42	9.5059811	9.9764464	9.5295347	10.4704653	10.0235536	10.4940189	18
43	9.5063542	9.9764036	9.5299505	10.4700495	10.0235964	10.4936458	17
44	9.5067269	9.9763608	9.5303661	10.4696339	10.0236392	10.4932731	16
45	9.5070992	9.9763179	9.5307813	10.4692187	10.0236821	10.4929008	15
46	9.5074712	9.9762750	9.5311961	10.4688039	10.0237250	10.4925288	14
47	9.5078428	9.9762321	9.5316107	10.4683893	10.0237679	10.4921572	13
48	9.5082141	9.9761891	9.5320250	10.4679750	10.0238109	10.4917859	12
49	9.5085850	9.9761461	9.5324389	10.4675611	10.0238539	10.4914150	11
50	9.5089556	9.9761030	9.5328526	10.4671474	10.0238970	10.4910444	10
51	9.5093258	9.9760599	9.5332659	10.4667341	10.0239401	10.4906742	9
52	9.5096956	9.9760167	9.5336789	10.4663211	10.0239833	10.4903044	8
53	9.5100651	9.9759736	9.5340916	10.4659084	10.0240264	10.4899349	7
54	9.5104343	9.9759303	9.5345040	10.4654960	10.0240697	10.4895657	6
55	9.5108031	9.9758870	9.5349161	10.4650839	10.0241130	10.4891969	5
56	9.5111716	9.9758437	9.5353278	10.4646722	10.0241563	10.4888284	4
57	9.5115397	9.9758004	9.5357393	10.4642607	10.0241996	10.4884603	3
58	9.5119074	9.9757570	9.5361505	10.4638495	10.0242430	10.4880926	2
59	9.5122749	9.9757135	9.5365613	10.4634387	10.0242865	10.4877251	1
60	9.5126419	9.9756701	9.5369719	10.4630281	10.0243299	10.4873581	0
		Sine.		Tang		Secant	M

71 *Degrees.*

A Table of Artificial Sines,

19 Degrees.

M	Sine.		Tang		Secant		M
0	9·5126419	9·9756701	9·5369719	10·4630281	10·0243293	10·4873581	60
1	9·5130086	9·9756265	9·5373821	10·4626179	10·0243735	10·4869914	59
2	9·5133750	9·9755830	9·5377920	10·4622080	10·0244170	10·4866250	58
3	9·5137410	9·9755394	9·5382017	10·4617983	10·0244606	10·4862590	57
4	9·5141067	9·9754957	9·5386110	10·4613890	10·0245403	10·4858933	56
5	9·5144721	9·9754521	9·5390200	10·4609800	10·0245479	10·4855279	55
6	9·5148371	9·9754083	9·5394287	10·4605713	10·0245917	10·4851623	54
7	9·5152017	9·9753646	9·5398371	10·4601629	10·0246354	10·4847983	53
8	9·5155660	9·9753208	9·5402453	10·4597547	10·0246792	10·4844340	52
9	9·5159300	9·9752769	9·5406531	10·4593469	10·0247231	10·4840700	51
10	9·5162936	9·9752330	9·5410606	10·4589394	10·0247670	10·4837064	50
11	9·5166569	9·9751891	9·5414678	10·4585322	10·0248109	10·4833431	49
12	9·5170198	9·9751451	9·5418747	10·4581253	10·0248549	10·4829802	48
13	9·5173824	9·9751011	9·5422813	10·4577187	10·0248989	10·4826176	47
14	9·5177447	9·9750570	9·5426877	10·4573123	10·0249430	10·4822553	46
15	9·5181066	9·9750129	9·5430937	10·4569063	10·0249871	10·4818934	45
16	9·5184682	9·9749688	9·5434994	10·4565006	10·0250312	10·4815318	44
17	9·5188295	9·9749246	9·5439048	10·4560952	10·0250754	10·4811705	43
18	9·5191904	9·9748804	9·5443100	10·4556900	10·0251196	10·4808096	42
19	9·5195510	9·9748361	9·5447148	10·4552852	10·0251639	10·4804490	41
20	9·5199112	9·9747918	9·5451193	10·4548807	10·0252082	10·4800888	40
21	9·5202711	9·9747475	9·5455236	10·4544764	10·0252525	10·4797289	39
22	9·5206307	9·9747031	9·5459276	10·4540724	10·0252969	10·4793693	38
23	9·5209899	9·9746587	9·5463312	10·4536688	10·0253413	10·4790101	37
24	9·5213488	9·9746142	9·5467346	10·4532654	10·0253858	10·4786512	36
25	9·5217074	9·9745697	9·5471377	10·4528623	10·0254303	10·4782926	35
26	9·5220656	9·9745252	9·5475405	10·4524595	10·0254748	10·4779344	34
27	9·5224235	9·9744806	9·5479430	10·4520570	10·0255194	10·4775765	33
28	9·5227811	9·9744359	9·5483452	10·4516548	10·0255641	10·4772189	32
29	9·5231383	9·9743913	9·5487471	10·4512529	10·0256087	10·4768617	31
30	9·5234953	9·9743466	9·5491487	10·4508513	10·0256534	10·4765047	30
M		Sine.		Tang.		Secant	M

70 Degrees.

19 Degrees.

M	Sine.		Tang.		Secant		M
30	9·5234913	9·9743466	9·5491487	10·4508513	10·0256534	10·4765047	30
31	9·5238518	9·9743018	9·5495500	10·4504500	10·0256982	10·4761482	29
32	9·5242081	9·9742570	9·5499511	10·4500489	10·0257430	10·4757919	28
33	9·5245640	9·9742122	9·5503519	10·4496481	10·0257878	10·4754360	27
34	9·5249196	9·9741673	9·5507523	10·4492477	10·0258327	10·4750804	26
35	9·5252749	9·9741224	9·5511525	10·4488475	10·0258776	10·4747251	25
36	9·5256298	9·9740774	9·5515524	10·4484476	10·0259226	10·4743702	24
37	9·5259844	9·9740324	9·5519521	10·4480479	10·0259676	10·4740156	23
38	9·5263387	9·9739873	9·5523514	10·4476486	10·0260127	10·4736613	22
39	9·5266927	9·9739422	9·5527504	10·4472496	10·0260578	10·4733073	21
40	9·5270463	9·9738971	9·5531492	10·4468508	10·0261029	10·4729537	20
41	9·5273997	9·9738519	9·5535477	10·4464523	10·0261481	10·4726003	19
42	9·5277526	9·9738067	9·5539459	10·4460541	10·0261933	10·4722474	18
43	9·5281053	9·9737615	9·5543438	10·4456562	10·0262385	10·4718947	17
44	9·5284577	9·9737162	9·5547415	10·4452585	10·0262838	10·4715423	16
45	9·5288097	9·9736709	9·5551388	10·4448612	10·0263291	10·4711903	15
46	9·5291614	9·9736255	9·5555359	10·4444641	10·0263745	10·4708386	14
47	9·5295128	9·9735801	9·5559327	10·4440673	10·0264199	10·4704872	13
48	9·5298638	9·9735346	9·5563292	10·4436708	10·0264654	10·4701362	12
49	9·5302146	9·9734891	9·5567255	10·4432745	10·0265109	10·4697854	11
50	9·5305650	9·9734435	9·5571214	10·4428786	10·0265565	10·4694350	10
51	9·5309151	9·9733980	9·5575171	10·4424829	10·0266020	10·4690849	9
52	9·5312649	9·9733523	9·5579125	10·4420875	10·0266477	10·4687351	8
53	9·5316143	9·9733067	9·5583077	10·4416923	10·0266933	10·4683857	7
54	9·5319635	9·9732610	9·5587025	10·4412975	10·0267390	10·4680365	6
55	9·5323123	9·9732152	9·5590971	10·4409029	10·0267848	10·4676877	5
56	9·5326608	9·9731694	9·5594914	10·4405086	10·0268306	10·4673392	4
57	9·5330090	9·9731236	9·5598854	10·4401146	10·0268764	10·4669910	3
58	9·5333569	9·9730777	9·5602792	10·4397208	10·0269223	10·4666431	2
59	9·5337044	9·9730318	9·5606727	10·4393273	10·0269682	10·4662956	1
60	9·5340517	9·9729858	9·5610659	10·4389341	10·0270142	10·4659483	0
		Sine.		Tang.		Secant	M

70 Degrees.

A Table of Artificial Sines,

20 Degrees.

M	Sine.		Tang		Secant		M
0	9·5342517	9·9729818	9·5612699	10·4389341	10 0270142	10·4659483	60
1	9·5343986	9 9729393	9·5614588	10 4385412	10 0270602	10·4656014	59
2	9·5347452	9·9728938	9·5618515	10·4381485	10 0271062	10·4652548	58
3	9·5350915	9 9728477	9·5622439	10.4377561	10·0271523	10·4649085	57
4	9·5354375	9 9728016	9·5626360	10·4373040	10 0271984	10.4645623	56
5	9·5357832	9·9727554	9·5630278	10.4369722	10 0272446	10·.642160	55
6	9 5361286	9 9727092	9·5634194	10·4365806	10 0272908	10·4638714	54
7	9·5364737	9 9726629	9 5638107	10 4361893	10 0273371	10.4635263	53
8	9 5368184	9·9726166	9·5642018	10·4357982	10 0273834	10.4631816	52
9	9·5371628	9·9725703	9·5645925	10.4354075	10·0274297	10·4628372	51
10	9·5375070	9·9725239	9 5649831	10 4350169	10·0274761	10 4624930	50
11	9·5378508	9·9724775	9 5653733	10·4346267	10·0275225	10 4621492	49
12	9·5381943	9·9724310	9 5657633	10 4342367	10 0275690	10·4618057	48
13	9 5385375	9·9723845	9·5661530	10·4338470	10·0276155	10·4614625	47
14	9 5388804	9·9723380	9 5665424	10·4334576	10·0276620	10·4611196	46
15	9·5392230	9·9722914	9·5669316	10·4330684	10 0277086	10 4607770	45
16	9 5395653	9·9722448	9·5673205	10·4326795	10·0277552	10 4604347	44
17	9·5399073	9·9721981	9·5677091	10 4322909	10·0278019	10·4600927	43
18	9·5402489	9·9721514	9·5680975	10 4319025	10 0278486	10 4597511	42
19	9 5405903	9·9721047	9·5684856	10 4315144	10 0278953	10·4594097	41
20	9·5407314	9·9720579	9·5688735	10·4311265	10 0279421	10 4590686	40
21	9·5412721	9·9720110	9·5692611	10·4307389	10·0279890	10·4587279	39
22	9·5416126	9·9719642	9 5696488	10·4303510	10·0280358	10 4583874	38
23	9·5419527	9·9719172	9·5700355	10 4299645	10·0280828	10·4580473	37
24	9·5422926	9·9718703	9·5704223	10·4295777	10·0281297	10 4577074	36
25	9 5426321	9·9718233	9·5708088	10 4291912	10 0281767	10 4573679	35
26	9·5429713	9·9717762	9·5711951	10 4288049	10·0282238	10 4570287	34
27	9·5433103	9·9717291	9·5815811	10·4284189	10 0282709	10·456.897	33
28	9·5436489	9·9716820	9 5719669	10·4280331	10·0283180	10·4563511	32
29	9·5439873	9·9716348	9 5723524	10·4276476	10 0283652	10·4560127	31
30	9·5443253	9·9715876	9·5727377	10·4272623	10·0284124	10 4556747	30
		Sine.		Tang.		Secant	M

69 Degrees.

20 Degrees.

M	Sine.		Tang		Secant		
30	9·5443253	9 9715876	9·5727377	10·4272623	10·0284124	10·4556747	30
31	9 5446630	9 9715404	9·5731227	10·4268773	10 0284596	10·4553370	29
32	9·5450005	9 9714931	9·5735074	10·4264926	10·0285069	10·4549995	28
33	9·5453376	9·9714457	9·5738919	10 4261081	10·0285543	10·4546624	27
34	9·5456745	9 9713984	9 5742761	10 4257239	10·0286016	10 4543255	26
35	9·5460110	9 9713509	9·5746601	10·4253399	10 0286491	10 4539890	25
36	9·5463472	9·9713035	9 5750438	10·4249562	10·0286965	10·4536528	24
37	9·5466832	9·9712560	9·5754272	10·4245728	10·0287440	10·4533168	23
38	9·5470189	9·9712084	9 5758104	10 4241896	10·0287916	10·4529811	22
39	9·5473542	9,9711608	9 5761934	10 4238066	10·0288392	10·4526458	21
40	9·5476893	9 9711132	9 5765761	10 4234239	10 0288868	10 4523107	20
41	9 5480240	9·9710655	9 5769585	10 4230415	10·0289345	10 4519760	19
42	9·5483585	9·9710178	9·5773407	10·4226593	10·0289822	10·4516415	18
43	9·5486927	9·9709701	9·5777226	10·4222774	10 0290299	10·4513073	17
44	9·5490266	9·9709223	9·5781043	10·4218957	10·0290777	10·4509734	16
45	9·5493602	9 9708744	9·5784858	10 4215142	10·0291256	10·4506398	15
46	9 5496935	9·9708265	9·5788669	10·4211331	10 0291735	10·4503065	14
47	9·5500265	9·9707786	9 5792479	10.4207521	10·0292214	10.4499735	13
48	9·5503592	9 9707306	9·5796286	10·4203714	10·0292694	10·4496408	12
49	9 5506916	9 9706826	9·5800090	10·4199910	10·0293174	10 4493084	11
50	9·5510237	9·9706346	9·5803892	10 4196108	10 0293654	10 4489763	10
51	9·5513556	9·9705865	9·5807691	10 4192309	10·0294135	10 4486444	9
52	9 5516871	9 9705383	9 5811488	10·4188512	10·0294617	10·4483129	8
53	9·5520184	9·9704902	9 5815282	10·4184718	10·0295098	10·4479816	7
54	9·5523494	9·9704419	9·5819074	10·4180926	10·0295581	10·4476506	6
55	9·5526801	9·9703937	9 5822864	10·4177136	10·0296062	10·4473199	5
56	9·5530105	9·9703454	9·5826651	10·4173349	10 0296546	10·4469895	4
57	9·5533406	9·9702970	9 5830435	10.4169565	10·0297030	10 4466593	3
58	9 5536704	9·9702486	9 5834217	10·4165783	10 0297514	10·4463296	2
59	9·5539999	9 9702002	9·5837997	10·4162003	10·0297998	10 4460001	1
60	9 5543292	9·9701517	9·5841774	10·4158226	10 0298483	10·4456708	0
		Sine.		Tang		Secant	M

69 Degrees.

A Table of Artificial Sines,

21 Degrees.

M	Sine.		Tang		Secant		
0	9 5543292	9 9701617	9·5841774	10·4158226	10 0298483	10 4456705	60
1	9 5546581	9·9701032	9 5845549	10·4154451	10 0298968	10 4453419	59
2	9 5549868	9 9700547	9·5849321	10·4150679	10 0299453	10 4450132	58
3	9·5553152	9·9700061	9·5853091	10·4146909	10·0299939	10·4446848	57
4	9·5556433	9·9699574	9·5856859	10·4143141	10·0300426	10·4443567	56
5	9·5559711	9·9699087	9 5860624	10 4139376	10·0300913	10·4440289	55
6	9·5562987	9 9698600	9·5864386	10·4135614	10·0301400	10·4437013	54
7	9 5566259	9 9698112	9·5868147	10 4131853	10 0301888	10 4433741	53
8	9·5569529	9·9697624	9 5871904	10 4128096	10 0302376	10·4430471	52
9	9 5572796	9·9697136	9 5875660	10·4124340	10 0302864	10 4427204	51
10	9·5576060	9·9696647	9·5879413	10 4120587	10·0303352	10·4423940	50
11	9 5579321	9·9696158	9·5883163	10 4116837	10 0303842	10·4420679	49
12	9·5582579	9·9695668	9 5886911	10·4113088	10·0304332	10·4417421	48
13	9·5585835	9 9695177	9·5890657	10 4109343	10·0304823	10 4414165	47
14	9 5589088	9 9694687	9·5894401	10·4105599	10 0305313	10·4410912	46
15	9·5592338	9·9694196	9 5898142	10 4101858	10·0305804	10 4407662	45
16	9·5595585	9·9693704	9 5901881	10·4098119	10 0306296	10·4404415	44
17	9 5598829	9·9693212	9 5905617	10 4094383	10·0306788	10·4401171	43
18	9·5602071	9 9692720	9·5909351	10·4090649	10·0307280	10·4397929	42
19	9 5605310	9·9692227	9·5913082	10 4086918	10·0307773	10·4394690	41
20	9·5608546	9·9691734	9·5916812	10·4083188	10·0308266	10·4391454	40
21	9·5611779	9·9691240	9·5920539	10·4079461	10 0308759	10·4388221	39
22	9·5615010	9 9690746	9 5924263	10 4075737	10·0309254	10 4384990	38
23	9·5618237	9·9690252	9·5927985	10·4072015	10·0309748	10·4381763	37
24	9·5621462	9·9689757	9·5931705	10 4068295	10·0310243	10·4378538	36
25	9·5624685	9·9689262	9 5935423	10 4064577	10 0310738	10·4375315	35
26	9 5627904	9 9688766	9·5939138	10·4060862	10 0311234	10·4372096	34
27	9 5631121	9 9688270	9·5942851	10·4057149	10 0311730	10·4368879	33
28	9·5634335	9·9687773	9·5946561	10 4053439	10 0312227	10 4365665	32
29	9·5637546	9 9687276	9 5950269	10·4049731	10·0312724	10·4362454	31
30	9·5640754	9·9686779	9 5953975	10·4046025	10 0313221	10 4359246	30
		Sine.		Tang.		Secant	M

68 Degrees.

21 Degrees.

M	Sine.		Tang		Secant		M
30	9 5642754	9.9683779	9.5953975	10.4046025	10.0313221	10 4359246	30
31	9.5643960	9.9686281	9.5957679	10 4042321	10 0313719	10.4356040	29
32	9.5647163	9.9685783	9.5961380	10 4038620	10 0314217	10.4352837	28
33	9.5650363	9 9685284	9.5965079	10 4034921	10 0314716	10.4349637	27
34	9.5653561	9.9684785	9.5968776	10.4031224	10.0315215	10 4346439	26
35	9.5656756	9.9684286	9 5972470	10.4027530	10.0315714	10 4343244	25
36	9.5659948	9.9683786	9.5976162	10.4023838	10.0316214	10.4340052	24
37	9.5663137	9.9683285	9.5979852	10.4020148	10.0316715	10.4336863	23
38	9.5666324	9.9682784	9 5983540	10.4016460	10.0317216	10.4333676	22
39	9.5669508	9 9682283	935987225	10.4012775	10 0317717	10.4330492	21
40	9.5672689	9.9681781	9 5990908	10.4009092	10.0318219	10.4327311	20
41	9 5675868	9.9681279	9 5994588	10.4005411	10.0318721	10 4324132	19
42	9.5679044	9.9680777	9.5998267	10 4001733	10 0319223	10.4320956	18
43	9.5682217	9.9680274	9.6001943	10.3998057	10.0319726	10.4317783	17
44	9.5685387	9 9679771	9 6005617	10 3994383	10.0320229	10.4314613	16
45	9.5688555	9.9679267	9.6009289	10 3990711	10 0320733	10.4311445	15
46	9.5691721	9 9678763	9.6012958	10.3987042	10.0321237	10.4308279	14
47	9.5694883	9.9678258	9 6016625	10.3983375	10.0321742	10.4305117	13
48	9.5698043	9.9677753	9.6020290	10.3979710	10.0322247	10.4301957	12
49	9.5701200	9.9677247	9.6023953	10 3976047	10.0322753	10.4298800	11
50	9 5704355	9.9676741	9 6027613	10.3972387	10 0323259	10.4295645	10
51	9.5707506	9.9676235	9 6031271	10.3968729	10 0323765	10.4292494	9
52	9.5710656	9.9675728	9 6034927	10.3965073	10.0324272	10.4289344	8
53	9.5713802	9.9675221	9.6038581	10 3961419	10 0324779	10.4286198	7
54	9.5716946	9.9674713	9.6042233	10 3957767	10.0325287	10 4283054	6
55	9.5720087	9 9674205	9.6045882	10.3954118	10 0325795	10.4279913	5
56	9.5723226	9 9673698	9.6049529	10.3950471	10 0326303	10.4276774	4
57	9.5726362	9.9673188	9.6053174	10.3946826	10.0326812	10 4.73638	3
58	9.5729495	9.9672679	9 6056817	10.3943183	10.0327321	10.4270505	2
59	9.5732626	9.9672169	9 6060457	10.3939543	10.0327831	10 4267374	1
60	9.5735754	9.9671659	9 6064096	10.3935904	10.0328341	10.4264246	0
M		Sine.		Tang		Secant	M

68 Degrees.

A Table of Artificial Sines,

22 Degrees.

M	Sine.		Tang		Secant		M
0	9·5735754	9·9671659	9·6064096	10 3935904	10 0328341	10·4264246	60
1	9·5738880	9 9671148	9·6067732	10·3932268	10 0328852	10·4261120	59
2	9·5742003	9 9670637	9·6071366	10 3928634	10·0329363	10 4257997	58
3	9·5745123	9 9670125	9 6074997	10·3925003	10·0329875	10·4254877	57
4	9·5748240	6·9669614	9·6078627	10·3921373	10·0330386	10·4251760	56
5	9·5751356	9·9669101	9·6082254	10·3917746	10·0330899	10·4248644	55
6	9·5754468	9·9668588	9·6085880	10·3914120	10 0331412	10·4245532	54
7	9 5757578	9 9668075	9 6089503	10·3910497	10·0331925	10·4242422	53
8	9 5760685	9 9667562	9·6093124	10·3906876	10·0332438	10·4239315	52
9	9·5763790	9·9667048	9·6096741	10·3903258	10·0332952	10·4236210	51
10	9·5766892	9·9666533	9 6100359	10·3899641	10 0333467	10·4233103	50
11	9 5769991	9·9666018	9·6103973	10·3896027	10 0333982	10·4230009	49
12	9·5773088	9·9665503	9 6107586	10·3892414	10·0334497	10·4226912	48
13	9·5776183	9·9664986	9·6111196	10·3888804	10 0335013	10 4223817	47
14	9·5779275	9·9664471	9 6114804	10·3885196	10 0335529	10·4220725	46
15	9·5782364	9·9663954	9·6118409	10·3881591	10 0336046	10·4217636	45
16	9·5785450	9·9663437	9·6122013	10·3877987	10·0336563	10·4214550	44
17	9 5788535	9·9662920	9·6125615	10·3874385	10 0337080	10·4211465	43
18	9·5791616	9·9662402	9 6129214	10·3870786	10 0337598	10·4208384	42
19	9·5794695	9·9661884	9 6132812	10 3867188	10·0338116	10·4205305	41
20	9 5797772	9·9661365	9 6136407	10·3863593	10 0338635	10·4202228	40
21	9·5800845	9 9660846	9·6140000	10·3860000	10·0339154	10·4199155	39
22	9 5803917	9 9660326	9 6143591	10·3856409	10·0339674	10·4196083	38
23	9 5806986	9·9659806	9·6147180	10·3852820	10·0340194	10·4193014	37
24	9 5810052	9 9659285	9·6150766	10·3849234	10·0340715	10·4189948	36
25	9·5813116	9·9658764	9 6154351	10·3845649	10 0341236	10 4186884	35
26	9·5816177	9·9658243	9·6157934	10·3842066	10·0341757	10 4183823	34
27	9·5819236	9·9657721	9 6161514	10 3838486	10 0342279	10 4180764	33
28	9·5822292	9 9657199	9·6165093	10 3834907	10 0342801	10·4177708	32
29	9·5825345	9·9656677	9·6168669	10 3831331	10·0343323	10 4174655	31
30	9·5828397	9·9656153	9·6172243	10·3827757	10·0343847	10·4171603	30
		Sine		Tang.		Secant	M

67 Degrees.

22 Degrees.

M	Sine.		Tang		Secant		M
30	9·5826397	9·9561153	9·6172243	10·3827757	10·0343847	10·4171603	30
31	9·5831445	9·9555630	9·6178115	10·3824185	10·0344570	10·4168555	29
32	9·5834491	9·9551136	9·6183985	10·3820615	10·0344834	10·4165503	28
33	9·5837535	9·9545632	9·6189853	10·3817047	10·0345418	10·4162465	27
34	9·5840576	9·9540257	9·6195719	10·3813481	10·0345943	10·4159424	26
35	9·5843615	9·9535532	9·6201583	10·3809917	10·0346468	10·4156385	25
36	9·5846651	9·9530305	9·6207445	10·3806355	10·0346994	10·4153349	24
37	9·5849685	9·9524880	9·6213205	10·3802795	10·0347520	10·4150315	23
38	9·5852716	9·9519553	9·6220762	10·3799238	10·0348047	10·4147284	22
39	9·5855745	9·9514226	9·6226318	10·3795682	10·0348574	10·4144255	21
40	9·5858771	9·9508899	9·6231872	10·3792128	10·0349101	10·4141229	20
41	9·5861795	9·9503571	9·6237423	10·3788577	10·0349629	10·4138205	19
42	9·5864816	9·9498243	9·6242974	10·3785026	10·0350157	10·4135184	18
43	9·5867835	9·9492914	9·6248520	10·3781480	10·0350686	10·4132165	17
44	9·5870851	9·9487585	9·6254066	10·3777934	10·0351215	10·4129149	16
45	9·5873865	9·9482256	9·6259609	10·3774391	10·0351744	10·4126135	15
46	9·5876876	9·9476926	9·6265150	10·3770850	10·0352274	10·4123124	14
47	9·5879885	9·9471595	9·6270690	10·3767310	10·0352805	10·4120115	13
48	9·5882892	9·9466265	9·6276227	10·3763773	10·0353335	10·4117108	12
49	9·5885896	9·9460933	9·6281763	10·3760237	10·0353867	10·4114104	11
50	9·5888897	9·9455602	9·6287296	10·3756704	10·0354398	10·4111103	10
51	9·5891897	9·9450269	9·6292827	10·3753173	10·0354931	10·4108103	9
52	9·5894893	9·9444937	9·6298356	10·3749644	10·0355463	10·4105107	8
53	9·5897888	9·9439604	9·6303884	10·3746116	10·0355996	10·4102112	7
54	9·5900880	9·9434270	9·6309409	10·3742591	10·0356530	10·4099120	6
55	9·5903869	9·9428937	9·6314932	10·3739068	10·0357063	10·4096131	5
56	9·5906856	9·9423602	9·6320454	10·3735546	10·0357598	10·4093144	4
57	9·5909841	9·9418268	9·6325973	10·3732027	10·0358132	10·4090159	3
58	9·5912823	9·9412932	9·6331491	10·3728509	10·0358668	10·4087177	2
59	9·5915803	9·9407597	9·6337006	10·3724994	10·0359203	10·4084197	1
60	9·5918780	9·9402261	9·6342519	10·3721481	10·0359739	10·4081220	0
M		Sine.		Tang		Secant	M

67 Degrees.

A Table of Artificial Sines,

23 Degrees.

M	Sine.		Tang		Secant		M
0	9.5918780	9.9640261	9.6278519	10.3721481	10.0359739	10.4081220	60
1	9 5921755	9.9639734	9.6282031	10.3717969	10.0360276	10.4078243	59
2	9.5924728	9 9639187	9.6285540	10.3714460	10.0360813	10.4075272	58
3	9 5927698	9.9638650	9.6289048	10.3710952	10 0361359	10.4072302	57
4	9.5930666	9.9638112	9.6292553	10 3707447	10.0361888	10.4069334	56
5	9.5933631	9.9637574	9.6296057	10 3703943	10.0362426	10.4066369	55
6	9.5936594	9.9637036	9.6299558	10.3700442	10.0362964	10 4063406	54
7	9.5939555	9.9636496	9.6303058	10.3696942	10.0363504	10.4060445	53
8	9.5942513	9.9635957	9.6306556	10 3693443	10.0364043	10.0457487	52
9	9.5945469	9.9635417	9.6310052	10 3689948	10 0364583	10 4054531	51
10	9.5948422	9.9634877	9.6313545	10.3686455	10.0365123	10.4051578	50
11	9.5951373	9 9634336	9 6317037	10.3682963	10 0365664	10.4048627	49
12	9.5954322	9.9633795	9.6320527	10 3679473	10 0366205	10.4045678	48
13	9.5957268	9.9633253	9 6324015	10.3675985	10 0366747	10.4 42732	47
14	9.5960212	9.9632711	9.6327501	10.3672499	10.0367289	10.4039788	46
15	9.5963154	9 9632168	9.6330985	10.3669015	10 0367832	10.4036846	45
16	9 5966093	9 9631625	9.6334468	10.3665532	10 0368375	10.4033907	44
17	9.5969030	9.9631082	9.6337948	10.3662052	10.0368918	10.4030970	43
18	9.5971965	9.9630538	9.6341426	10.3658574	10.0369462	10.4028035	42
19	9.5974897	9.9629994	9.6344903	10.3655097	10 0370006	10 4025103	41
20	9.5977827	9.9629449	9.6348378	10 3651622	10 0370551	10.4022175	40
21	9.5980754	9.9628904	9 6351850	10 3648150	10.0371096	10.4019246	39
22	9.5983680	9.9628358	9.6355321	10 3644679	10 0371642	10 4016321	38
23	9.5986602	9.9627812	9.6358790	10 3641210	10.0372188	10. 4013398	37
24	9.5989523	9 9627266	9.6362257	10 3637743	10 0372734	10.4010477	36
25	9.5992441	9.9626719	9.6365722	10.3634278	10 0373281	10 4007559	35
26	9.5995357	9 9626172	9.6369185	10.3630815	10.0373828	10.4004643	34
27	9.5998270	9.9625624	9.6372646	10 3627354	10 0374376	10.4001730	33
28	9.6001181	9.9625076	9.6376106	10 3623894	10 0374924	10.4998819	32
29	9 6004090	9.9624527	9.6379563	10.3620437	10.0375473	10.4995910	31
30	9.6006997	9.9623978	9.6383019	10.3616981	10.0376022	10.4993003	30
M		Sine.		Tang.		Secant	M

66 Degrees.

23 Degrees.

M	Sine.		Tang		Secant		
30	9 6005937	9 9623978	9.6383219	10.3616981	10 0376022	10.3993023	30
31	9 6009301	9.9623328	9.6386473	10.3613527	10.0376672	10 3990029	29
32	9 6012663	9 9622678	9.6389725	10.3610275	10 0377322	10 3987037	28
33	9 6016023	9 9622028	9 6393375	10.3606625	10.0377972	10 3984047	27
34	9.6018600	9.9621777	9.6396823	10 3603177	10.0378223	10.3981400	26
35	9.6021495	9.9621226	9 6400269	10.3599731	10.0378774	10.3978505	25
36	9 6024788	9.9620574	9 6403714	10.3596286	10 0,79426	10 3975612	24
37	9 6027273	9 9620122	9 6407156	10 3592844	10.0379878	10 3972 22	23
38	9.6030166	9.9619563	9.6410597	10.3589303	10.0380431	10 39-9834	22
39	9.6033052	9 9619.6	9 6414036	10.3585964	10.0380984	10 3966946	21
40	9 6035936	9.9618463	9.6417473	10.3582527	10.0381537	10.3964064	20
41	9 6038817	9 9617909	9.6420908	10.3579092	10 0382091	10.3,61183	19
42	9 6041696	9.96 7355	9 6423342	10 3576658	10 0382645	10 3958304	18
43	9.6044573	9.9616800	9 6427773	10.3572227	10.0383200	10 3955427	17
44	9 6047448	9 9616245	9 6431203	10.3568797	10.0383755	10.3952522	16
45	9 6050320	9.9615683	9 6434631	10.3565370	10.0384311	10.3949680	15
46	9.6053192	9 9615133	9.643 057	10.3561943	10 0384867	10 3946810	14
47	9.6056057	9.9614576	9.6441481	10 3558519	10 0385424	10 3943943	13
48	9.6058923	9.9614020	9 6444901	10.3555097	10.0385980	10.3941077	12
49	9.6061786	9.9613463	9.6448324	10.3551676	10.0.86538	10 3938214	11
50	9 6064647	9.9612904	9 6451743	10.3548257	10.0386096	10 3935353	10
51	9.6067506	9.9612346	9.6455160	10 3544840	10.0387654	10 3932494	9
52	9 6070362	9.9611787	9 6458575	10.3541425	10.0388213	10 3929638	8
53	9 6073216	9.9611228	9.6461988	10 3538012	10.0388772	10 3926784	7
54	9.6076068	9.9610668	9 6465400	10 3534600	10 0389332	10 3923932	6
55	9.6078918	9.9610108	9.6468810	10.3531190	10 0389892	10 3921082	5
56	9.6081765	9.9609548	9 6472217	10.3527.83	10.0390452	10.3918235	4
57	9.6084611	9 9608987	9.6475624	10.3524376	10.0391013	10.3915389	3
58	9.6087454	9.9608426	9.6479028	10.3520972	10 0391574	10 3912546	2
59	9 6090294	9 9607864	9 6482431	10 3517569	10.0392136	10 3909706	1
60	9.6093133	9.9607302	9 6485831	10 3514169	10.0392698	10 3906867	0
M		Sine.		Tang.		Secant	M

66 Degrees.

A Table of Artificial Sines,

24 Degrees.

M	Sine.		Tang		Secant		M
0	9.6093133	9.9607302	9.6485831	10.3514169	10.0392638	10.3906867	60
1	9.6095969	9.9606739	9.6489230	10.3510770	10.0393261	10.3904031	59
2	9.6098803	9.9606176	9.6492628	10.3507372	10.0393824	10.3901197	58
3	9.6101635	9.9605612	9.6496023	10.3503977	10.0394388	10.3898365	57
4	9.6104465	9.9605048	9.6499417	10.3500583	10.0394952	10.3895535	56
5	9.6107293	9.9604484	9.6502809	10.3497191	10.0395516	10.3892707	55
6	9.6110118	9.9603919	9.6506199	10.3493801	10.0396081	10.3889882	54
7	9.6112941	9.9603354	9.6509587	10.3490413	10.0396646	10.3887059	53
8	9.6115762	9.9602788	9.6512974	10.3487026	10.0397212	10.3884238	52
9	9.6118580	9.9602222	9.6516359	10.3483641	10.0397778	10.3881420	51
10	9.6121397	9.9601655	9.6519742	10.3480258	10.0398345	10.3878603	50
11	9.6124211	9.9601088	9.6523123	10.3476877	10.0398912	10.3875789	49
12	9.6127023	9.9600520	9.6526503	10.3473497	10.0399480	10.3872977	48
13	9.6129833	9.9599952	9.6529881	10.3470119	10.0400048	10.3870167	47
14	9.6132641	9.9599384	9.6533257	10.3466743	10.0400616	10.3867359	46
15	9.6135446	9.9598815	9.6536631	10.3463369	10.0401185	10.3864554	45
16	9.6138250	9.9598246	9.6540004	10.3459996	10.0401754	10.3861750	44
17	9.6141051	9.9597676	9.6543375	10.3456625	10.0402324	10.3858949	43
18	9.6143850	9.9597106	9.6546744	10.3453256	10.0402894	10.3856150	42
19	9.6146647	9.9596535	9.6550112	10.3449888	10.0403465	10.3853353	41
20	9.6149441	9.9595964	9.6553477	10.3446523	10.0404036	10.3850559	40
21	9.6152234	9.9595393	9.6556841	10.3443159	10.0404607	10.3847766	39
22	9.6155024	9.9594821	9.6560204	10.3439796	10.0405179	10.3844976	38
23	9.6157812	9.9594248	9.6563564	10.3436436	10.0405752	10.3842188	37
24	9.6160598	9.9593675	9.6566923	10.3433077	10.0406325	10.3839401	36
25	9.6163382	9.9593102	9.6570280	10.3429720	10.0406898	10.3836618	35
26	9.6166164	9.9592528	9.6573636	10.3426364	10.0407472	10.3833836	34
27	9.6168944	9.9591954	9.6576989	10.3423011	10.0408046	10.3831056	33
28	9.6171721	9.9591380	9.6580341	10.3419659	10.0408620	10.3828279	32
29	9.6174496	9.9590805	9.6583692	10.3416308	10.0409195	10.3825504	31
30	9.6177270	9.9590229	9.6587041	10.3412960	10.0409771	10.3822730	30
		Sine		Tang.		Secant	M

65 Degrees.

24 Degrees.

M	Sine.		Tang		Secant		M
30	9 6177270	9·9590229	9·9587041	10·3412960	10 0409771	10 3822730	30
31	9·6180341	9 9589655	9 6590387	10·3409613	10 0410347	10 3819959	29
32	9·6182809	9 9589077	9·6593733	10·3406267	10 0410923	10 3817191	28
33	9·6185576	9·9588500	9·6597076	10·3402924	10·0411500	10·3814424	27
34	9·6188341	9·9587923	9 6600418	10·3399582	10·0412077	10 3811659	26
35	9·6191103	9·9587345	9 6603758	10·3396242	10·0412655	10 3808897	25
36	9 6193864	9·9586767	9 6607097	10·3392903	10·0413233	10 3806136	24
37	9·6196622	9·9586188	9·6610434	10 3389566	10 0413812	10·3803378	23
38	9 6199378	9·9585609	9 6613769	10 3386231	10·0414391	10·3800622	22
39	9 6202132	9·9585030	9 6617103	10 3382897	10·0414970	10·3797868	21
40	9·6204884	9·9584450	9·6620434	10 3379566	10·0415550	10·3795116	20
41	9·6207634	9·9583869	9·6623765	10 3376235	10·0416131	10·3792366	19
42	9 6210382	9·9583288	9·6627093	10·3372907	10 0416712	10 3789618	18
43	9·6213127	9·9582707	9 6630420	10 3369580	10·0417293	10·3786837	17
44	9 6215871	9·9582125	9 6633745	10 3366255	10·0417875	10·3784129	16
45	9·6218612	9·9581543	9·6637069	10·3362931	10 0418457	10 3781388	15
46	9·6221351	9·9580961	9 6640391	10 3359609	10·0419039	10 3778649	14
47	9·6224088	9·9580378	9·6643711	10·3356289	10·0419622	10·3775912	13
48	9·6226824	9·9579794	9·6647030	10 3352970	10·0420206	10·3773176	12
49	9 6229557	9·9579210	9 6650346	10·3349654	10 0420790	10·3770443	11
50	9·6232287	9·9578626	9 6653662	10·3346338	10·0421374	10 3767713	10
51	9 6235016	9·9578041	9·6656975	10·3343025	10·0421959	10·3764984	9
52	9·6237743	9·9577456	9·6660288	10·3339712	10·0422544	10 3762257	8
53	9·6240468	9 9576870	9·6663598	10·3336402	10 0423130	10·3759532	7
54	9·6243190	9 9576284	9·6666907	10·3333093	10·0423716	10·3756810	6
55	9·6245911	9·9575697	9·6670214	10·3329786	10·0424303	10·3754089	5
56	9·6248629	9 9575110	9·6673519	10·3326481	10·0424890	10·3751371	4
57	9·6251346	9·9574522	9·6676823	10·3323177	10·0425478	10·3748654	3
58	9·6254060	9·9573934	9·6680126	10·3319874	10 0426066	10·3745940	2
59	9·6256772	9·9573346	9·6683426	10·3316574	10·0426654	10 3743228	1
60	9·6259483	9·9572757	9 6686725	10·3313275	10 0427243	10·3740517	0
		Sine.		Tang		Secant	M

65 Degrees.

A Table of Artificial Sines,

25 Degrees.

M	Sine.		Tang		Secant		M
0	9.6259483	9.9572757	9.6686725	10 3313275	10.0427243	10.3740517	60
1	9 6262191	9 9572163	9.6690033	10.3309977	10 0427832	10.3737809	59
2	9 6264897	9.9571573	9.6693319	10 3306681	10 0428422	10 3735103	58
3	9.6267601	9.9570988	9 6696613	10.3303387	10.0429012	10.3732399	57
4	9 6270303	9.9570397	9.6699906	10.3300094	10.0429603	10.3729697	56
5	9.6273003	9 9569806	9.6703197	10 3296803	10.0430194	10.3726997	55
6	9.6275701	9.9569215	9 6706486	10.3293514	10.0430785	10.3724299	54
7	9 6278397	9.9568623	9.6709774	10.3290226	10.0431377	10.3721603	53
8	9.6281090	9.9568030	9.6713060	10.3286940	10 0431970	10.3718910	52
9	9 6283782	9 9567437	9.6716345	10 3283655	10.0432563	10.3716218	51
10	9 6286472	9.9566844	9 6719628	10.3280372	10.0433156	10.3713528	50
11	9.6289160	9.9566250	9.6722910	10.3277090	10.0433750	10.3710840	49
12	9.6291845	9.9565656	9.6726190	10 3273810	10.0434344	10.3708155	48
13	9.6294529	9.9565061	9.6729468	10.3270532	10.0434939	10 3705471	47
14	9.6297211	9.9564466	9.6732745	10.3267255	10.0435534	10.3702789	46
15	9 6299892	9 9563870	9.6736020	10 3263980	10.0436130	10.3700110	45
16	9 6302568	9.9563274	9.6739294	10 3260706	10 0436726	10.3697432	44
17	9.6305243	9.9562678	9 6742566	10.3257434	10 0437322	10 3694757	43
18	9 6307917	9 9562081	9 6745836	10.3254164	10 0437919	10 3692083	42
19	9.6310589	9.9561483	9.6749105	10 3250895	10.0438517	10.3689411	41
20	9.6313258	9 9560886	9 6752372	10.3247628	10.0439114	10.3686742	40
21	9 6315926	9.9560287	9.6755638	10.3244362	10.0439713	10.3684074	39
22	9 6318591	9.9559689	9.6758903	10.3241097	10.0440311	10.3681409	38
23	9 6321255	9.9559089	9.6762165	10.3237835	10.0440911	10.3678745	37
24	9.6323916	9 9558490	9.6765426	10.3234574	10.0441510	10 3676084	36
25	9 6326576	9.9557890	9 6768686	10 3231314	10.0442110	10 3673424	35
26	9.6329233	9.9557289	9.6771944	10.3228056	10.0442711	10 3670767	34
27	9.6331889	9.9556688	9 6775201	10.3224799	10 0443312	10.3668111	33
28	9.6334542	9.9556087	9.6778456	1 .3221541	10.0443913	10.3665458	32
29	9 6337194	9 9555485	9 6781709	10.3218291	10.0444515	10.3662806	31
30	9 6339844	9.9554882	9.6784961	10.3215039	10 0445118	10.3660156	30
M		Sine.		Tang.		Secant	M

64 Degrees.

25 Degrees.

M	Sine.		Tang		Secant		M
30	9.6339844	9.9554882	9 6731961	10 3215039	10.0445118	10.3660156	30
31	9 6342491	9.9554283	9.6788211	10.3211789	10.0445720	10.3657509	29
32	9.6345137	9 9553676	9.6791460	10.3208540	10 0446324	10.3654863	28
33	9 6347782	9.9553073	9 6794708	10.3205292	10.0446927	10 3652220	27
34	9.6350422	9.9552469	9 6797953	10.3202047	10.0447531	10136493578	26
35	9.6353062	9 9551864	9.6801198	10.3198802	10 0448136	10.3646938	25
36	9.6355699	9.9551259	9.6804440	10.3195560	10 0448741	10 3644301	24
37	9.6358335	9.9550653	9.6807682	10.3192318	10.0449347	10 3641665	23
38	9.6360969	9.9550047	9 6810921	10.3189079	10 0449953	10 3639031	22
39	9.6363601	9.9549441	9 6814160	10.3185840	10.0450559	10 3636399	21
40	9.6366231	9 9548834	9 6817396	10.3182604	10.0451166	10.3633762	20
41	9.6368859	9.9548227	9 6820632	10 3179368	10 0451773	10.3631141	19
42	9 6371484	9.9547619	9.6823865	10 3176135	10 0452381	10.3628516	18
43	9 6374108	9.9547011	9.6827098	10.3172902	10.0452989	10.3625892	17
44	9 6376731	9.9546402	9.6830328	10.3169672	10 0453589	10.3623269	16
45	9.6379351	9.9545793	9.6833557	10.3165443	10.0454207	10 3620649	15
46	9.6381969	9.9545184	9.6836785	10.3163215	10.0454816	10 3618031	14
47	9.6384585	9 9544574	9.6840011	10.3159989	10 0455426	10.3615415	13
48	9.6387199	9.9543963	9.6843236	10.3156764	10.0456037	10.3612801	12
49	9.6389812	9.9543352	9 6846459	10 3153541	10.0456648	10.3610183	11
50	9.6392422	9.9542741	9.6849681	10.3150319	10.0457259	10.3607578	10
51	9.6395030	9 9542129	9.6852901	10.3147099	10.0457871	10 3604970	9
52	9.6397637	9.9541517	9.6856120	10 3143880	10.0458483	10.3602363	8
53	9.6400241	9 9540904	9 6859338	10.3140662	10.0459096	10.3599759	7
54	9.6402844	9.9540291	9 6862553	10 3137447	10 0459709	10.3597156	6
55	9.6405445	9.9539677	9.6865768	10 3134232	10.0460323	10.3594555	5
56	9.6408044	9.9539063	9 6868981	10.3131019	10.0460937	10.3591956	4
57	9 6410640	9.9538448	9.6872192	10.3127808	10.0461552	10.3589360	3
58	9.6413235	9.9537833	9.6875402	10 3124598	10 0462167	10.3586765	2
59	9.6415828	9.9537218	9 6878611	10.3121389	10.0462782	10.3584172	1
60	9 6418420	9.9536602	9 6881818	10.3118182	10 0463398	10 3581580	0
		Sine.		Tang.		Secant	M

64 Degrees.

A Table of Artificial Sines,

26 Degrees.

M	Sine.		Tang		Secant		M
0	9.6418420	9.9536602	9.6881818	10.3118182	10.0463598	10.3581580	60
1	9.6421009	9.9535985	9.6885223	10.3114977	10.0464015	10.3578991	59
2	9.6423595	9.9535369	9.6888627	10.3111773	10.0464631	10.3576404	58
3	9.6426182	9.9534751	9.6892030	10.3108570	10.0465249	10.3573818	57
4	9.6428765	9.9534134	9.6895431	10.3105369	10.0465866	10.3571235	56
5	9.6431347	9.9533515	9.6897831	10.3102169	10.0466485	10.3568653	55
6	9.6433926	9.9532897	9.6901030	10.3098970	10.0467103	10.3566074	54
7	9.6436504	9.9532278	9.6904226	10.3095774	10.0467722	10.3563496	53
8	9.6439080	9.9531658	9.6907422	10.3092573	10.0468342	10.3560920	52
9	9.6441654	9.9531038	9.6910616	10.3089384	10.0468962	10.3558346	51
10	9.6444226	9.9530418	9.6913807	10.3086191	10.0469582	10.3555774	50
11	9.6446796	9.9529797	9.6917000	10.3083000	10.0470203	10.3553204	49
12	9.6449365	9.9529175	9.6920189	10.3079811	10.0470825	10.3550635	48
13	9.6451931	9.9528553	9.6923378	10.3076622	10.0471447	10.3548069	47
14	9.6454496	9.9527931	9.6926565	10.3073435	10.0472069	10.3545504	46
15	9.6457058	9.9527308	9.6929750	10.3070250	10.0472692	10.3542942	45
16	9.6459619	9.9526685	9.6932934	10.3067066	10.0473315	10.3540381	44
17	9.6462178	9.9526061	9.6936117	10.3063883	10.0473939	10.3537822	43
18	9.6464735	9.9525437	9.6939298	10.3060702	10.0474563	10.3535265	42
19	9.6467290	9.9524813	9.6942478	10.3057522	10.0475187	10.3532710	41
20	9.6469844	9.9524188	9.6945656	10.3054344	10.0475812	10.3530156	40
21	9.6472395	9.9523562	9.6948833	10.3051167	10.0476438	10.3527605	39
22	9.6474945	9.9522936	9.6952009	10.3047991	10.0477064	10.3525055	38
23	9.6477492	9.9522310	9.6955183	10.3044817	10.0477690	10.3522508	37
24	9.6480038	9.9521683	9.6958355	10.3041645	10.0478317	10.3519962	36
25	9.6482582	9.9521055	9.6961527	10.3038473	10.0478945	10.3517418	35
26	9.6485124	9.9520428	9.6964697	10.3035303	10.0479572	10.3514876	34
27	9.6487665	9.9519799	9.6967865	10.3032135	10.0480201	10.3512335	33
28	9.6490203	9.9519171	9.6971032	10.3028968	10.0480829	10.3509797	32
29	9.6492740	9.9518541	9.6974198	10.3025802	10.0481459	10.3507260	31
30	9.6495274	9.9517912	9.6977363	10.3022637	10.0482088	10.3504726	30
		Sine.		Tang.		Secant	M

63 Degrees.

26 Degrees.

M	Sine.		Tang		Secant		M
30	9·6495274	9·9517912	9·6977363	10 3022637	10 0482088	10 3504726	30
31	9·6497807	9·9517252	9 6980526	10 3019474	10 0482718	10·3502193	29
32	9·6500338	9·9516651	9·6983687	10·3016313	10·0483349	10 3499662	28
33	9 650·868	9·9516020	9·6986847	10·3013153	10·0483980	10·3497132	27
34	9·6503395	9·9515389	9·6990006	10·3009994	10·0484611	10 3494605	26
35	9·6507920	9·9514757	9 6993164	10·3006836	10 0485243	10·3492080	25
36	9 6510444	9 9514124	9 6996322	10 3003680	10·0485876	10 3489556	24
37	9·6512966	9 9513492	9·6999474	10·3000526	10·0486508	10 3487034	23
38	9·6515486	9·9512858	9·7002628	10·2997372	10·0487142	10234884514	22
39	9 6518004	9 9512224	9 7005780	10·2994220	10 0487776	10·3481996	21
40	9 6520521	9·9511590	9 7008930	10 2991070	10·0488410	10 3479479	20
41	9·6523035	9·9510956	9·7012080	10·2987920	10 0489044	10 3476965	19
42	9·6525548	9·9510320	9·7015227	10·2984773	10·0489680	10 3474452	18
43	9·6528059	9 950·685	9·7018374	10 2981626	10 0490315	10·3471941	17
44	9 6532568	9·9509049	9·7021519	10·2978481	10 0490951	10·3469432	16
45	9·6533075	9·9508412	9·7024665	10 2975337	10·0491588	10 3466925	15
46	9·6535581	9 9507775	9·7027805	10·2972195	10·0492225	10 3464419	14
47	9·6538084	9·9507138	9 7030946	10·2969054	10 0492862	10·3461916	13
48	9 6540586	9·9506500	9·7034086	10 2965914	10·0493500	10 3459414	12
49	9·6543086	9 9505861	9 7037225	10·2962775	10 0494139	10 3456914	11
50	9 6545584	9·9505223	9 7040362	10 2959638	10 0494777	10·3454416	10
51	9·6548081	9·9504583	9·7043497	10 2956503	10·0495417	10 3451919	9
52	9·6550575	9 9503944	9 7046632	10·2953368	10·0496056	10·3449425	8
53	9·6553065	9·9503303	9 7049765	10 2950235	10004496697	10 3446932	7
54	9 6555559	9·9502663	9 7052897	10·2947103	10 0497337	10·3444441	6
55	9·6558048	9 9502022	9·7056027	10·2943973	10·0497978	10·3441952	5
56	9·6560536	9 9501380	9 7059156	10 2940844	10·0498620	10·3439404	4
57	9 6563021	9 9500738	9 7062284	10 2937716	10·0499262	10 3436979	3
58	9·6565505	9·9500095	9 7·65410	10·2934590	10 0499905	10 3434495	2
59	9 6567987	9·9499452	9 7068535	10·2931465	10·0500543	10·3432013	1
60	9·6570468	9·9498809	9·7071659	10·2928341	10·0501191	10·3429532	0
		Sine.		Tang		Secant	M

63 Degrees.

A Table of Artificial Sines,

27 Degrees.

M	Sine.		Tang		Secant		M
0	9·6570368	9·9438809	9·7071657	10·2918341	10·2501191	10·3425532	60
1	9·6572946	9·9438165	9·7074781	10·2925219	10·2501835	10·3427054	59
2	9·6575523	9·9437521	9·7077902	10·2932098	10·2502479	10·3428577	58
3	9·6578098	9·9436876	9·7081022	10·2938978	10·2503124	10·3430102	57
4	9·6580671	9·9436230	9·7084141	10·2945859	10·2503770	10·3431629	56
5	9·6583242	9·9435585	9·7087258	10·2952742	10·2504415	10·3433158	55
6	9·6585812	9·9434938	9·7090374	10·2959626	10·2505062	10·3434688	54
7	9·6587380	9·9434291	9·7093488	10·2966512	10·2505708	10·3436220	53
8	9·6590946	9·9433645	9·7096601	10·2973399	10·2506355	10·3437754	52
9	9·6593510	9·9432997	9·7099713	10·2980287	10·2507003	10·3439290	51
10	9·6596073	9·9432349	9·7102824	10·2987176	10·2507651	10·3440827	50
11	9·6598634	9·9431700	9·7105933	10·2994067	10·2508300	10·3442367	49
12	9·6601193	9·9431051	9·7109041	10·3000959	10·2508949	10·3443907	48
13	9·6603750	9·9430402	9·7112148	10·3007852	10·2509598	10·3445450	47
14	9·6606305	9·9429752	9·7115254	10·3014746	10·2510248	10·3446995	46
15	9·6608859	9·9429101	9·7118358	10·3021642	10·2510899	10·3448541	45
16	9·6611411	9·9428450	9·7121461	10·3028539	10·2511550	10·3450089	44
17	9·6613961	9·9427799	9·7124562	10·3035438	10·2512201	10·3451639	43
18	9·6616510	9·9427147	9·7127662	10·3042338	10·2512853	10·3453190	42
19	9·6619057	9·9426495	9·7130761	10·3049239	10·2513505	10·3454743	41
20	9·6621601	9·9425842	9·7133859	10·3056141	10·2514158	10·3456298	40
21	9·6624145	9·9425189	9·7136956	10·3063044	10·2514811	10·3457855	39
22	9·6626686	9·9424535	9·7140051	10·3069949	10·2515465	10·3459414	38
23	9·6629226	9·9423881	9·7143145	10·3076855	10·2516119	10·3460974	37
24	9·6631764	9·9423227	9·7146237	10·3083763	10·2516773	10·3462536	36
25	9·6634300	9·9422572	9·7149329	10·3090671	10·2517428	10·3464100	35
26	9·6636833	9·9421916	9·7152419	10·3097581	10·2518084	10·3465665	34
27	9·6639365	9·9421260	9·7155508	10·3104492	10·2518740	10·3467232	33
28	9·6641896	9·9420604	9·7158595	10·3111405	10·2519396	10·3468801	32
29	9·6644426	9·9419947	9·7161682	10·3118318	10·2520053	10·3470372	31
30	9·6646954	9·9419289	9·7164767	10·3125233	10·2520711	10·3471944	30
′		Sine.		Tang		Secant	M

62 Degrees.

27 Degrees.

M	Sine.		Tang		Secant		M
30	9·6544256	9·9179283	9·7164797	10·2835233	10·0520711	10·3355944	30
31	9·6549402	9·9178631	9·7167851	10·2832149	10·0521363	10·3353518	29
32	9·6548526	9·9177973	9·7170933	10·2829067	10·0522027	10·3351094	28
33	9·6551329	9·9177314	9·7174014	10·2825986	10·0522686	10·3348671	27
34	9·6553743	9·9176655	9·7177094	10·2822906	10·0523345	10·3346251	26
35	9·6556168	9·9175995	9·7180173	10·2819827	10·0524005	10·3343832	25
36	9·6558586	9·9175335	9·7183251	10·2816749	10·0524665	10·3341414	24
37	9·6561001	9·9174674	9·7186327	10·2813673	10·0525326	10·3338993	23
38	9·6563415	9·9174013	9·7189402	10·2810598	10·0525987	10·3336585	22
39	9·6565828	9·9173352	9·7192476	10·2807524	10·0526648	10·3334172	21
40	9·6568238	9·9172689	9·7195549	10·2804451	10·0527311	10·3331762	20
41	9·6570647	9·9172027	9·7198620	10·2801380	10·0527973	10·3329353	19
42	9·6573054	9·9171364	9·7201690	10·2798310	10·0528636	10·3326946	18
43	9·6575459	9·9170700	9·7204759	10·2795241	10·0529300	10·3324541	17
44	9·6577863	9·9170036	9·7207827	10·2792173	10·0529964	10·3322137	16
45	9·6580265	9·9169372	9·7210893	10·2789107	10·0530628	10·3319735	15
46	9·6582665	9·9168707	9·7213958	10·2786042	10·0531293	10·3317335	14
47	9·6585064	9·9168043	9·7217022	10·2782978	10·0531958	10·3314936	13
48	9·6587461	9·9167376	9·7220085	10·2779915	10·0532624	10·3312539	12
49	9·6589856	9·9166710	9·7223147	10·2776853	10·0533290	10·3310144	11
50	9·6592250	9·9166043	9·7226207	10·2773793	10·0533957	10·3307750	10
51	9·6594642	9·9165376	9·7229266	10·2770734	10·0534624	10·3305358	9
52	9·6597032	9·9164708	9·7232324	10·2767676	10·0535292	10·3302968	8
53	9·6599420	9·9164040	9·7235381	10·2764619	10·0535960	10·3300580	7
54	9·6701807	9·9163371	9·7238436	10·2761564	10·0536629	10·3298193	6
55	9·6704192	9·9162702	9·7241490	10·2758510	10·0537298	10·3295808	5
56	9·6706576	9·9162032	9·7244543	10·2755457	10·0537968	10·3293424	4
57	9·6708958	9·9161362	9·7247595	10·2752405	10·0538638	10·3291042	3
58	9·6711338	9·9160692	9·7250646	10·2749354	10·0539308	10·3288662	2
59	9·6713716	9·9160021	9·7253695	10·2746305	10·0539979	10·3286284	1
60	9·6716093	9·9159349	9·7256741	10·2743256	10·0540651	10·3283907	0
M		Sine.		Tang		Secant	M

62 Degrees.

A Table of Artificial Sines,

28 Degrees.

M	Sine.		Tang		Secant		M
0	9 6716093	9 9459349	9·7256744	10 2743256	10·0542651	10 3283907	60
1	9·6718463	9 9458677	9·7259791	10 2740209	10·0541323	10·3281532	59
2	9·6720841	9 9458005	9 7262836	10·2737163	10·0541995	10·3279159	58
3	9 6723213	9·9457332	9 7265881	10 2734119	10·0542668	10·3276787	57
4	9·6725583	9·9456659	9 7268925	10·2731075	10·0543341	10 3274417	56
5	9 6727952	9·9455985	9·7271967	10·2728033	10·0544015	10·3272048	55
6	9·6730319	9 9455310	9 7275008	10 2724992	10·0544690	10 3269681	54
7	9 6732684	9 9454636	9 7278048	10 2721952	10·0545364	10·3267316	53
8	9·6735047	9·9453960	9·7281087	10·2718913	10 0546040	10·3264953	52
9	9·6737409	9 9453285	9 7284124	10·2715876	10 0546715	10·3262591	51
10	9·6739769	9 9452609	9·7287161	10·2712839	10 0547391	10 3260231	50
11	9·6742128	9·9451932	9 7290196	10·2709804	10·0548065	10·3257872	49
12	9·6744485	9·9451255	9·7293230	10·2706770	10·0548745	10·3255515	48
13	9·6746840	9·9450577	9 7296263	10·2703737	10·0549423	10 3253160	47
14	9 6749194	9·9449899	9·7299295	10 2700705	10 0550101	10·3250806	46
15	9·6751546	9 9449220	9·7302325	10 2697675	10 0550780	10·3248454	45
16	9 6753896	9 9448541	9·7305354	10 2694646	10 0551459	10 3246104	44
17	9·6756245	9 9447862	9·7308383	10·2691617	10·0552138	10·3243756	43
18	9·6758592	9 9447182	9·7311410	10·2688590	10 0552818	10 3241408	42
19	9 6760937	9·9446501	9·7314436	10 2685564	10 0553499	10·3239063	41
20	9·6763281	9·9445821	9·7317460	10·2682540	10 0554179	10·3236719	40
21	9·6765623	9 9445139	9·7320484	10 2679516	10·0554861	10·3234377	39
22	9 6767963	9·9444457	9 7323506	10·2676494	10·0555543	10·3232037	38
23	9·6770302	9·9443775	9·7326527	10 2673473	10·0556225	10·3229698	37
24	9·6772640	9·9443092	9·7329547	10·2670453	10·0556908	10 3227360	36
25	9·6774975	9 9442409	9·7332566	10·2667434	10 0557591	10 3225025	35
26	9·6777309	9·9441725	9 7335584	10·2664416	10·0558275	10 3222691	34
27	9·6779642	9·9441042	9·7338601	10·2661399	10 0558959	10 3220358	33
28	9·6781972	9 9440356	9·7341616	10·2658384	10·0559644	10 3218028	32
29	9·6784301	9 9439671	9·7344631	10 2655369	10 0560329	10·3215699	31
30	9 6786629	9 9438985	9·7347644	10·2652356	10·0561015	10·3213371	30
M		Sine.		Tang.		Secant	M

61 Degrees.

28 Degrees.

M	Sine.		Tang		Secant		M
30	9·6786629	9 9438985	9 7347644	10 2652356	10 0561015	10·3213371	30
31	9·6788955	9 9438299	9·7350656	10·2649344	10 0561701	10·3211045	29
32	9·6791279	9·9437612	9·7353667	10 2646333	10 0562388	10·3208721	28
33	9·6793602	9·9436925	9 7356677	10·2643323	10·0563075	10 3206398	27
34	9·6795923	9·9436238	9·7359685	10·2640315	10·0563762	10·3204077	26
35	9·6798243	9·9435549	9·7362693	10·2637307	10·0564451	10·3201757	25
36	9 6800560	9·9434861	9·7365699	10·2634301	10·0565139	10·3199440	24
37	9·6802877	9 9434172	9·7368705	10·2631295	10·0565828	10·3197123	23
38	9·6805191	9·9433482	9 7371709	10·2628291	10·0566518	10·3194809	22
39	9·6807504	9 9432792	9·7374712	10 2625288	10·0567208	10 3192496	21
40	9 6809816	9·9432102	9 7377714	10·2622286	10 0567898	10·3190184	20
41	9·6812126	9·9431411	9·7380715	10 2619285	10·0568589	10·3187874	19
42	9·6814434	9·9430720	9·7383714	10 2616286	10·0569280	10·3185566	18
43	9 6816741	9·9430028	9·7386713	10·2613287	10·0569972	10·3183259	17
44	9 6819046	9·9429335	9·7389710	10·2610290	10·0570665	10·3180954	16
45	9·6821349	9·9428643	9 7392707	10·2607293	10 0571357	10 3178651	15
46	9·6823651	9 9427949	9 7395702	10·2604298	10 0572051	10·3176349	14
47	9·6825952	9·9427255	9 7398696	10·2601304	10·0572745	10·3174048	13
48	9·6828250	9·9426561	9·7401689	10 2598311	10·0573439	10·3171750	12
49	9·6830548	9·9425866	9 7404681	10·2595319	10·0574134	10·3169452	11
50	9·6832843	9·9425171	9 7407672	10·2592328	10 0574829	10·3167157	10
51	9·6835137	9·9424476	9·7410662	10·2589338	10·0575524	10·3164863	9
52	9·6837430	9 9423779	9·7413650	10·2586350	10·0576221	10·3162570	8
53	9 6839720	9 9423083	9·7416638	10·2583362	10·0576917	10·3160280	7
54	9·6842010	9·9422386	9·7419624	10·2580376	10·0577614	10·3157990	6
55	9·6844297	9·9421688	9·7422609	10·2577391	10 0578312	10 3155703	5
56	9·6846583	9·9420990	9 7425594	10·2574406	10 0579010	10 3153417	4
57	9·6848868	9·9420291	9·7428577	10·2571423	10·0579709	10·3151132	3
58	9 6851151	9 9419592	9·7431559	10·2568441	10·0580408	10·3148849	2
59	9·6853432	9·9418893	9 7434540	10 2565460	10 0581107	10·3146568	1
60	9·6855712	9·9418193	9·7437520	10·2562480	10 0581807	10 3144288	0
M		Sine.		Tang		Secant	M

61 Degrees.

A Table of Artificial Sines,

29 Degrees.

M	Sine.		Tang.		Secant		M
0	9.6855712	9.9418193	9 7437520	10 2562480	10.0081807	10.3144288	60
1	9 6857931	9.9417492	9.7440493	10.2559501	10.0082508	10.3142069	59
2	9 6860267	9.9416791	9 7443476	10.2556524	10.0083209	10.3139733	58
3	9.6862542	9 9416090	9 7446453	10.2553547	10.0083910	10.3137458	57
4	9.6864816	9 9415388	9.7449428	10 2550572	10.0084612	10.3135184	56
5	9.6867088	9.9414685	9.7452403	10.2547597	10.0085315	10 3132912	55
6	9.6869359	9.9413982	9 7455376	10.2544624	10 0086018	10.3130641	54
7	9 6871628	9.9413279	9.7458349	10 2541651	10 0086721	10.3128372	53
8	9.6873895	9 9412575	9.7461320	10.2538680	10 0087425	10 3126105	52
9	9.6876161	9.9411871	9.7464290	10.2535710	10.0088129	10 3123839	51
10	9.6878425	9 9411166	9.7467259	10 2532741	10.0088834	10.3121575	50
11	9.6880688	9.9410461	9 7470227	10.2529773	10.0089539	10.3119312	49
12	9.6882949	9 9409755	9.7473194	10.2526806	10.0090245	10.3117051	48
13	9 6885209	9.9409048	9.7476160	10.2523840	10 0090952	10 3114791	47
14	9.6887467	9 9408342	9 7479125	10.2520875	10.0091658	10.3112533	46
15	9.6889723	9 9407634	9.7482089	10.2517911	10.0092366	10.3110277	45
16	9.6891978	9 9406927	9.7485052	10.2514948	10.0093073	10 3108022	44
17	9.6894232	9 9406219	9.7488013	10.2511987	10.0093781	10 3105768	43
18	9.6896484	9.9405510	9.7490974	10 2509026	10.0094490	10.3103516	42
19	9.6898734	9.9404801	9.7493934	10 2506066	10.0095199	10.3101266	41
20	9.6900983	9.9404091	9.7496892	10 2503108	10.0095909	10 3099017	40
21	9.6903231	9.9403381	9.7499850	10.2500150	10.0096619	10.3096769	39
22	9.6905476	9.9402670	9 7502806	10.2497194	10 0097330	10.3094524	38
23	9 6907721	9.9401959	9.7505762	10.2494238	10.0098041	10.3092279	37
24	9.6909964	9 9401248	9 7508716	10 2491284	10.0098752	10 3090036	36
25	9.6912205	9.9400535	9.7511669	10 2488331	10.0099465	10 3087795	35
26	9 6914445	9.9399823	9.7514622	10.2485378	10.0100177	10.3085555	34
27	9.69 6683	9.9399110	9.7517573	10.2482427	10.0100890	10 3083317	33
28	9.6918919	9.9398396	9.7520523	10.2479477	10 0101604	10.3081081	32
29	9.6921155	9.9397682	9 7523472	10.2476528	10.0102318	10 3078845	31
30	9 6923388	9.9396968	9.7526420	10 2473580	10.0103032	10.3076612	30
M		Sine.		Tang.		Secant	M

60 Degrees.

29 Degrees.

M	Sine		Tang		Secant		M
30	9 6923388	9·9396968	9·7526420	10 2473580	10 0603032	10 3076612	30
31	9·6925620	9·9396253	9·7529368	10·2470633	10·0603747	10·3074380	29
32	9·6927851	9 9395537	9·7532314	10·2467686	10·0604463	10·3072149	28
33	9·6930080	9 9394821	9·7535259	10·2464741	10 0605179	10 3069919	27
34	9·6932308	9·9394105	9·7538203	10·2461797	10·0605895	10·3067692	26
35	9·6934534	9·9393388	9·7541145	10 2458854	10 0606612	10·3065466	25
36	9 6936758	9 9392671	9·7544088	10 2455912	10 0607329	10·3063242	24
37	9 6938981	9 9391953	9 7547029	10·2452971	10 0608047	10·3061019	23
38	9·6941203	9 9391234	9·7549969	10·2450031	10·0608766	10·3058797	22
39	9·6943423	9·9390515	9·7552908	10·2447091	10 0609485	10·3056577	21
40	9·6945642	9·9389796	9·7555846	10·2444154	10·0610204	10·3054358	20
41	9·6947859	9·9389076	9 7558783	10 2441217	10·0610924	10·3052141	19
42	9·6950074	9·9388356	9 7561718	10·2438282	10·0611644	10 3049926	18
43	9·6952288	9 9387635	9·7564653	10·2435347	10 0612365	10·3047712	17
44	9 6954501	9·9386914	9·7567587	10·2432413	10·0613086	10·3045499	16
45	9 6956712	9·9386192	9·7570520	10·2429480	10 0613808	10·3043288	15
46	9 6958922	9·9385470	9·7573452	10·2426548	10·0614530	10 3041078	14
47	9 6961130	9 9384747	9·7576383	10·2423617	10·0615253	10·3038870	13
48	9·6963336	9·9384024	9 7579313	10·2420687	10·0615976	10·3036664	12
49	9 6965541	9·9383300	9·7582242	10·2417758	10·0616700	10·3034459	11
50	9 6967745	9·9382576	9·7585170	10 2414830	10·0617424	10·3032255	10
51	9·6969947	9·9381851	9·7588096	10·2411904	10·0618149	10 3030053	9
52	9·6972148	9 9381127	9·7591022	10·2408978	10·0618874	10·3027852	8
53	9 6974347	9 9380400	9·7593947	10·2406053	10 0619600	10·3025653	7
54	9·6976545	9·9379674	9·7596871	10·2403129	10 0620326	10·3023455	6
55	9·6978741	9·9378947	9·7599794	10·2400206	10 0621053	10. 3021259	5
56	9·6980936	9·9378220	9 7602716	10·2397284	10·0621780	10·3019064	4
57	9·6983129	9·9377492	9 7605637	10 2394363	10 0622508	10·3016871	3
58	9·6985321	9·9376764	9 7608557	10 2391443	10·0623236	10 3014679	2
59	9·6987511	9·9376035	9·7611476	10 2388524	10·0623965	10·3012489	1
60	9·6989700	9 9375306	9·7614394	10·2385606	10·0624694	10·3010300	0
M		Sine.		Tang.		Secant	M

60 Degrees.

A Table of Artificial Sines,

30 Degrees.

M	Sine.		Tang		Secant		M
0	9·6989700	9·9375306	9 7614394	10·2385606	10 0624694	10·3010300	60
1	9 6991887	9·9374577	9 7617311	10·2382689	10·0625423	10·3008113	59
2	9 6994073	9·9373847	9·7620227	10·2379773	10 0626153	10·3005927	58
3	9·6996258	9·9373116	9·7623142	19·2376858	10 0626884	10·3003742	57
4	9·6998441	9·9372385	9 7626056	10·2373944	10·0627615	10·3001559	56
5	9·7000622	9·9371653	9·7628969	10·2371031	10·0628347	10 2999378	55
6	9 7002802	9·9370921	9·7631881	10·2368119	10 0629079	10 2997198	54
7	9·7004981	9·9370189	9·7634792	10 2365208	10 0629811	10·2995019	53
8	9·7007158	9 9369456	9·7637702	10·2362298	10·0630544	10·2992842	52
9	9 7009334	9·9368722	9·7640612	10·2359388	10 0631278	10·2990666	51
10	9·7011508	9·9367988	9·7643520	10·2356480	10·0632012	10·2988492	50
11	9·7013681	9·9367254	9·7646427	10·2353573	10·0632746	10 2986319	49
12	9·7015852	9·9366519	9·7649334	10 2350666	10 0633481	10·2984148	48
13	9 7018022	9·9365783	9·7652239	10 2347761	10·0634217	10·2981978	47
14	9·7020190	9·9365047	9·7655143	10·2344857	10 0634953	10·2979810	46
15	9·7022357	9 9364311	9·7658047	10·2341953	10 0635689	10·2977663	45
16	9·7024523	9 9363574	9 7660949	10·2339051	10 0636426	10·2975477	44
17	9·7026687	9·9362836	9 7663851	10·2336149	10·0637164	10·2973313	43
18	9·7028849	9 9362098	9·7666751	10 2333249	10·0637902	10·2971151	42
19	9·7031011	9 9361360	9 7669651	10·2330349	10 0638640	10·2968989	41
20	9·7033170	9 9360621	9·7672550	10 2327450	10 0639379	10·2966830	40
21	9 7035329	9·9359881	9·7675448	10 2324552	10·0640119	10 2964671	39
22	9·7037486	9·9359141	9 7678344	10·2321656	10 0640859	10·2962514	38
23	9·7039641	9·9358401	9·7681240	10·2318760	10 0641599	10·2960359	37
24	9·7041795	9·9357660	9·7684135	10·2315865	10 0642340	10·2958205	36
25	9 7043947	9·9356918	9·7687029	10 2312971	10 0643082	10 2956052	35
26	9·7046099	9·9356177	9·7689922	10·2310078	10·0643823	10·2953901	34
27	9·7048248	9 9355434	9 7692814	10·2307186	10·0644566	10·2951752	33
28	9·7050397	9·9354691	9·7695705	10·2304295	10·0645309	10·2949603	32
29	9·7052543	9·9353948	9 7698596	10·2301404	10·0646052	10·2947457	31
30	9·7054689	9·9353204	9·7701485	10·2298515	10 0646796	10·2945311	30
		Sine.		Tang.		Secant	M

59 Degrees.

Tangents, and Secants.

30 Degrees.

M	Sine.		Tang		Secant		M
30	9·7054689	9·9353204	9·7701485	10·2298515	10·0646796	10·2945311	30
31	9·7056833	9·9352459	9·7704373	10·2295627	10·0647541	10·2943167	29
32	9·7058975	9·9351715	9·7707261	10·2292739	10·0648285	10·2941025	28
33	9·7061116	9·9350969	9·7710147	10·2289853	10·0649031	10·2938884	27
34	9·7063256	9·9350223	9·7713033	10·2286967	10·0649777	10·2936744	26
35	9·7065394	9·9349477	9·7715917	10·2284083	10·0650523	10·2934606	25
36	9·7067531	9·9348730	9·7718801	10·2281199	10·0651270	10·2932469	24
37	9·7069667	9·9347983	9·7721684	10·2278316	10·0652017	10·2930333	23
38	9·7071801	9·9347235	9·7724566	10·2275434	10·0652765	10·2928199	22
39	9·7073933	9·9346486	9·7727447	10·2272553	10·0653514	10·2926067	21
40	9·7076064	9·9345738	9·7730327	10·2269673	10·0654·62	10·2923936	20
41	9·7078194	9·9344988	9·7733206	10·2266794	10·0655012	10·2921806	19
42	9·7080323	9·9344238	9·7736084	10·2263916	10·0655762	10·2919677	18
43	9·7082450	9·9343488	9·7738961	10·2261039	10·0656512	10·2917550	17
44	9·7084575	9·9342737	9·7741838	10·2258162	10·0657263	10·2915425	16
45	9·7086699	9·9341986	9·7744713	10·2255287	10·0658014	10·2913301	15
46	9·7088822	9·9341234	9·7747588	10·2252412	10·0658766	10·2911178	14
47	9·7090943	9·9340482	9·7750462	10·2249538	10·0659518	10·2909057	13
48	9·7093063	9·9339729	9·7753334	10·2246666	10·0660271	10·2906937	12
49	9·7095182	9·9338976	9·7756206	10·2243794	10·0661024	10·2904818	11
50	9·7097299	9·9338222	9·7759077	10·2240923	10·0661778	10·2902701	10
51	9·7099415	9·9337467	9·7761947	10·2238053	10·0662533	10·2900585	9
52	9·7101529	9·9336713	9·7764816	10·2235184	10·0663287	10·2898471	8
53	9·7103642	9·9335957	9·7767685	10·2232315	10·0664043	10·2896358	7
54	9·7105753	9·9335201	9·7770552	10·2229448	10·0664799	10·2894247	6
55	9·7107863	9·9334445	9·7773418	10·2226582	10·0665555	10·2892137	5
56	9·7109972	9·9333688	9·7776284	10·2223716	10·0666312	10·2890028	4
57	9·7112080	9·9332931	9·7779149	10·2220851	10·0667069	10·2887920	3
58	9·7114186	9·9332173	9·7782012	10·2217988	10·0667827	10·2885814	2
59	9·7116290	9·9331415	9·7784875	10·2215125	10·0668585	10·2883710	1
60	9·7118393	9·9330656	9·7787737	10·2212263	10·0669344	10·2881607	0
		Sine.		Tang.		Secant	M

59 Degrees.

A Table of Artificial Sines,

31 Degrees.

M	Sine.		Tang		Secant		M
0	9·7118393	9·9330656	9·7787737	10·2212262	10·0669344	10·2881607	60
1	9·7120495	9·9329897	9·7790599	10·2209401	10·0670103	10·2879505	59
2	9·7122596	9·9329137	9·7793459	10·2206541	10·0670863	10·2877404	58
3	9·7124695	9·9328376	9·7796318	10·2203682	10·0671624	10·2875305	57
4	9·7126792	9·9327616	9·7799177	10·2200823	10·0672384	10·2873208	56
5	9·7128889	9·9326854	9·7802034	10·2197965	10·0673146	10·2871111	55
6	9·7130983	9·9326092	9·7804891	10·2195109	10·0673908	10·2869017	54
7	9·7133077	9·9325330	9·7807747	10·2192253	10·0674670	10·2866923	53
8	9·7135169	9·9324567	9·7810602	10·2189398	10·0675433	10·2·64831	52
9	9·7137260	9·9323804	9·7813456	10·2186544	10·0676196	10·2862740	51
10	9·7139349	9·9323040	9·7816309	10·2183691	10·0676960	10·2860651	50
11	9·7141437	9·9322276	9·7819162	10·2180838	10·0677724	10·2858563	49
12	9·7143524	9·9321511	9·7822013	10·2177987	10·0678489	10·2856476	48
13	9·7145609	9·9320746	9·7824864	10·2175136	10·0679254	10·2854391	47
14	9·7147693	9·9319980	9·7827713	10·2172287	10·0680020	10·2852307	46
15	9·7149776	9·9319213	9·7830562	10·2169438	10·0680787	10·2850224	45
16	9·7151857	9·9318447	9·7833410	10·2166590	10·0681553	10·2848143	44
17	9·7153937	9·9317679	9·7836258	10·2163742	10·0682321	10·2846063	43
18	9·7156015	9·9316911	9·7839104	10·2160896	10·0683089	10·2843985	42
19	9·7158092	9·9316143	9·7841949	10·2158051	10·0683857	10·2841908	41
20	9·7160168	9·9315374	9·7844794	10·2155206	10·0684626	10·2839832	40
21	9·7162243	9·9314605	9·7847638	10·2152362	10·0685395	10·2837757	39
22	9·7164316	9·9313835	9·7850481	10·2149519	10·0686165	10·2835684	38
23	9·7166387	9·9313065	9·7853323	10·2146677	10·0686935	10·2833613	37
24	9·7168458	9·9312294	9·7856164	10·2143836	10·0687706	10·2831542	36
25	9·7170526	9·9311522	9·7859004	10·2140996	10·0688478	10·2829474	35
26	9·7172594	9·9310750	9·786·844	10·2138156	10·0689250	10·2827406	34
27	9·7174660	9·9309978	9·7864682	10·2135318	10·0690022	10·2825340	33
28	9·7176725	9·9309205	9·7867520	10·2132480	10·0690795	10·2823275	32
29	9·7178789	9·9308432	9·7870357	10·2129643	10·0691568	10·2821211	31
30	9·7180851	9·9307658	9·7873193	10·2126807	10·0692342	10·2819149	30
		Sine.		Tang		Secant	M

58 Degrees.

31 Degrees.

M	Sine.		Tang		Secant		M
30	9·7180651	9·9307653	9·7873193	10·2126807	10·0692342	10·2819149	30
31	9·7182912	9·9306883	9·7876028	10·2123972	10·0693117	10·2817088	29
32	9·7185171	9·9306109	9·7878863	10·2121137	10·0693891	10·2815029	28
33	9·7187430	9·9305333	9·7881696	10·2118304	10·0694667	10·2812970	27
34	9·7189686	9·9304557	9·7884529	10·2115471	10·0695443	10·2810914	26
35	9·7191942	9·9303781	9·7887361	10·2112639	10·0696219	10·2808858	25
36	9·7194196	9·9303004	9·7890192	10·2109808	10·0696996	10·2806804	24
37	9·7196449	9·9302226	9·7893023	10·2106977	10·0697774	10·2804751	23
38	9·7198702	9·9301448	9·7895852	10·2104148	10·0698552	10·2802700	22
39	9·7199350	9·9300670	9·7898681	10·2101319	10·0699330	10·2800650	21
40	9·7201309	9·9299891	9·7901508	10·2098492	10·0700109	10·2798601	20
41	9·7203447	9·9299112	9·7904335	10·2095665	10·0700886	10·2796553	19
42	9·7205493	9·9298332	9·7907161	10·2092839	10·0701668	10·2794507	18
43	9·7207538	9·9297551	9·7909987	10·2090013	10·0702449	10·2792462	17
44	9·7209581	9·9296770	9·7912811	10·2087189	10·0703230	10·2790419	16
45	9·7211623	9·9295989	9·7915635	10·2084365	10·0704011	10·2788377	15
46	9·7213664	9·9295207	9·7918458	10·2081542	10·0704793	10·2786336	14
47	9·7215704	9·9294424	9·7921280	10·2078720	10·0705576	10·2784296	13
48	9·7217742	9·9293641	9·7924101	10·2075899	10·0706359	10·2782258	12
49	9·7219779	9·9292857	9·7926921	10·2073079	10·0707143	10·2780221	11
50	9·7221814	9·9292073	9·7929741	10·2070259	10·0707927	10·2778186	10
51	9·7223848	9·9291287	9·7932560	10·2067440	10·0708711	10·2776152	9
52	9·7225881	9·9290504	9·7935378	10·2064622	10·0709496	10·2774119	8
53	9·7227913	9·9289718	9·7938195	10·2061805	10·0710283	10·2772087	7
54	9·7229943	9·9288932	9·7941011	10·2058989	10·0711068	10·2770057	6
55	9·7231972	9·9288145	9·7943827	10·2056173	10·0711855	10·2768028	5
56	9·7234000	9·9287358	9·7946641	10·2053359	10·0712643	10·2766000	4
57	9·7236026	9·9286571	9·7949455	10·2050545	10·0713429	10·2763974	3
58	9·7238051	9·9285783	9·7952268	10·2047732	10·0714217	10·2761949	2
59	9·7240075	9·9284994	9·7955081	10·2044919	10·0715006	10·2759925	1
60	9·7242097	9·9284205	9·7957892	10·2042108	10·0715795	10·2757903	0
M	Sine.		Tang		Secant		M

58 Degrees.

A Table of Artificial Sines,

32 Degrees.

M	Sine		Tang		Secant		M
0	9 7241037	9 9264205	9 7357892	10 2642108	10.0715745	10.2735953	60
1	9.7244118	9.9263415	9.7360703	10.2639297	10 0716585	10.2735082	59
2	9.7.48138	9.9262625	9 7363513	10 2636487	10.0717375	10 2734212	58
3	9.7248156	9 9261834	9.7366322	10.2633678	10.0718165	10.2733344	57
4	9 7250171	9.9261043	9 7369130	10 2630870	10.0718957	10.2732520	56
5	9 7252180	9.9260251	9 7371938	10.2628062	10.0719749	10.2731811	55
6	9 7254204	9 9259459	9 7374745	10 2625255	10 0720541	10.2730990	54
7	9 7256217	9.9258666	9.7377552	10 2622449	10.0721334	10.2730183	53
8	9 7258229	9.9257873	9.7380356	10.2619644	10 0722127	10 2741771	52
9	9.7260240	9.9277079	9.7953160	10.2016840	10.0722921	10 2739760	51
10	9 7262249	9 9276285	9 7955964	10 2014036	10 0723715	10 2737751	50
11	9 7264257	9.9275490	9 7958767	10.2011233	10 0724510	10.2735743	49
12	9 7266264	9 9274695	9.7961569	10.2008431	10.0725305	10.2733736	48
13	9.7268269	9.9273899	9.7964370	10 2005630	10.0726101	10.2731731	47
14	9.7270273	9.9273103	9.7967170	10.2002830	10.0726897	10 2729727	46
15	9 7272276	9.9272306	9.7969970	10 2000030	10 0727694	10. 727724	45
16	9 7274278	9 9271509	9.8002769	10.1997231	10 0728491	10 2725722	44
17	9 7276278	9.9270711	9 8005567	10.1994433	10.0729289	10.2723722	43
18	9 7278277	9 9269913	9.8008365	10.1991635	10 0730087	10 2721723	42
19	9.7280275	9 9269114	9.8011161	10 1988839	10.0730886	10 2719725	41
20	9.7282271	9.9268314	9 8013957	10.1986043	10.0731686	10 2717729	40
21	9.7284267	9 9267514	9.8016752	10 1983248	10.0732486	10.2715733	39
22	9.7286260	9.9266714	9.8019546	10.1980454	10 0733286	10.2713740	38
23	9.7288253	9.9265913	9 8022340	10.1977660	10.0734087	10.2711747	37
24	9.7290244	9 9265112	9.8025133	10.1974867	10.0734888	10.2709756	36
25	9 7292234	9.9264310	9.8027925	10.1972075	10 0735690	10.2707766	35
26	9.7294223	9.9263507	9.8030716	10.1969284	10.0736493	10.2705777	34
27	9.7296211	9.9262701	9 8033506	10.1966494	10.0737296	10.2703790	33
28	9.7298197	9.9261901	9.8036296	10.1963704	10.0738099	10.2701823	32
29	9.7300182	9.9261096	9 8039085	10.1960915	10.0738904	10.2699818	31
30	9.7302165	9.9260292	9.8041873	10.1958127	10 0739708	10.2697835	30
M	Sine		Tang		Secant		M

57 Degrees.

32 Degrees.

M	Sine.		Tang		Secant		
30	9.7302165	9.9260292	9.8041873	10.1958127	10.0739708	10.2697835	30
31	9.7304148	9.9259487	9.8044661	10.1955339	10.0740513	10.2695852	29
32	9.7306129	9.9258681	9.8047447	10.1952553	10.0741319	10.2693871	28
33	9.7308109	9.9257875	9.8050233	10.1949767	10.0742125	10.2691891	27
34	9.7310087	9.9257069	9.8053019	10.1946981	10.0742931	10.2689913	26
35	9.7312064	9.9256261	9.8055803	10.1944197	10.0743739	10.2687936	25
36	9.7314040	9.9255454	9.8058587	10.1941413	10.0744546	10.2685960	24
37	9.7316015	9.9254646	9.8061370	10.1938630	10.0745354	10.2683985	23
38	9.7317989	9.9253837	9.8064152	10.1935848	10.0746163	10.2682011	22
39	9.7319961	9.9253028	9.8066933	10.1933067	10.0746972	10.2680039	21
40	9.7321932	9.9252218	9.8069714	10.1930286	10.0747782	10.2678068	20
41	9.7323902	9.9251408	9.8072494	10.1927506	10.0748592	10.2676098	19
42	9.7325870	9.9250597	9.8075273	10.1924727	10.0749403	10.2674130	18
43	9.7327837	9.9249786	9.8078052	10.1921948	10.0750214	10.2672163	17
44	9.7329803	9.9248974	9.8080829	10.1919171	10.0751026	10.2670197	16
45	9.7331768	9.9248161	9.8083606	10.1916394	10.0751839	10.2668232	15
46	9.7333731	9.9247349	9.8086383	10.1913617	10.0752651	10.2666269	14
47	9.7335693	9.9246535	9.8089158	10.1910842	10.0753465	10.2664307	13
48	9.7337654	9.9245721	9.8091933	10.1908067	10.0754279	10.2662346	12
49	9.7339614	9.9244907	9.8094707	10.1905293	10.0755093	10.2660386	11
50	9.7341572	9.9244092	9.8097480	10.1902520	10.0755908	10.2658428	10
51	9.7343529	9.9243277	9.8100253	10.1899747	10.0756723	10.2656471	9
52	9.7345485	9.9242461	9.8103025	10.1896975	10.0757539	10.2654515	8
53	9.7347440	9.9241644	9.8105796	10.1894204	10.0758356	10.2652560	7
54	9.7349393	9.9240827	9.8108566	10.1891434	10.0759173	10.2650607	6
55	9.7351345	9.9240110	9.8111336	10.1888664	10.0759990	10.2648655	5
56	9.7353296	9.9239191	9.8114105	10.1885895	10.0760809	10.2646704	4
57	9.7355246	9.9238373	9.8116873	10.1883127	10.0761627	10.2644754	3
58	9.7357195	9.9237554	9.8119641	10.1880359	10.0762446	10.2642805	2
59	9.7359142	9.9236734	9.8122408	10.1877592	10.0763266	10.2640858	1
60	9.7361088	9.9235914	9.8125174	10.1874826	10.0764086	10.2638912	0
		Sine.		Tang		Secant	M

57 Degrees.

A Table of Artificial Sines,

33 Degrees.

M	Sine.		Tang		Secant		M
0	9 7361038	9·9235914	9·8125174	10·1874826	10 0764086	10 2638912	60
1	9·7363032	9·9235093	9·8127939	10 1872061	10 0764907	10 2636968	59
2	9·7364976	9·9234272	9·8130704	10·1869296	10·0765728	10 2635024	58
3	9·7366918	9·9233450	9 8133468	10 1866532	10 0766550	10·2633082	57
4	9·7368859	9 9232628	9·8136231	10·1863769	10·0767372	10·2631141	56
5	9·7370799	9·9231805	9·8138993	10·1861007	10·0768195	10·2629201	55
6	9 7372737	9·9230982	9·8141755	10·1858243	10·0769018	10·2627263	54
7	9·7374675	9·9230158	9·8144516	10·1855484	10 0769842	10·2625325	53
8	9·7376611	9·9229334	9·8147277	10 1852723	10·0770666	10 2623389	52
9	9·7378546	9 9228509	9 8150036	10·1849964	10·0771491	10·2621454	51
10	9·7380479	9 9227684	9·8152795	10·1847205	10 0772316	10·2619521	50
11	9 7382412	9·9226858	9·8155554	10·1844446	10·0773142	10·2617588	49
12	9 7384343	9·9226032	9·8158311	10·1841689	10·0773969	10·2615657	48
13	9 7386273	9·9225205	9·8161068	10 1838932	10·0774795	10·2613727	47
14	9·7388201	9·9224377	9·8163824	10·1836176	10·0775623	10 2611799	46
15	9 7390129	9 9223549	9 8166580	10·1833420	10·0776451	10·2609871	45
16	9·7392055	9·9222721	9 8169335	10·1830665	10·0777279	10·2607945	44
17	9 7393980	9 9221891	9·8172089	10·1827911	10·0778109	10·2606020	43
18	9 7395904	9 9221062	9 8174842	10·1825158	10·0778938	10·2604096	42
19	9·7397827	9 9220232	9 8177595	10·1822405	10·0779768	10·2602173	41
20	9·7399748	9·9219401	9 8180347	10 1819653	10 0780599	10·2600252	40
21	9·7401668	9 9218570	9·8183098	10·1816902	10·0781430	10·2598332	39
22	9 7403587	9·9217738	9·8185849	10·1814151	10 0782262	10 2596413	38
23	9 7405505	9 9216906	9·8188599	10·1811401	10 0783094	10·2594495	37
24	9·7407421	9 9216073	9 8191348	10·1808652	10·0783927	10 2592579	36
25	9·7409337	9·9215240	9·8194096	10 1805904	10 0784760	10·2590663	35
26	9 7411251	9·9214406	9·8196844	10 1803156	10·0785594	10 2588749	34
27	9 7413164	9 9213572	9·8199592	10·1800408	11·0786428	10 2586836	33
28	9·7415075	9·9212737	9·8102338	10·1797662	10 0787263	10 2584925	32
29	9·7416986	9·9211902	9 8105084	10·1794916	10 0788038	10 2583014	31
30	9·7418895	9·9211066	9·8107829	10 1792171	10·0788934	10·2581105	30
		Sine.		Tang		Secant	M

56 Degrees.

33 Degrees.

M	Sine.		Tang		Secant		
30	9·7418695	9·9211056	9·8207829	10 1792171	10 0788914	10 2581139	30
31	9·7420503	9·9210219	9 8210374	10 1789426	10 0789771	10 2579997	29
32	9 7422710	9·9209383	9·8213317	10 1786683	10·0790627	10·2578855	28
33	9·7424616	9·9208555	9 8216260	10·1783940	10·0791445	10·2575384	27
34	9 7426520	9 9207717	9·8218803	10·1781197	10 0792283	10 2573480	26
35	9·7428423	9·9206878	9·8221545	10 1778455	10·0793122	10 2571577	25
36	9 7430325	9·9206039	9 8224286	10·1775714	10·0793961	10·2569675	24
37	9·7432226	9·9205200	9·8227026	10·1772974	10·0794800	10·2567774	23
38	9·7434126	9·9204360	9·8229766	10·1770234	10·0795640	10·2565874	22
39	9 7436024	9 9203519	9·8232505	10·1767495	10·0796481	10·2563976	21
40	9·7437921	9 9202678	9·8235244	10 1764756	10·0797322	10·2562079	20
41	9·7439817	9 9201863	9·8237981	10 1762019	10·0798164	10 2560183	19
42	9·7441712	9·9200994	9·8240719	10 1759281	10 0799006	10·2558288	18
43	9·7443606	9·9200151	9·8243455	10·1756545	10 0799849	10·2556394	17
44	9·7445498	9·9199308	9 8246191	10·1753809	10·0800692	10 2554502	16
45	9·7447390	9·9198464	9·8248926	10·1751074	10·0801536	10 2552610	15
46	9·7449280	9·9197619	9 8251660	10·1748340	10·0802381	10 2550720	14
47	9 7451169	9·9196775	9·8254394	10·1745606	10·0803225	10·2548831	13
48	9 7453056	9·9195929	9·8257127	10·1742873	10 0804071	10·2546944	12
49	9·7454943	9·9195083	9·8259860	10 1740140	10·0804917	10·2545057	11
50	9·7456828	9·9194237	9 8262592	10·1737408	10 0805763	10·2543172	10
51	9 7458712	9·9193390	9 8265323	10·1734677	10 0806610	10·2541288	9
52	9·7460595	9·9192542	9·8268053	10 1731947	10 0807458	10 2539405	8
53	9 7462477	9·9191694	9 8270783	10 1729217	10 0808306	10·2537523	7
54	9·7464358	9·9190845	9·8273513	10 1726487	10·0809155	10·2535642	6
55	9·7466237	9·9189996	9 8276241	10 1723759	10 0810004	10 2533763	5
56	9 7468115	9·9189146	9·8278969	10 1721031	10·0810854	10 2531885	4
57	9·7469992	9 9188296	9 8281696	10·1718304	10 0811704	10·2530008	3
58	9 7461868	9·9187445	9·8284423	10·1715577	10·0812555	10 2528132	2
59	9·7463743	9 9186594	9·8287149	10·1712851	10·0813406	10 2526257	1
60	9·7465617	9 9185742	9·8289874	10·1710126	10 0814258	10 2524383	0
M		Sine.		Tang.		Secant	M

56 Degrees.

A Table of Artificial Sines,

34 Degrees.

M	Sine.		Tang		Secant		
0	9·7475617	9·9186742	9·8289874	10·1701120	10·0814258	10·2524334	60
1	9·7477489	9·9184890	9·8292599	10·1707191	10·0814110	10·2522311	59
2	9·7479360	9·9183037	9·8295323	10·1704977	10·0815963	10·2520040	58
3	9·7481230	9·9183183	9·8298047	10·1701953	10·0816817	10·2518770	57
4	9·7483099	9·9182329	9·8300769	10·1699131	10·0817671	10·2516901	56
5	9·7484967	9·9181475	9·8303492	10·1696308	10·0818525	10·2515033	55
6	9·7486833	9·9180620	9·8306213	10·1693487	10·0819380	10·2513167	54
7	9·7488698	9·9179764	9·8308934	10·1690665	10·0820236	10·2511302	53
8	9·7490562	9·9178908	9·8311654	10·1687845	10·0821092	10·2509438	52
9	9·7492425	9·9178051	9·8314374	10·1685026	10·0821949	10·2507575	51
10	9·7494287	9·9177194	9·8317093	10·1682207	10·0822806	10·2505713	50
11	9·7496148	9·9176336	9·8319811	10·1679389	10·0823664	10·2503852	49
12	9·7498007	9·9175478	9·8322529	10·1676571	10·0824522	10·2501993	48
13	9·7499866	9·9174619	9·8325246	10·1673754	10·0825381	10·2500134	47
14	9·7501723	9·9173760	9·8327963	10·1670937	10·0826240	10·2498277	46
15	9·7503579	9·9172900	9·8330679	10·1668121	10·0827100	10·2496421	45
16	9·7505434	9·9172040	9·8333394	10·1665306	10·0827960	10·2494566	44
17	9·7507287	9·9171179	9·8336109	10·1662491	10·0828821	10·2492713	43
18	9·7509140	9·9170317	9·8338825	10·1659677	10·0829683	10·2490860	42
19	9·7510991	9·9169455	9·8341536	10·1656864	10·0830545	10·2489009	41
20	9·7512842	9·9168593	9·8344249	10·1654051	10·0831407	10·2487158	40
21	9·7514691	9·9167730	9·8346961	10·1651239	10·0832270	10·2485309	39
22	9·7516539	9·9166866	9·8349673	10·1648427	10·0833134	10·2483462	38
23	9·7518386	9·9166002	9·8352384	10·1645616	10·0833998	10·2481615	37
24	9·7520231	9·9165137	9·8355094	10·1642806	10·0834863	10·2479769	36
25	9·7522075	9·9164272	9·8357804	10·1639996	10·0835728	10·2477925	35
26	9·7523919	9·9163406	9·8360513	10·1637187	10·0836594	10·2476081	34
27	9·7525761	9·9162539	9·8363221	10·1634379	10·0837461	10·2474239	33
28	9·7527602	9·9161673	9·8365929	10·1631571	10·0838327	10·2472398	32
29	9·7529442	9·9160805	9·8368636	10·1628764	10·0839196	10·2470558	31
30	9·7531280	9·9159937	9·8371342	10·1625957	10·0840063	10·2468720	30
		Sine.		Tang		Secant	M

55 Degrees.

34 Degrees.

M	Sine		Tang		Secant		M
30	9·7531200	9·9159737	9·8371341	10·1·28657	10·0342035	10·2468720	30
31	9·7533110	9·9159039	9·8374049	10·1625951	10·0340731	10·2466662	29
32	9·7534954	9·9158200	9·8376755	10·1623245	10·0341800	10·2465046	28
33	9·7536732	9·9157350	9·8379460	10·1620540	10·0342670	10·2463210	27
34	9·7538624	9·9156400	9·8382164	10·1617836	10·0343542	10·2461376	26
35	9·7540457	9·9155589	9·8384867	10·1615133	10·0844412	10·2459545	25
36	9·7542288	9·9154718	9·8387571	10·1612429	10·0345282	10·2457712	24
37	9·7544119	9·9153846	9·8390273	10·1609727	10·0846154	10·2455881	23
38	9·7545949	9·9152974	9·8392975	10·1607025	10·0347026	10·2454051	22
39	9·7547777	9·9152101	9·8395676	10·1604324	10·0847897	10·2452223	21
40	9·7549604	9·9151228	9·8398377	10·1601623	10·0348772	10·2450396	20
41	9·7551431	9·9150354	9·8401077	10·1598923	10·0849646	10·2448569	19
42	9·7553256	9·9149479	9·8403776	10·1596224	10·0850521	10·2446744	18
43	9·7555080	9·9148604	9·8406475	10·1593525	10·0851396	10·2444920	17
44	9·7556902	9·9147729	9·8409174	10·1590826	10·0852271	10·2443098	16
45	9·7558724	9·9146852	9·8411871	10·1588129	10·0853148	10·2441276	15
46	9·7560544	9·9145976	9·8414569	10·1585431	10·0854024	10·2439456	14
47	9·7562364	9·9145099	9·8417265	10·1582735	10·0854901	10·2437636	13
48	9·7564182	9·9144221	9·8419961	10·1580039	10·0855779	10·2435818	12
49	9·7565999	9·9143342	9·8422657	10·1577343	10·0856658	10·2434001	11
50	9·7567815	9·9142464	9·8425351	10·1574649	10·0857536	10·2432185	10
51	9·7569630	9·9141584	9·8428046	10·1571954	10·0858416	10·2430370	9
52	9·7571444	9·9140704	9·8430739	10·1569261	10·0859296	10·2428556	8
53	9·7573256	9·9139824	9·8433432	10·1566568	10·0860176	10·2426744	7
54	9·7575068	9·9138943	9·8436125	10·1563876	10·0861057	10·2424932	6
55	9·7576878	9·9138061	9·8438817	10·1561183	10·0861939	10·2423122	5
56	9·7578687	9·9137179	9·8441508	10·1558492	10·0862821	10·2421313	4
57	9·7580495	9·9136296	9·8444199	10·1555801	10·0863704	10·2419505	3
58	9·7582302	9·9135413	9·8446889	10·1553111	10·0864587	10·2417698	2
59	9·7584108	9·9134530	9·8449579	10·1550421	10·0865471	10·2415892	1
60	9·7585913	9·9133645	9·8452268	10·1547732	10·0866355	10·2414087	0
M	Sine.		Tang.		Secant		M

55 Degrees.

A Table of Artificial Sines,

35 Degrees.

M	Sine.		Tang		Secant		M
0	9·7585913	9·9133045	9·8452268	10·1547732	10·0866355	10·2414037	60
1	9 7587717	9 9132760	9·8454956	10 1545044	10 0867240	10·2412283	59
2	9·7589519	9 9131875	9 8457644	10 1542356	10 0868125	10·2410481	58
3	9·7591321	9·9130989	9·8460332	10·1539668	10 0869011	10 2408679	57
4	9·7593121	9·9130102	9·8463018	10·1536982	10 0869898	10 2406879	56
5	9 7594920	9·9129215	9 8465705	10 1534295	10·0870785	10 2405080	55
6	9·7596718	9 9128328	9 8468390	10 1531610	10·0871672	10·2403282	54
7	9 7598515	9 9127440	9 8471075	10·1528925	10 0872560	10·2401485	53
8	9·7600311	9·9126551	9 8473760	10·1526240	10 0873449	10 2399689	52
9	9·7602106	9 9125662	9 8476444	10·1523556	10·0874338	10·2397894	51
10	9·7603899	9 9124772	9·8479127	10 1520873	10·0875228	10·2396101	50
11	9 7605692	9·9123882	9·8481810	10.1518190	10 0876118	10 2394308	49
12	9·7607483	9·9122991	9 8484492	10·1515508	10 0877009	10·2392517	48
13	9·7609274	9·9122099	9 8487174	1·01512826	10·0877901	10·2390726	47
14	9·7611063	9·9121207	9·8489855	1·01510145	10 0878793	10·2388937	46
15	9·7612851	9·9120315	9·8492536	10·1507464	10·0879685	10·2387149	45
16	9·7614638	9 9119422	9·8495216	10·1504784	10·0880578	10 2385362	44
17	9·7616424	9 9118528	9·8497896	10·1502104	10·0881472	10·2383576	43
18	9 7618208	9·9117634	9·8500575	10 1499425	10 0882366	10 2381792	42
19	9·7619992	9 9116739	9 8503253	10·1496747	10·0883261	10·2380008	41
20	9 7621775	9·9115844	9·8505931	10·1494069	10 0884156	10·2378225	40
21	9 7623556	9·9114948	9·8508608	10·1491392	10 0885052	10 2376444	39
22	9 7625337	9 9114051	9·8511285	10.1488715	10·0885949	10 2374663	38
23	9·7627116	9·9113155	9·8513961	10.1486039	10 0886845	10 2372884	37
24	9·7628894	9·9112257	9 8516637	10·1483363	10 0887743	10 2371106	36
25	9 7630 71	9·9111359	9 8519312	10 1480688	10·0888641	10 2369329	35
26	9 7632447	9·9110460	9·8521987	10 1478013	10·0889540	10·2367553	34
27	9 7634222	9·9109561	9·8524661	10·1475339	10 0890439	10·2365778	33
28	9 7635996	9 9108661	9 8527335	10·1472665	10·0891339	10·2364004	32
29	9 7637769	9·9107761	9 8530008	10·1469992	10·0892239	10·2362231	31
30	9 7639540	9 9106860	9 8532680	10·1467320	10·0893140	10 2360460	30
		Sine.		Tang.		Secant	M

54 Degrees.

35 Degrees.

M	Sine.		Tang		Secant		M
30	9.7633540	9.9106860	9.8532680	10.1467320	10.0893140	10.2360460	30
31	9.7641311	9.9105959	9.8535352	10.1464648	10.0894041	10.2358687	29
32	9.7649080	9.9105057	9.8538023	10.1461977	10.0894943	10.2356920	28
33	9.7656849	9.9104155	9.8540694	10.1459306	10.0895846	10.2355151	27
34	9.7664616	9.9103251	9.8543365	10.1456635	10.0896749	10.2353384	26
35	9.7672382	9.9102348	9.8546034	10.1453966	10.0897652	10.2351618	25
36	9.7680147	9.9101444	9.8548704	10.1451296	10.0898556	10.2349853	24
37	9.7687911	9.9100539	9.8551372	10.1448628	10.0899461	10.2348089	23
38	9.7695674	9.9099633	9.8554041	10.1445959	10.0900366	10.2346326	22
39	9.7703436	9.9098728	9.8556708	10.1443292	10.0901272	10.2344564	21
40	9.7711197	9.9097821	9.8559376	10.1440624	10.0902179	10.2342803	20
41	9.7718957	9.9096915	9.8562042	10.1437958	10.0903085	10.2341043	19
42	9.7726715	9.9096007	9.8564708	10.1435292	10.0903993	10.2339285	18
43	9.7734473	9.9095099	9.8567374	10.1432626	10.0904901	10.2337527	17
44	9.7742229	9.9094190	9.8570039	10.1429961	10.0905810	10.2335771	16
45	9.7749985	9.9093281	9.8572704	10.1427296	10.0906719	10.2334015	15
46	9.7757739	9.9092371	9.8575368	10.1424632	10.0907629	10.2332261	14
47	9.7765492	9.9091461	9.8578031	10.1421969	10.0908539	10.2330508	13
48	9.7773244	9.9090550	9.8580694	10.1419306	10.0909450	10.2328756	12
49	9.7780996	9.9089639	9.8583357	10.1416643	10.0910361	10.2327004	11
50	9.7788746	9.9088727	9.8586019	10.1413981	10.0911273	10.2325254	10
51	9.7796494	9.9087814	9.8588680	10.1411320	10.0912186	10.2323506	9
52	9.7804242	9.9086901	9.8591341	10.1408659	10.0913099	10.2321758	8
53	9.7811989	9.9085988	9.8594002	10.1405998	10.0914012	10.2320011	7
54	9.7819735	9.9085073	9.8596661	10.1403339	10.0914927	10.2318265	6
55	9.7827480	9.9084159	9.8599321	10.1400679	10.0915841	10.2316520	5
56	9.7835223	9.9083243	9.8601980	10.1398020	10.0916757	10.2314777	4
57	9.7842966	9.9082327	9.8604638	10.1395362	10.0917673	10.2313034	3
58	9.7850707	9.9081411	9.8607296	10.1392704	10.0918589	10.2311293	2
59	9.7858448	9.9080494	9.8609954	10.1390046	10.0919506	10.2309553	1
60	9.7866187	9.9079576	9.8612610	10.1387390	10.0920424	10.2307813	0
		Sine.		Tang.		Secant	M

54 Degrees.

A Table of Artificial Sines,

36 Degrees.

M	Sine.		Tang		Secant		M
0	9 7692187	9·9079576	9·8612610	10·1387390	10 0920424	10 2307813	60
1	9·7693925	9·9078658	9 8615267	10 1384733	10·0921342	10·2306075	59
2	9·7695662	9 9077742	9 8617923	10·1382077	10 0922260	10·2304338	58
3	9·7697398	9·9076820	9 8620578	10·1379422	10·0923180	10·2302602	57
4	9·7699134	9·9075901	9·8622233	10·1376767	10 0924099	10 2300866	56
5	9 7700868	9·9074980	9·8625887	10·1374113	10·0925020	10·2299132	55
6	9·7702601	9 9074059	9 8628541	10·1371459	10 0925941	10 2297399	54
7	9·7704333	9 9073138	9·8631195	10·1368805	10·0926862	10·2295668	53
8	9·7706063	9 9072216	9·8633848	10 1366152	10·0927784	10·2293937	52
9	9 7707793	9·9071293	9·8636500	10·1363500	10·0928707	10·2292207	51
10	9·7709522	9 9070370	9·8639152	10·1360848	10 0929630	10·2290478	50
11	9·7711249	9·9069446	9 8641803	10·1358197	10·0930554	10 2288751	49
12	9·7712976	9·9068522	9·8644454	10 1355546	10·0931478	10 2287024	48
13	9·7714702	9·9067597	9·8647105	10·1352895	10·0932403	10·2285298	47
14	9 7716426	9·9066671	9·8649755	10·1350245	10·0933329	10·2283574	46
15	9 7718150	9·9065745	9·8652404	10·1347596	10 0934255	10·2281850	45
16	9·7719872	9·9064819	9·8655053	10·1344947	10 0935181	10·2280128	44
17	9 7721593	9·9063892	9·8657702	10·1342298	10·0936108	10·2278407	43
18	9 7723314	9·9062964	9·8660350	10·1339650	10 0937036	10·2276686	42
19	9·7725033	9 9062036	9·8662997	10·1337003	10 0937964	10·2274967	41
20	9·7726751	9·9061107	9·8665644	10·1334356	10 0938893	10 2273249	40
21	9·7728468	9·9060177	9·8668291	10·1331709	10·0939823	10·2271532	39
22	9·7730185	9·9059247	9·8670937	10·1329063	10·0940753	10·2269815	38
23	9·7731900	9 9058317	9 8673583	10·1326417	10·0941683	10 2268100	37
24	9·7733614	9·9057386	9·8676228	10·1323772	10 0942614	10·2266386	36
25	9·7735327	9·9056454	9·8678873	10·1321127	10·0943546	10·2264673	35
26	9·7737039	9·9055522	9·8681517	10·1318483	10·0944478	10·2262961	34
27	9·7738749	9·9054589	9·8684160	10·1315840	10·0945411	10 2261251	33
28	9·7740459	9·9053656	9·8686804	10·1313196	10·0946344	10·2259541	32
29	9·7742168	9·9052722	9 8689446	10 1310554	10 0947278	10·2257832	31
30	9·7743876	9·9051787	9 8692089	10·1307911	10·0948213	10·2256124	30
M		Sine.		Tang.		Secant	M

53 Degrees.

36 Degrees.

M	Sine.		Tang		Secant		M
30	9 7743876	9·9051787	9·8692089	10·1307911	10·0948213	10·2256124	30
31	9·7745583	9·9050852	9 8694731	10·1305269	10 0949148	10 2254417	29
32	9·7747288	9·9049916	9·8697372	10·1302628	10·0950084	10·2252712	28
33	9·7748993	9·9048980	9 8700013	10·1299987	10·0951020	10 2251007	27
34	9·7750697	9·9048043	9·8702653	10·1297347	10 0951957	10·2249303	26
35	9·7752399	9·9047106	9·8705293	10 1294707	10 0952894	10·22 7601	25
36	9 7754101	9 9046168	9 8707933	10·1292067	10·0953832	10 22 5899	24
37	9 7755801	9 9045230	9·8710572	10·1289428	10 0954770	10·2244193	23
38	9·7757501	9·9044291	9·8713210	10·1286790	10 0955709	10 2242493	22
39	9·7759199	9·9043351	9·8715848	10·1284152	10·0956649	10 2240801	21
40	9·7760897	9·9042411	9 8718486	10·1281514	10·0957589	10·2239103	20
41	9·7762593	9 9041470	9·8721123	10·1278877	10 0958530	10 22 [illegible]	19
42	9·7764289	9 9040529	9·8723760	10·1276240	10 0959471	10 [illegible]	18
43	9·7765983	9·9039587	9·8726396	10·1273604	10·0960413	10·2234017	17
44	9·7767676	9·9038644	9·8729032	10·1270368	10 0961356	10·2232324	16
45	9·7769369	9 9037701	9·8731668	10·1268332	10 0962299	10 2230631	15
46	9·7771060	9·9036757	9·8734302	10 1265698	10 0963243	10·2228940	14
47	9·7772750	9·9035813	9·8736937	10·1263063	10·0964187	10·2227250	13
48	9·7774439	9·9034868	9·8739571	10 1260120	10 0965132	10 2225561	12
49	9 7776128	9 9033923	9·8742204	10 1257796	10·0966077	10·2223872	11
50	9·7777815	9 9032977	9·8744838	10 1255162	10 0967023	10·2222185	10
51	9·7779501	9·9032031	9·8747470	10·1252530	10·0967969	10 2220499	9
52	9·7781186	9·9031084	9 8750102	10 12498 8	10 0968916	10 2218814	8
53	9·7782870	9·9030136	9·8752734	10·1247266	10·0969864	10·2217130	7
54	9 7784553	9·9029188	9 8755365	10·1244635	10·0970812	10 2215447	6
55	9·7786235	9·9028239	9·8757996	10·1242004	10 0971761	10·2213756	5
56	9·7787916	9·9027289	9·8760627	10 1239373	10 0972711	10·2212084	4
57	9 7789596	9·9026339	9·8763257	10·1236743	10·0973661	10 2210404	3
58	9·7791275	9 9025389	9·8765886	10·1234114	10·0974611	10·2208725	2
59	9 7792953	9 9024438	9·8768515	10 1231485	10 0975562	10 2207047	1
60	9·7794630	9·9023486	9·8771144	10·1228856	10 0976514	10 2205370	0
		Sine.		Tang		Secant	M

53 Degrees.

A Table of Artificial Sines,

37 Degrees.

	Sine.		Tang		Secant		
0	9.7946320	9.9223486	9.8771144	10.1228856	10.0976514	10.2205370	60
1	9.7956206	9.9225534	9.8773772	10.1226228	10.0977466	10.2203694	59
2	9.7966091	9.9227581	9.8776400	10.1223600	10.0978419	10.2202019	58
3	9.7975955	9.9229628	9.8779027	10.1220973	10.0979372	10.2200345	57
4	9.7985823	9.9231674	9.8781654	10.1218346	10.0980326	10.2198672	56
5	9.7995690	9.9233719	9.8784281	10.1215719	10.0981281	10.2197000	55
6	9.8005571	9.9237764	9.8786907	10.1213093	10.0982236	10.2195329	54
7	9.8016341	9.9241808	9.8789533	10.1210467	10.0983192	10.2193659	53
8	9.8026010	9.9245852	9.8792158	10.1207842	10.0984148	10.2191990	52
9	9.8035677	9.9249895	9.8794782	10.1205218	10.0985105	10.2190323	51
10	9.8045344	9.9253938	9.8797407	10.1202593	10.0986062	10.2188656	50
11	9.8055010	9.9257980	9.8800031	1.0119969	10.0987020	10.2186990	49
12	9.8064675	9.9262021	9.8802654	1.0119734	10.0987979	10.2185325	48
13	9.8076339	9.9266062	9.8805277	10.1194723	10.0988938	10.2183661	47
14	9.8083002	9.9270102	9.8807900	10.1192100	10.0989898	10.2181998	46
15	9.8092564	9.9274142	9.8810522	10.1189478	10.0990858	10.2180336	45
16	9.8102324	9.9278181	9.8813144	10.1186856	10.0991819	10.2178676	44
17	9.8112984	9.9282219	9.8815765	10.1184235	10.0992781	10.2177016	43
18	9.8124643	9.9286257	9.8818386	10.1181614	10.0993743	10.2175357	42
19	9.8136301	9.9290294	9.8821007	10.1178993	10.0994708	10.2173699	41
20	9.8147958	9.9294331	9.8823627	10.1176374	10.0995669	10.2172042	40
21	9.8159614	9.9298367	9.8826246	10.1173754	10.0996633	10.2170386	39
22	9.8171268	9.9302403	9.8828866	10.1171134	10.0997597	10.2168732	38
23	9.8182922	9.9306438	9.8831484	10.1168516	10.0998562	10.2167078	37
24	9.8194575	9.9310472	9.8834103	10.1165897	10.0999528	10.2165425	36
25	9.8206227	9.8994506	9.8836721	10.1163279	10.1000494	10.2163773	35
26	9.8217878	9.8998539	9.8839338	10.1160662	10.1001461	10.2162122	34
27	9.8229528	9.8997572	9.8841956	10.1158044	10.1002428	10.2160472	33
28	9.8241177	9.8996604	9.8844572	10.1155428	10.1003396	10.2158823	32
29	9.8252824	9.8995636	9.8847189	10.1152811	10.1004364	10.2157176	31
30	9.8264471	9.8994667	9.8849805	10.1150195	10.1005333	10.2155529	30
		Sine.		Tang		Secant	M

52 Degrees.

37 Degrees.

M	Sine.		Tang		Secant		
30	9.7844471	9.8994667	9.8849805	10.1150195	10.1005333	10.2155529	30
31	9.7846117	9.8993697	9.8852420	10.1147580	10.1006303	10.2153883	29
32	9.7847762	9.8992727	9.8855035	10.1144965	10.1007273	10.2152238	28
33	9.7849406	9.8991756	9.8857650	10.1142350	10.1008244	10.2150594	27
34	9.7851049	9.8990784	9.8860264	10.1139737	10.1009216	10.2148951	26
35	9.7852691	9.8989812	9.8862878	10.1137122	10.1010188	10.2147309	25
36	9.7854332	9.8988840	9.8865492	10.1134508	10.1011160	10.2145668	24
37	9.7855972	9.8987867	9.8868105	10.1131895	10.1012133	10.2144028	23
38	9.7857611	9.8986893	9.8870718	10.1129282	10.1013107	10.2142389	22
39	9.7859249	9.8985919	9.8873330	10.1126670	10.1014081	10.2140751	21
40	9.7860886	9.8984944	9.8875942	10.1124058	10.1015056	10.2139114	20
41	9.7862522	9.8983968	9.8878554	10.1121446	10.1016032	10.2137478	19
42	9.7864157	9.8982992	9.8881165	10.1118837	10.1017008	10.2135843	18
43	9.7865791	9.8982015	9.8883775	10.1116225	10.1017985	10.2134209	17
44	9.7867424	9.8981038	9.8886386	10.1113614	10.1018962	10.2132576	16
45	9.7869056	9.8980060	9.8888996	10.1111004	10.1019940	10.2130944	15
46	9.7870687	9.8979082	9.8891605	10.1108395	10.1020918	10.2129313	14
47	9.7872317	9.8978103	9.8894214	10.1105786	10.1021897	10.2127683	13
48	9.7873946	9.8977123	9.8896823	10.1103177	10.1022877	10.2126054	12
49	9.7875574	9.8976143	9.8899432	10.1100568	10.1023857	10.2124426	11
50	9.7877202	9.8975162	9.8902040	10.1097060	10.1024838	10.2122798	10
51	9.7878828	9.8974181	9.8904647	10.1095353	10.1025819	10.2121172	9
52	9.7880453	9.8973199	9.8907254	10.1092746	10.1026801	10.2119547	8
53	9.7882077	9.8972216	9.8909861	10.1090139	10.1027784	10.2117923	7
54	9.7883701	9.8971233	9.8912468	10.1087532	10.1028767	10.2116299	6
55	9.7885323	9.8970249	9.8915074	10.1084926	10.1029751	10.2114677	5
56	9.7886944	9.8969265	9.8917679	10.1082321	10.1030735	10.2113056	4
57	9.7888565	9.8968280	9.8920285	10.1079715	10.1031720	10.2111435	3
58	9.7890184	9.8967294	9.8922890	10.1077110	10.1032706	10.2109816	2
59	9.7891802	9.8966308	9.8925494	10.1074506	10.1033692	10.2108198	1
60	9.7893420	9.8965321	9.8928098	10.1071902	10.1034679	10.2106580	0
		Sine.		Tang		Secant	M

52 Degrees.

A Table of Artificial Sines,

38 Degrees.

M	Sine.		Tang		Secant		M
0	9 7893420	9 8965321	9.8928098	10·1071902	10·1034679	10·2106580	60
1	9·7895036	9·8964334	9·8930702	10 1069298	10·1035666	10·2104964	59
2	9·7896652	9·8963346	9 8933306	10·1066694	10·1036654	10 2103348	58
3	9 7898266	9·8962358	9 8935909	10 1064091	10·1037642	10·2101734	57
4	9 7899880	9·8961369	9 8938511	10·1061489	10 1038631	10·2100120	56
5	9·7901493	9·8960379	9·8941114	10·1058886	10·1039621	10·2098507	55
6	9·7903104	9·8959389	9 8943715	10·1056285	10 1040611	10·2096896	54
7	9 7904715	9 8958398	9 8946317	10·1053683	10·1041602	10·2095285	53
8	9·7906325	9·8957406	9·8948918	10·1051082	10·1042594	10·2093675	52
9	9 7907933	9·8956414	9·8951519	10·1048481	10 1043586	10·2092067	51
10	9·7909541	9 8955422	9 8954119	10·1045881	10 1044578	10 2090459	50
11	9·7911148	9·8954429	9·8956719	10·1043281	10 1045572	10 2088852	49
12	9·7912754	9 8953435	9·8959319	10 1040681	10·1046565	10·2087246	48
13	9 7914359	9 8952440	9·8961918	10 1038082	10 1047560	10·2085641	47
14	9 79 5963	9 8951445	9 8964517	10·1035483	10 1048555	10·2084037	46
15	9 7917566	9 8950450	9·8967116	10·1032884	10·1049550	10·2082434	45
16	9·7919168	9 8949453	9·8969714	10·1030286	10·1050547	10·2080832	44
17	9·7920769	9·8948457	9·8972312	10·1027688	10·1051543	10·2079231	43
18	9 7922369	9·8947459	9·8974910	10·1025090	10·1052541	10·2077631	42
19	9·7923968	9 8946461	9 8977507	10·1022493	10·1053539	10·2076032	41
20	9 7925566	9 8945463	9·8980104	10·1019896	10 1054537	10·2074434	40
21	9·7927163	9·8944463	9·8982700	10·1017300	10·1055537	10·2072837	39
22	9 7928760	9 8943464	9·8985296	10 1014704	10·1056536	10·2071240	38
23	9 7930355	9·8942463	9 8987892	10·1012108	10·1057537	10·2069645	37
24	9·7931949	9·8941462	9·8990487	10·1009513	10·1058538	10 2068051	36
25	9·7933543	9 8940461	9·8993082	10·1006918	10·1059539	10 2066457	35
26	9·7935135	9·8939458	9·8995677	10 1004323	10·1060542	10·2064865	34
27	9 7936727	9 8938456	9·8998271	10·1001729	10·1061544	10·2063273	33
28	9 7938317	9 8937452	9·9000865	10 0999135	10 1062548	10·2061683	32
29	9·7939907	9·8936448	9 9003459	10·0996541	10·1063552	10·2060093	31
30	9 7941496	9·8935444	9·9006052	10 0993948	10·1064556	10·2058504	30
		Sine.		Tang		Secant	M

51 Degrees.

38 Degrees.

M	Sine.		Tang		Secant		M
30	9.7911496	9.8935444	9.9066052	10.0393948	10.1264550	10.0258501	30
31	9.7943083	9.8931439	9.9088645	10.0911355	10.1265561	10.0256917	29
32	9.7944672	9.8933433	9.9111237	10.0888763	10.1266567	10.0255330	28
33	9.7946256	9.8932426	9.9133830	10.0866170	10.1267574	10.0253744	27
34	9.7947841	9.8931419	9.9156422	10.0843578	10.1268581	10.0252159	26
35	9.7949425	9.8930412	9.9179013	10.0820987	10.1269588	10.0250575	25
36	9.7951008	9.8929404	9.9201604	10.0798396	10.1270596	10.0248992	24
37	9.7952590	9.8928395	9.9224195	10.0775805	10.1271605	10.0247410	23
38	9.7954171	9.8927385	9.9246786	10.0753214	10.1272615	10.0245829	22
39	9.7955751	9.8926375	9.9269376	10.0730624	10.1273625	10.0244249	21
40	9.7957330	9.8925365	9.9291966	10.0708034	10.1274635	10.0242670	20
41	9.7958909	9.8924354	9.9314555	10.0685445	10.1275646	10.0241091	19
42	9.7960486	9.8923342	9.9337144	10.0662856	10.1276658	10.0239514	18
43	9.7962062	9.8922329	9.9359733	10.0640267	10.1277671	10.0237938	17
44	9.7963638	9.8921316	9.9382321	10.0617679	10.1278684	10.0236362	16
45	9.7965212	9.8920303	9.9404910	10.0595090	10.1279697	10.0234788	15
46	9.7966786	9.8919289	9.9427497	10.0572503	10.1280711	10.0233214	14
47	9.7968359	9.8918274	9.9450085	10.0549915	10.1281726	10.0231641	13
48	9.7969930	9.8917258	9.9472672	10.0527328	10.1282742	10.0230070	12
49	9.7971501	9.8916242	9.9495259	10.0504741	10.1283758	10.0228499	11
50	9.7973071	9.8915226	9.9517845	10.0482155	10.1284774	10.0226929	10
51	9.7974640	9.8914208	9.9540431	10.0459569	10.1285792	10.0225360	9
52	9.7976208	9.8913191	9.9563017	10.0436983	10.1286809	10.0223792	8
53	9.7977775	9.8912172	9.9585603	10.0414397	10.1287828	10.0222225	7
54	9.7979341	9.8911153	9.9608188	10.0391812	10.1288847	10.0220659	6
55	9.7980906	9.8910133	9.9630773	10.0369227	10.1289867	10.0219094	5
56	9.7982470	9.8909113	9.9653357	10.0346643	10.1290887	10.0217530	4
57	9.7984034	9.8908092	9.9675941	10.0324059	10.1291908	10.0215966	3
58	9.7985596	9.8907071	9.9698525	10.0301475	10.1292929	10.0214404	2
59	9.7987158	9.8906049	9.9721109	10.0278891	10.1293951	10.0212842	1
60	9.7988718	9.8905026	9.9743692	10.0256308	10.1294974	10.0211282	0
		Sine.		Tang.		Secant	M

51 Degrees.

A Table of Artificial Sines,

39 Degrees.

M	Sine.		Tang		Secant		M
0	9.7988718	9.8905026	9.9083692	10.0916308	10.1094974	10.2011282	60
1	9.7992275	9.8904273	9.9086275	10.0913725	10.1095997	10.2009722	59
2	9.7995836	9.8902979	9.9088858	10.0911142	10.1097021	10.2008164	58
3	9.7999394	9.8901954	9.9091440	10.0908560	10.1098046	10.2006606	57
4	9.8002951	9.8900329	9.9094022	10.0905978	10.1099071	10.2005049	56
5	9.8006507	9.8899103	9.9096603	10.0903397	10.1100097	10.2003493	55
6	9.8010062	9.8897877	9.9099185	10.0900815	10.1101123	10.2001938	54
7	9.8013616	9.8896650	9.9101766	10.0898234	10.1102150	10.2000384	53
8	9.8017169	9.8895422	9.9104347	10.0895653	10.1103178	10.1998831	52
9	9.8020721	9.8894194	9.9106927	10.0893073	10.1104206	10.1997279	51
10	9.8024272	9.8892965	9.9109507	10.0890493	10.1105235	10.1995728	50
11	9.8027823	9.8891736	9.9112087	10.0887913	10.1106264	10.1994177	49
12	9.8031372	9.8890506	9.9114666	10.0885334	10.1107294	10.1992628	48
13	9.8034921	9.8891675	9.9117245	10.0882755	10.1108325	1.01991079	47
14	9.8038468	9.8890044	9.9119824	10.0880176	10.1109356	1.01989532	46
15	9.8042015	9.8889612	9.9122403	10.0877597	10.1110388	10.1987985	45
16	9.8045561	9.8888580	9.9124981	10.0875019	10.1111420	10.1986439	44
17	9.8049106	9.8887547	9.9127559	10.0872441	10.1112453	10.1984894	43
18	9.8052649	9.8886513	9.9130137	10.0869863	10.1113487	10.1983351	42
19	9.8056192	9.8885479	9.9132714	10.0867286	10.1114521	10.1981808	41
20	9.8059735	9.8884444	9.9135291	10.0864709	10.1115556	10.1980265	40
21	9.8063276	9.8883408	9.9137868	10.0862132	10.1116592	10.1978724	39
22	9.8066816	9.8882372	9.9140444	10.0859556	10.1117627	10.1977184	38
23	9.8070355	9.8881335	9.9143020	10.0856980	10.1118665	10.1975645	37
24	9.8073894	9.8880298	9.9145596	10.0854404	10.1119702	10.1974106	36
25	9.8077431	9.8879260	9.9148171	10.0851829	10.1120740	10.1972569	35
26	9.8080968	9.8878221	9.9150747	10.0849253	10.1121779	10.1971032	34
27	9.8084504	9.8877182	9.9153322	10.0846678	10.1122818	10.1969496	33
28	9.8088038	9.8876142	9.9155896	10.0844104	10.1123858	10.1967962	32
29	9.8091572	9.8875102	9.9158471	10.0841529	10.1124898	10.1966428	31
30	9.8095105	9.8874061	9.9161045	10.0838955	10.1125939	10.1964895	30
M		Sine.		Tang.		Secant	M

50 Degrees.

39 Degrees.

M	Sine.		Tang		Secant		M
30	9 8035105	9 8874051	9 9161645	10 0338955	10.1125939	10 1964895	30
31	9.8036637	9.8873019	9.9163613	10.0336382	10.1126981	10.1963363	29
32	9.8038168	9.8871977	9.9166192	10.0333808	10 1128023	10.1961832	28
33	9.8039699	9.8870934	9.9168705	10.0331235	10.1129066	10.1960301	27
34	9.8041228	9.8869890	9.9171328	10 0328662	10 1130110	10.1958772	26
35	9.8042757	9.8868846	9 9173911	10.0326089	10.1131154	10.1957243	25
36	9.8044284	9.8867801	9.9176483	10 0323517	10.1132199	10.1955716	24
37	9.8045811	9.8866756	9.9179055	10.0320945	10.1133244	10 1954189	23
38	9.8047336	9.8865710	9.9181627	10.0318373	10.1134290	10.1952664	22
39	9.8048861	9.8864663	9 9184198	10.0315802	10.1135337	10.1951139	21
40	9.8050385	9.8863616	9.9186769	10.0313231	10.1136384	10 1949615	20
41	9.8051908	9.8862568	9.9189340	10.0310660	10.1137432	10.1948092	19
42	9.8053430	9.8861519	9.9191911	10 0308089	10.1138481	10.1946570	18
43	9.8054951	9.8860470	9.9194481	10.0305519	10.1139530	10 1945049	17
44	9 8056472	9.8859420	9 9197051	10 0302949	10.1140580	10.1943528	16
45	9.8057991	9.8858370	9.9199621	10.0300379	10.1141630	10.1942008	15
46	9.8059510	9.8857319	9 9202191	10.0297809	10.1142681	10.1940490	14
47	9.8061027	9 8856267	9.9204760	10.0795240	10 1143733	10.1938973	13
48	9.8062544	9.8855215	9.9207329	10.0792671	10.1144785	10.1937456	12
49	9.8064060	9.8854162	9.9209868	10.0790102	10.1145838	10.1935940	11
50	9.8065575	9 8853109	9.9212466	10.0787534	10.1146891	10.1934425	10
51	9 8067089	9 8852055	9.9215034	10.0784966	10 1147945	10.1932911	9
52	9.8068602	9.8851000	9.9217602	10 0782398	10.1149000	10.1931398	8
53	9.8070114	9.8849945	9.9220170	10.0779830	10.1150055	10.1929886	7
54	9.8071626	9 8848889	9.9222737	10.0777263	10.1151111	10.1928374	6
55	9.8073136	9.8847832	9.9225304	10.0774696	10.1152168	10.1926864	5
56	9.8074646	9.8846775	9.9227871	10.0772129	10 1153225	10.1925354	4
57	9.8076154	9.8845717	9.9230437	10 0769563	10.1154283	10.1923846	3
58	9.8077662	9.8844659	9.9233004	10.0766996	10 1155341	10.1922338	2
59	9.8079169	9.8843599	9.9235570	10 0764430	10 1156401	10.1920831	1
60	9.8080675	9.8842540	9.9238135	10.0761865	10.1157460	10.1919325	0
M		Sine.		Tang.		Secant	M

50 Degrees.

A Table of Artificial Sines,

40 Degrees.

M	Sine.		Tang		Secant		M
0	9.8080675	9.8842540	9.9238135	10.0761865	10.1157460	10 1919325	60
1	9 8081180	9.8841479	9.9240701	10.0759299	10.1158521	10.1917820	59
2	9.8083684	9.8840418	9.9243266	10.0756734	10.1159582	10 1916316	58
3	9.8085188	9.8839357	9.9245831	10.0754169	10.1160643	10.1914812	57
4	9.8086690	9.8838294	9.9248396	10.0751604	10 1161706	10.1913310	56
5	9.8088192	9.8837232	9.9250960	10.0749040	10.1162768	10.1911808	55
6	9.8089692	9.8836168	9.9253524	10.0746476	10.1163832	10.1910308	54
7	9.8091192	9.8835104	9 9256088	10.0743912	10 1164896	10.1908808	53
8	9.8092691	9.8834039	9.9258652	10 0741348	10.1165961	10.1907309	52
9	9.8094189	9 8832974	9.9261215	10.0738785	10.1167026	10.1905811	51
10	9.8095686	9.8831908	9.9263778	10.0736222	10.1168092	10.1904314	50
11	9.8097182	9.8830841	9.9266341	10.0733659	10.1169159	10.1902818	49
12	9 8098678	9.8829774	9 9268904	10 0731096	10.1170226	10.1901322	48
13	9.8100172	9.8828706	9 9271466	10.0728534	10.1171294	10.1899828	47
14	9 8101666	9.8827638	9.9274028	10.0725972	10.1172362	10.1898334	46
15	9.8103159	9 8826568	9.9276590	10 0723410	10.1173432	10.1896841	45
16	9 8104650	9.8825499	9.9279152	10.0720848	10.1174501	10.1895350	44
17	9.8106141	9.8824428	9.9281713	10.0718287	10.1175572	10 1893859	43
18	9.8107631	9.8823357	9.9284274	10.0715726	10 1176643	10.1892369	42
19	9.8109121	9.8822285	9.9286835	10.0713165	10.1177715	10.1890879	41
20	9.8110609	9.8821213	9.9289396	10.0710604	10.1178787	10 1889391	40
21	9.8112096	9.8820140	9.9291956	10.0708044	10.1179860	10.1887904	39
22	9.8113583	9.8819067	9.9294516	10.0705484	10.1180933	10.1886417	38
23	9 8115069	9.8817992	9.9297076	10.0702924	10.1182008	10.1884931	37
24	9 8116554	9.8816918	9.9299636	10.0700364	10 1183082	10.1883446	36
25	9.8118038	9.8815842	9.9302195	10.0697805	10.1184158	10.1881962	35
26	9.8119521	9.8814766	9 9304755	10.0695245	10.1185234	10.1880479	34
27	9.8121003	9 8813689	9 9307314	10.0692686	10.1186311	10.1878997	33
28	9.8122484	9.8812612	9.9309872	10.0690128	10.1187388	10.1877516	32
29	9.8123965	9 8811534	9.9312431	10.0687569	10.1188466	10.1876035	31
30	9.8125444	9.8810155	9 9314989	10.0685011	10.1189545	10.1874556	30
M		Sine.		Tang.		Secant	M

49 Degrees.

1

40 Degrees.

M	Sine.		Tang		Secant		M
30	9.8125444	9.8810455	9.9314989	10.0685011	10.1189545	10.1874556	30
31	9.8126323	9.8809376	9.9317547	10.0682453	10.1190624	10.1873077	29
32	9.8128401	9.8808296	9.9320105	10.0679895	10.1191704	10.1871599	28
33	9.8129878	9.8807215	9.9322662	10.0677338	10.1192785	10.1870122	27
34	9.8131354	9.8806134	9.9325220	10.0674780	10.1193866	10.1868646	26
35	9.8132829	9.8805052	9.9327777	10.0672223	10.1194948	10.1867171	25
36	9.8134303	9.8803970	9.9330334	10.0669666	10.1196030	10.1865697	24
37	9.8135777	9.8802887	9.9332890	10.0667110	10.1197113	10.1864223	23
38	9.8137250	9.8801803	9.9335446	10.0664554	10.1198197	10.1862750	22
39	9.8138721	9.8800719	9.9338003	10.0661997	10.1199281	10.1861279	21
40	9.8140192	9.8799634	9.9340559	10.0659441	10.1200366	10.1859808	20
41	9.8141662	9.8798548	9.9343114	10.0656886	10.1201452	10.1858338	19
42	9.8143131	9.8797462	9.9345670	10.0654330	10.1202538	10.1856869	18
43	9.8144600	9.8796375	9.9348225	10.0651775	10.1203625	10.1855400	17
44	9.8146067	9.8795287	9.9350780	10.0649220	10.1204713	10.1853933	16
45	9.8147534	9.8794199	9.9353335	10.0646665	10.1205801	10.1852466	15
46	9.8148999	9.8793110	9.9355889	10.0644111	10.1206890	10.1851001	14
47	9.8150464	9.8792021	9.9358444	10.0641556	10.1207979	10.1849536	13
48	9.8151928	9.8790930	9.9360998	10.0639002	10.1209070	10.1848072	12
49	9.8153391	9.8789840	9.9363552	10.0636448	10.1210160	10.1846609	11
50	9.8154854	9.8788748	9.9366105	10.0633895	10.1211252	10.1845146	10
51	9.8156315	9.8787656	9.9368659	10.0631341	10.1212344	10.1843685	9
52	9.8157776	9.8786563	9.9371212	10.0628788	10.1213437	10.1842224	8
53	9.8159235	9.8785470	9.9373765	10.0626235	10.1214530	10.1840765	7
54	9.8160694	9.8784376	9.9376318	10.0623682	10.1215624	10.1839306	6
55	9.8162152	9.8783281	9.9378871	10.0621129	10.1216719	10.1837848	5
56	9.8163609	9.8782186	9.9381423	10.0618577	10.1217814	10.1836391	4
57	9.8165066	9.8781090	9.9383975	10.0616025	10.1218910	10.1834934	3
58	9.8166521	9.8779994	9.9386527	10.0613473	10.1220006	10.1833479	2
59	9.8167975	9.8778896	9.9389079	10.0610921	10.1221104	10.1832025	1
60	9.8169429	9.8777799	9.9391631	10.0608369	10.1222201	10.1830571	0
M		Sine.		Tang.		Secant	M

49 Degrees.

A Table of Artificial Sines,

41 Degrees.

M	Sine.		Tang		Secant		M
1	9.8169420	9.8777799	9.9391630	10.0608369	10.1222201	10.1830571	60
2	9.8170882	9.8776720	9.9394182	10.0605818	10.1223300	10.1829118	59
	9.8172331	9 8775601	9.9396733	10 0603267	10.1224399	10 1827666	58
3	9 8173785	9 8774501	9 9399284	10 0600716	10 1225499	10.1826215	57
4	9.8175235	9.8773421	9.9401835	10 0598165	10 1226599	10 1824765	56
5	9 8176685	9.8772300	9.9404385	10.0596615	10 1227700	10.1823315	55
6	9.8178133	9.8771198	9.9406936	10.0593064	10.1228802	10.1821867	54
7	9.8179581	9.8770096	9.9409486	10 0590514	10.1229924	10.1820419	53
8	9.8181028	9 8768993	9.9412036	10 0587964	10.1231007	10.1818972	52
9	9.8182474	9.8767889	9 9414585	10.0585415	10 1232111	10 1817526	51
10	9.8183919	9.8766785	9 9417135	10.0582865	10.1233215	10.1816081	50
11	9 8185364	9.8765680	9.9419684	10 0580316	10.1234320	10.1814636	49
12	9 8186807	9.8764574	9.9422233	10 0577767	10 1235426	10 1813193	48
13	9 8188250	9.8763468	9.9424782	10.0575218	10.1236532	10.1811750	47
14	9 8189692	9.8762361	9 9427331	10.0572569	10.1237639	10 1810308	46
15	9.8191133	9 8761253	9 9429879	10.0570121	10.1238747	10 1808867	45
16	9.8192573	9.8760145	9.9432428	10.0567572	10.1239855	10.1807427	44
17	9.8194012	9.8759036	9.9434976	10.0565024	10.1240964	10.1805988	43
18	9.8195450	9 8757927	9 9437524	10 0562476	10.1242073	10.1804550	42
19	9 8196888	9.8756816	9.9440072	10.0559928	10.1243184	10.1803112	41
20	9.8198325	9 8755706	9.9442619	10.0557381	10.1244294	10 1801675	40
21	9.8199761	9.8754594	9.9445166	10.0554834	10.1245406	10 1800239	39
22	9.8201196	9.8753482	9.9447714	10.0552286	10.1246518	10.1798804	38
23	9.8202630	9 8752369	9.9450261	10 0549739	10.1247631	10.1797370	37
24	9.8204063	9 8751256	9.9452807	10.0547193	10.1248744	10.1795937	36
25	9.8205496	9.8750142	9 9455354	10.0544646	10.1249858	10.1794504	35
26	9.8206927	9.8749027	9.9457900	10 0542100	10.1250973	10 1793073	34
27	9.8208358	9.8747912	9.9460447	10.0539553	10.1252088	10.1791642	33
28	9 8209788	9.8746795	9 9462993	10.0537007	10.1253205	10.1790212	32
29	9.8211217	9.8745679	9 9465539	10 0534461	10.1254321	10.1788783	31
30	9 8212646	9.8744561	9.9468084	10.0531916	10.1255439	10 1787354	30
M		Sine.		Tang		Secant	M

48 Degrees.

41 Degrees.

M	Sine.		Tang		Secant		M
30	9.8212646	9.8744561	9 9468048	10 0531916	10.1255439	10 1787354	30
31	9.8214073	9 8743443	9.9470530	10.0529370	10.1256557	10 1785927	29
32	9.8215500	9.8742325	9.9473175	10.0526825	10.1257675	10.1784500	28
33	9.8216926	9 8741205	9.9475720	10.0524280	10 1258795	10.1783074	27
34	9.8218351	9.8740085	9.9478265	10.0521735	10 1259915	10.1781649	26
35	9.8219775	9.8738965	9.9480810	10.0519190	10.1261035	10.1780225	25
36	9.8221198	9.8737844	9.9483355	10.0516645	10.1262156	10.1778802	24
37	9.8222621	9.8736722	9.9485899	10.0514101	10.1263278	10.1777379	23
38	9.8224042	9.8735599	9.9488443	10.0511557	10.1264401	10.1775958	22
39	9.8225463	9.8734476	9 9490987	10.0509013	10 1265524	10.1774537	21
40	9.8226883	9.8733352	9.9493531	10.0506469	10.1266648	10.1773117	20
41	9.8228302	9.8732227	9.9496075	10.0503925	10 1267773	10 1771698	19
42	9.8229721	9.8731102	9.9498619	10 0501381	10.1268898	10 1770279	18
43	9.8231138	9.8729976	9 9501162	10 0498838	10.1270024	10.1768862	17
44	9.8232555	9.8728849	9.9503705	10.0496295	10.1271151	10.1767445	16
45	9.8233971	9.8727722	9.9506248	10.0493752	10 1272278	10.1766025	15
46	9 8235386	9.8726594	9 9508791	10.0491209	10 1273406	10 1764614	14
47	9 8236800	9.8725466	9.9511334	10 0488666	10 1274534	10 1763200	13
48	9.8238213	9 8724337	9.9513876	10.0486124	10.1275663	10 1761787	12
49	9.8239626	9.8723207	9.9516419	10.0483581	10.1276793	10.1760374	11
50	9.8241037	9.8722076	9.9518961	10.0481039	10.1277924	10.1758963	10
51	9 8242448	9.8720945	9.9521503	10 0478497	10.1279055	10.1757552	9
52	9.8243858	9 8719813	9.9524045	10.0475955	10.1280187	10.1756142	8
53	9.8245267	9.8718681	9.9526587	10.0473413	10.1281319	10.1754733	7
54	9.8246676	9 8717548	9 9529128	10.0470872	10.1282452	10.1753324	6
55	9.8248083	9.8716414	9.9531670	10.0468330	10.1283586	10.1751917	5
56	9.8249490	9.8715279	9.9534211	10.0465789	10.1284721	10.1750510	4
57	9 8250896	9 8714144	9 9536752	10 0463248	10.1285856	10.1749104	3
58	9 8252301	9.8713008	9.9539293	10.0460707	10 1286992	10.1747699	2
59	9.8253705	9.8711872	9 9541834	10.0458166	10 1288128	10.1746295	1
60	9 8255109	9 8710735	9.9544374	10.0455626	10.1289265	10.1744891	0
		Sine.		Tang		Secant	M

48 Degrees.

A Table of Artificial Sines,

42 Degrees.

M	Sine.		Tang		Secant		M
0	9 8255109	9 8710735	9.9544374	10.0455626	10.1289265	10.1744891	60
1	9.8256512	9.8709597	9.9546915	10.0453085	10.1290403	10.1743488	59
2	9 8257913	9.8708458	9.9549455	10.0450545	10.1291542	10.1742087	58
3	9.8259314	9.8707319	9.9551995	10 0448005	10.1292681	10.1740686	57
4	9.8260715	9.8706179	9.9554535	10.0445465	10.1293821	10.1739285	56
5	9.8262114	9.8705039	9.9557075	10.0442925	10.1294961	10.1737886	55
6	9 8263512	9.8703898	9.9559615	10 0440385	10 1296102	10.1736488	54
7	9.8264910	9.8702756	9.9562154	10.0437846	10 1297244	10.1735090	53
8	9.8266307	9.8701613	9.9564694	10 0435307	10.1298387	10 1733693	52
9	9 8267703	9.8700470	9 9567233	10 0432767	10.1299530	10.1732297	51
10	9 8269098	9.8699326	9.9569772	10.0430228	10.1300674	10.1730902	50
11	9.8270493	9.8698182	9 9572311	10.0427689	10.1301818	10.1729507	49
12	9.8271887	9.8697037	9.9574850	10.0425150	10.1302963	10.1728113	48
13	9.8273279	9.8695891	9.9577389	10.0422611	10.1304109	10.1726721	47
14	9.8274671	9.8694744	9.9579927	10.0420073	10.1305256	10.1725329	46
15	9.8276063	9.8693597	9 9582465	10.0417535	10.1306403	10.1723937	45
16	9 8277453	9.8692449	9 9585004	10.0414996	10.1307551	10 1722547	44
17	9.8278843	9.8691301	9.9587542	10.0412458	10.1308699	10.1721157	43
18	9.8280231	9.8690152	9 9590080	10 0409920	10.1309848	10 1719769	42
19	9.8281619	9.8689002	9.9592618	10.0407382	10.1310998	10.1718381	41
20	9.8283006	9.8687851	9.9595155	10.0404845	10.1312149	10.1716994	40
21	9.8284393	9.8686700	9.9597693	10.0402307	10.1313300	10.1715607	39
22	9 8285778	9.8685548	9 9600230	10 0399770	10.1314452	10 1714222	38
23	9.8287163	9.8684396	9.9602767	10.0397233	10.1315604	10 1712837	37
24	9 8288547	9.8683242	9.9605305	10.0394695	10.1316758	10.1711453	36
25	9.8289930	9.8682088	9 9607842	10.0392158	10.1317912	10.1710070	35
26	9.8291312	9.8680934	9.9610378	10.0389621	10.1319066	10.1708688	34
27	9 8292694	9.8679779	9.9612915	10.0387085	10.1320221	10.1707306	33
28	9.8294075	9.8678623	9 9615542	10.0384548	10.1321377	10.1705925	32
29	9.8295454	9 8677466	9.9617988	10 0382012	10.1322534	10 1704546	31
30	9.8296833	9 8676309	9 9620525	10.0379475	10.1323691	10.1703167	30
M		Sine.		Tang.		Secant	M

47 Degrees.

42 Degrees.

M	Sine.		Tang		Secant		M
30	9.8296833	9.8676309	9.9620525	10.0379475	10.1323691	10.1703167	30
31	9.8298212	9.8675151	9.9623061	10.0376939	10.1324849	10.1701788	29
32	9.8299589	9.8673992	9.9625597	10.0374403	10.1326008	10.1700411	28
33	9.8300966	9.8672833	9.9628133	10.0371867	10.1327167	10.1699034	27
34	9.8302342	9.8671673	9.9630669	10.0369331	10.1328327	10.1697658	26
35	9.8303717	9.8670512	9.9633204	10.0366796	10.1329488	10.1696283	25
36	9.8305091	9.8669351	9.9635740	10.0364260	10.1330649	10.1694909	24
37	9.8306464	9.8668189	9.9638275	10.0361725	10.1331811	10.1693536	23
38	9.8307837	9.8667026	9.9640811	10.0359189	10.1332974	10.1692163	22
39	9.8309209	9.8665863	9.9643346	10.0356654	10.1334137	10.1690791	21
40	9.8310580	9.8664699	9.9645881	10.0354119	10.1335301	10.1689420	20
41	9.8311950	9.8663534	9.9648416	10.0351584	10.1336466	10.1688050	19
42	9.8313320	9.8662369	9.9650951	10.0349049	10.1337631	10.1686680	18
43	9.8314688	9.8661203	9.9653486	10.0346514	10.1338797	10.1685312	17
44	9.8316056	9.8660036	9.9656020	10.0343980	10.1339964	10.1683944	16
45	9.8317423	9.8658868	9.9658555	10.0341445	10.1341132	10.1682577	15
46	9.8318789	9.8657700	9.9661089	10.0338911	10.1342300	10.1681211	14
47	9.8320155	9.8656531	9.9663623	10.0336377	10.1343469	10.1679845	13
48	9.8321519	9.8655362	9.9666157	10.0333843	10.1344638	10.1678481	12
49	9.8322883	9.8654192	9.9668692	10.0331308	10.1345808	10.1677117	11
50	9.8324246	9.8653021	9.9671225	10.0328775	10.1346979	10.1675754	10
51	9.8325609	9.8651849	9.9673759	10.0326241	10.1348151	10.1674391	9
52	9.8326970	9.8650677	9.9676293	10.0323707	10.1349323	10.1673030	8
53	9.8328331	9.8649504	9.9678827	10.0321173	10.1350496	10.1671669	7
54	9.8329691	9.8648331	9.9681360	10.0318640	10.1351669	10.1670309	6
55	9.8331050	9.8647156	9.9683893	10.0316107	10.1352844	10.1668950	5
56	9.8332408	9.8645981	9.9686427	10.0313573	10.1354019	10.1667592	4
57	9.8333766	9.8644806	9.9688960	10.0311040	10.1355194	10.1666234	3
58	9.8335122	9.8643629	9.9691493	10.0308507	10.1356371	10.1664878	2
59	9.8336478	9.8642452	9.9694026	10.0305974	10.1357548	10.1663522	1
60	9.8337833	9.8641275	9.9696559	10.0303441	10.1358725	10.1662167	0
		Sine.		Tang		Secant	M

47 Degrees.

A Table of Artificial Sines,

43 Degrees.

M	Sine.		Tang		Secant		M
0	9.8337833	9.8641275	9.9696559	10.0303441	10.1358725	10.1662167	60
1	9.8339188	9.8640036	9.9699091	10.0300909	10.1359924	10.1660812	59
2	9.8340541	9.8638917	9.9701624	10.0298376	10.1361083	10.1659459	58
3	9.8341893	9.8637737	9.9704157	10.0295843	10.1362263	10.1658106	57
4	9.8343240	9.8636557	9.9706689	10.0293311	10.1363443	10.1656754	56
5	9.8344597	9.8635376	9.9709221	10.0290779	10.1364624	10.1655403	55
6	9.8345948	9.8634194	9.9711754	10.0288246	10.1365806	10.1654052	54
7	9.8347297	9.8633011	9.9714286	10.0285714	10.1366989	10.1652703	53
8	9.8348646	9.8631828	9.9716818	10.0283182	10.1368172	10.1651354	52
9	9.8349994	9.8630644	9.9719350	10.0280650	10.1369356	10.1650006	51
10	9.8351341	9.8629460	9.9721882	10.0278118	10.1370540	10.1648659	50
11	9.8352688	9.8628274	9.9724413	10.0275587	10.1371726	10.1647312	49
12	9.8354033	9.8627088	9.9726945	10.0273055	10.1372912	10.1645967	48
13	9.8355378	9.8625902	9.9729477	10.0270523	10.1374098	10.1644622	47
14	9.8356722	9.8624714	9.9732018	10.0267992	10.1375286	10.1643278	46
15	9.8358066	9.8623526	9.9734539	10.0265461	10.1376474	10.1641934	45
16	9.8359408	9.8622338	9.9737071	10.0262929	10.1377662	10.1640592	44
17	9.8360750	9.8621148	9.9739602	10.0260398	10.1378852	10.1639250	43
18	9.8362091	9.8619958	9.9742133	10.0257867	10.1380042	10.1637909	42
19	9.8363431	9.8618767	9.9744664	10.0255336	10.1381233	10.1636569	41
20	9.8364771	9.8617576	9.9747195	10.0252805	10.1382424	10.1635229	40
21	9.8366109	9.8616383	9.9749726	10.0250274	10.1383617	10.1633891	39
22	9.8367447	9.8615190	9.9752257	10.0247743	10.1384810	10.1632553	38
23	9.8368784	9.8613997	9.9754787	10.0245213	10.1386003	10.1631216	37
24	9.8370121	9.8612803	9.9757318	10.0242682	10.1387197	10.1629879	36
25	9.8371456	9.8611608	9.9759849	10.0240251	10.1388392	10.1628544	35
26	9.8372791	9.8610412	9.9762379	10.0237621	10.1389588	10.1627209	34
27	9.8374125	9.8609215	9.9764909	10.0235091	10.1390785	10.1625875	33
28	9.8375458	9.8608018	9.9767440	10.0232560	10.1391982	10.1624542	32
29	9.8376790	9.8606821	9.9769970	10.0230030	10.1393179	10.1623210	31
30	9.8378122	9.8605622	9.9772500	10.0227500	10.1394378	10.1621878	30
		Sine.		Tang.		Secant	M

46 Degrees.

43 Degrees.

M	Sine.		Tang		Secant		M
30	9.8378122	9.8605622	9.9772500	10.0227500	10.1394378	10.1621878	30
31	9.8379453	9.8604423	9.9775030	10.0224970	10.1395577	10.1620547	29
32	9.8380783	9.8603223	9.9777560	10.0222440	10.1396777	10.1619217	28
33	9.8382112	9.8602022	9.9780090	10.0219910	10.1397978	10.1617888	27
34	9.8383441	9.8600821	9.9782620	10.0217380	10.1399179	10.1616559	26
35	9.8384769	9.8599619	9.9785149	10.0214851	10.1400381	615231	25
36	9.8386066	9.8598416	9.9787679	10.0212321	10.1401584	10.1613924	24
37	9.8387422	9.8597213	9.9790209	10.0209791	10.1402787	10.1612578	23
38	9.8388747	9.8596009	9.9792738	10.0207262	10.1403991	10.1611253	22
39	9.8390072	9.8594804	9.9795268	10.0204732	10.1405196	10.1609928	21
40	9.8391396	9.8593599	9.9797797	10.0202203	10.1406401	10.1608604	20
41	9.8392719	9.8592393	9.9800326	10.0199674	10.1407607	10.1607281	19
42	9.8394041	9.8591186	9.9802856	10.0197144	10.1408814	10.1605959	18
43	9.8395363	9.8589978	9.9805385	10.0194615	10.1410022	10.1604637	17
44	9.8396684	9.8588770	9.9807914	10.0192086	10.1411230	10.1603316	16
45	9.8398004	9.8587561	9.9810443	10.0189557	10.1412439	10.1601996	15
46	9.8399323	9.8586351	9.9812972	10.0187028	10.1413649	10.1600677	14
47	9.8400642	9.8585141	9.9815501	10.0184499	10.1414859	10.1599358	13
48	9.8401959	9.8583929	9.9818030	10.0181970	10.1416071	10.1598041	12
49	9.8403276	9.8582718	9.9820559	10.0179441	10.1417282	10.1596724	11
50	9.8404593	9.8581505	9.9823087	10.0176913	10.1418495	10.1595407	10
51	9.8405908	9.8580292	9.9825616	10.0174384	10.1419708	10.1594092	9
52	9.8407223	9.8579078	9.9828145	10.0171855	10.1420922	10.1592777	8
53	9.8408537	9.8577863	9.9830673	10.0169327	10.1422137	10.1591463	7
54	9.8409850	9.8576648	9.9833202	10.0166798	10.1423352	10.1590150	6
55	9.8411162	9.8575432	9.9835730	10.0164270	10.1424568	10.1588838	5
56	9.8412474	9.8574215	9.9838259	10.0161741	10.1425785	10.1587526	4
57	9.8413785	9.8572998	9.9840787	10.0159213	10.1427002	10.1586215	3
58	9.8415095	9.8571779	9.9843315	10.0156685	10.1428221	10.1584905	2
59	9.8416404	9.8570561	9.9845844	10.0154156	10.1429439	10.1583596	1
60	9.8417713	9.8569341	9.9848372	10.0151628	10.1430659	10.1582287	0
M		Sine.		Tang.		Secant	M

46 Degrees.

A Table of Artificial Sines,

44 Degrees.

M	Sine		Tang		Secant		M
0	9·8417713	9·8569341	9·9848372	10·0151628	10·1430659	10 1582287	60
1	9·8419021	9 8568121	9·9850900	10·0149100	10 1431879	10·1583979	59
2	9 8420328	9·8566900	9·9853428	10·0146572	10·1433100	10·1579672	58
3	9 8421634	9 8565678	9·9855956	10 0144044	10 1434322	10·1578366	57
4	9 8422939	9·8564455	9·9858484	10·0141516	10·1435545	10 1577061	56
5	9 8424244	9·8563232	9·9861012	10·0138988	10·1436768	10·1575756	55
6	9·8425548	9·8562008	9 9863540	10·0136460	10·1437992	10·1574452	54
7	9 8426851	9·8560784	9·9866068	10·0133932	10 1439216	10.1573149	53
8	9·8428154	9·8559558	9·9868596	10·0131404	10·1440442	10·1571846	52
9	9·8429456	9·8558332	9·9871123	10·0128877	10·1441668	10 1570544	51
10	9·8430757	9·8557106	9·9873651	10.0126349	10·1442894	10 1569243	50
11	9·8432057	9·8555878	9·9876179	10 0123821	10.1444122	10.1567943	49
12	9·8433356	9·8554650	9·9878706	10·0121294	10.1445350	10.1566644	48
13	9.8434655	9 8553421	9·9881234	10·0118766	10·1446579	10 1565345	47
14	9·8435953	9·8552192	9 9883761	10·0116239	10·1447808	10.1564047	46
15	9 8437250	9·8550961	9·9886289	10 0113711	10.1449039	10 1562750	45
16	9·8438547	9·8549730	9·9888816	10·0111184	10 1450270	10·1561453	44
17	9·8439842	9·8548499	9 9891344	10·0108656	10·1451501	10·1560158	43
18	9·8441137	9 8547266	9·9893871	10 0106129	10·1452734	10.1558863	42
19	9 8442432	9 8546033	9·9896399	10·0103601	10·1453967	10.1557568	41
20	9·8443725	9·8544799	9 9898926	10·0101074	10.1455201	10 1556275	40
21	9·8445018	9 8543564	9 9901453	10 0098547	10·1456436	10·1554982	39
22	9 8446310	9 8542329	9·9903981	10 0096019	10·1457671	10·1553690	38
23	9·8447601	9·8541093	9·9906508	10 0093492	10.1458907	10·1552399	37
24	9·8448891	9·8539856	9 9909035	10·0090965	10·1460144	10·1551109	36
25	9 8450181	9 8538619	9 9911562	10·0088438	10 1461381	10.1549819	35
26	9 8451470	9·8537381	9 9914089	10·0085911	10 1462619	10 1548530	34
27	9·8452758	9·8536142	9·9916616	10.0083384	10·1463858	10·1547242	33
28	9·8454045	9·8534902	9·9919143	10.0080857	10 1465098	10·1545955	32
29	9·8455332	9·8533662	9·9921670	10.0078330	10 1466338	10·1544668	31
30	9·8456618	9·8532421	9·9924197	10.0075803	10·1467579	10·1543382	30
M		Sine.		Tang.		Secant	M

45 Degrees.

44 Degrees.

M	Sine.		Tang		Secant		M
30	9.8456618	9.8532421	9.9924197	10.0075803	10.1467579	10.1543382	30
31	9.8457903	9.8531179	9.9926724	10.0073276	10.1468821	10.1542097	29
32	9.8459188	9.8529936	9.9929251	10.0070749	10.1470064	10.1540812	28
33	9.8460471	9.8528693	9.9931778	10.0068222	10.1471307	10.1539519	27
34	9.8461754	9.8527449	9.9934305	10.0065695	10.1472551	10.1538246	26
35	9.8463036	9.8526204	9.9936832	10.0063168	10.1473796	10.1536964	25
36	9.8464318	9.8524959	9.9939359	10.0060641	10.1475041	10.1535682	24
37	9.8465599	9.8523713	9.9941886	10.0058114	10.1476287	10.1534401	23
38	9.8466879	9.8522466	9.9944413	10.0055587	10.1477534	10.1533121	22
39	9.8468158	9.8521218	9.9946940	10.0053060	10.1478782	10.1531842	21
40	9.8469436	9.8519970	9.9949466	10.0050534	10.1480030	10.1530564	20
41	9.8470741	9.8518721	9.9951993	10.0048007	10.1481279	10.1529286	19
42	9.8471991	9.8517471	9.9954520	10.0045480	10.1482529	10.1528009	18
43	9.8473267	9.8516220	9.9957047	10.0042953	10.1483780	10.1526733	17
44	9.8474543	9.8514969	9.9959573	10.0040427	10.1485031	10.1525457	16
45	9.8475817	9.8513717	9.9962100	10.0037900	10.1486283	10.1524183	15
46	9.8477091	9.8512465	9.9964627	10.0035373	10.1487535	10.1522909	14
47	9.8478365	9.8511211	9.9967154	10.0032846	10.1488789	10.1521635	13
48	9.8479637	9.8509957	9.9969680	10.0030320	10.1490043	10.1520363	12
49	9.8480909	9.8508702	9.9972207	10.0027793	10.1491298	10.1519091	11
50	9.8482180	9.8507446	9.9974734	10.0025266	10.1492554	10.1517820	10
51	9.8483450	9.8506190	9.9977260	10.0022740	10.1493810	10.1516550	9
52	9.8484720	9.8504933	9.9979787	10.0020213	10.1495067	10.1515280	8
53	9.8485989	9.8503675	9.9982314	10.0017686	10.1496325	10.1514011	7
54	9.8487257	9.8502417	9.9984840	10.0015160	10.1497583	10.1512743	6
55	9.8488524	9.8501157	9.9987367	10.0012633	10.1498843	10.1511476	5
56	9.8489791	9.8499897	9.9989893	10.0010107	10.1500103	10.1510209	4
57	9.8491057	9.8498637	9.9992420	10.0007580	10.1501363	10.1508943	3
58	9.8492322	9.8497375	9.9994947	10.0005053	10.1502625	10.1507678	2
59	9.8493586	9.8496113	9.9997473	10.0002527	10.1503887	10.1506414	1
60	9.8494850	9.8494850	10.0000000	10.0000000	10.1505150	10.1505150	0
M		Sine.		Tang		Secant	M

45 Degrees.

the Compass) maketh with the Meridian.

NORTH.	SOUTH.	Points.	D.	M.	NORTH.	SOUTH.
		1/4	02	49		
		1/2	05	37		
		3/4	08	26		
North by East	South by East	1	11	15	N. by W.	S. by W.
		1 1/4	14	04		
		1 1/2	16	52		
		1 3/4	19	41		
N. N. E.	S. S. E.	2	22	30	N. N. W.	S. S. W.
		2 1/4	25	19		
		2 1/2	28	07		
		2 3/4	30	56		
N. E. by N.	S. E. by S.	3	33	45	N. W. by N.	S. W. by S.
		3 1/4	36	34		
		3 1/2	39	22		
		3 3/4	42	11		
North-East.	South-East.	4	45	00	North-West	South-West.
		4 1/4	47	49		
		4 1/2	50	37		
		4 3/4	53	26		
N. E. by E.	S. E. by E.	5	56	15	N. W. by W.	S. W. by W.
		5 1/4	59	04		
		5 1/2	61	52		
		5 3/4	64	42		
E. N. E.	E. S. E.	6	67	30	W. N. W.	W. S. W.
		6 1/4	70	19		
		6 1/2	73	07		
		6 3/4	75	56		
East by North	East by South	7	78	45	W. by N.	W. by S.
		7 1/4	81	34		
		7 1/2	84	22		
		7 3/4	87	11		
East.	East.	8	90	00	West.	West.

FINIS.